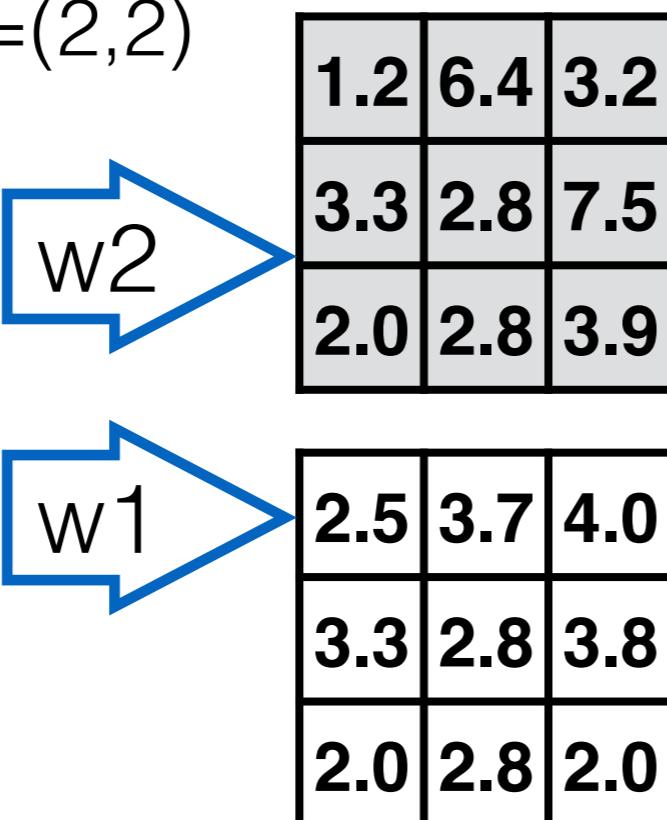


# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

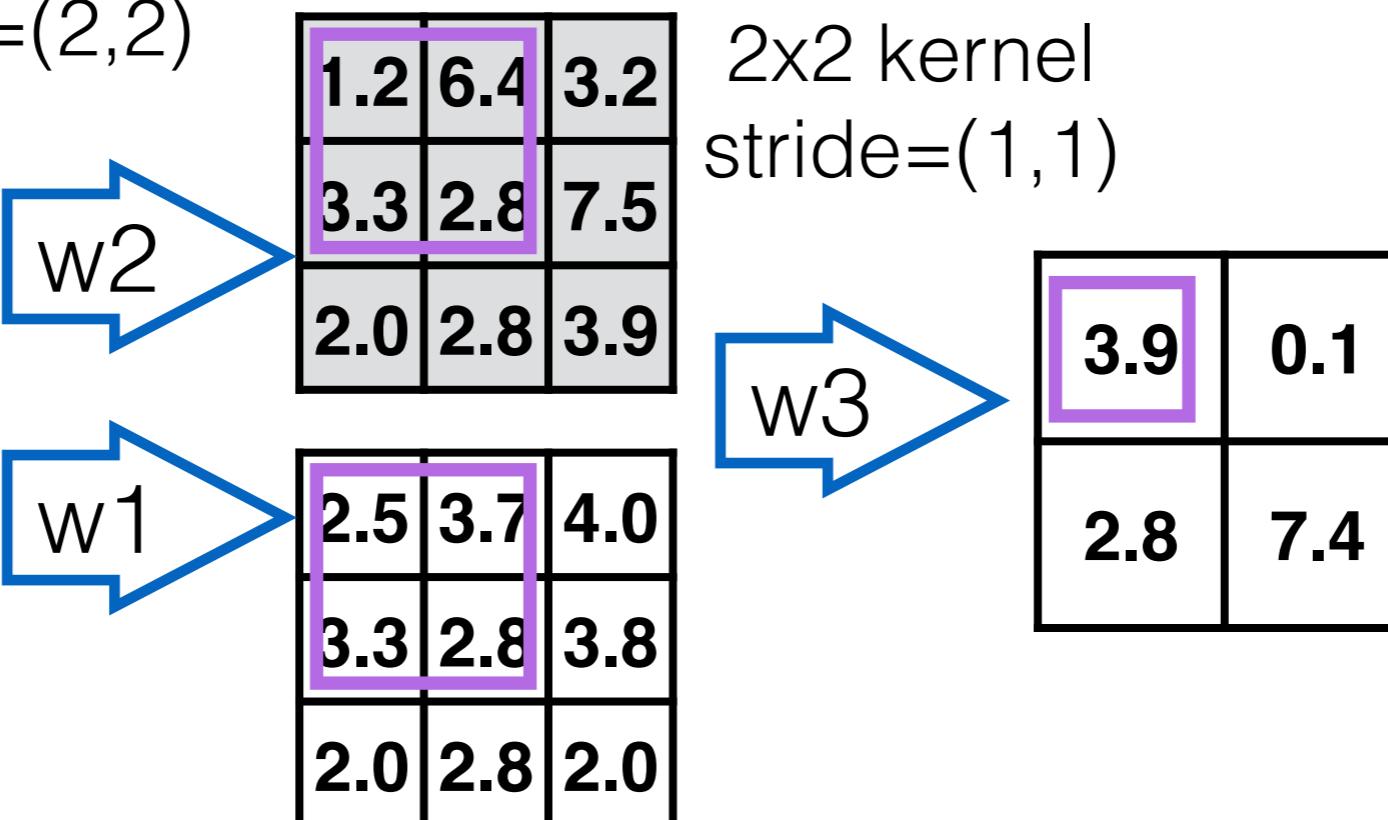
2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

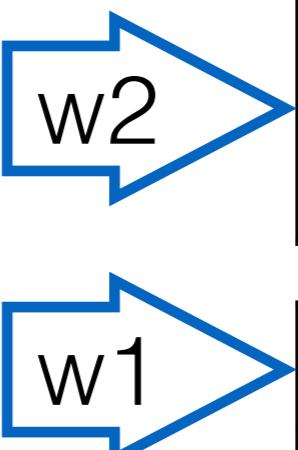
2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



1.2	6.4	3.2
3.3	2.8	7.5
2.0	2.8	3.9

2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0

2x2 kernel  
stride=(1,1)

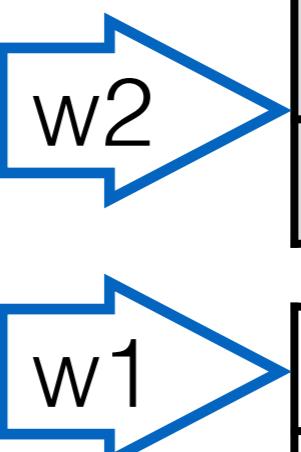


3.9	0.1
2.8	7.4

# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

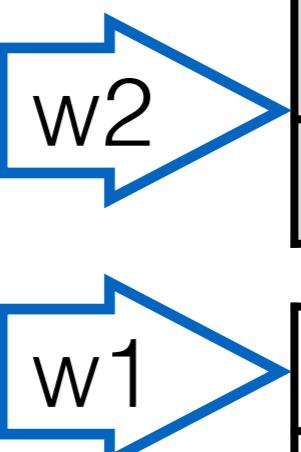
2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



1.2	6.4	3.2
3.3	2.8	7.5
2.0	2.8	3.9

2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0



2x2 kernel  
stride=(1,1)

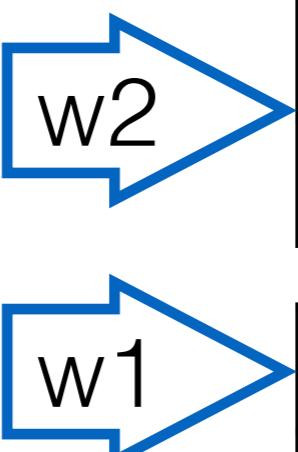


3.9	0.1
2.8	7.4

# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



1.2	6.4	3.2
3.3	2.8	7.5
2.0	2.8	3.9

2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0

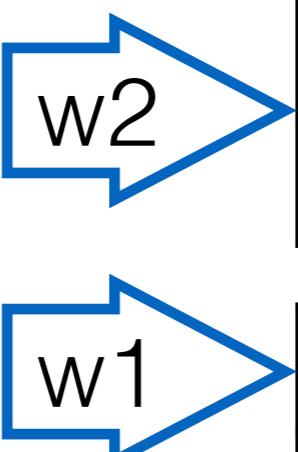
2x2 kernel  
stride=(1,1)

3.9	0.1
2.8	7.4

# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3

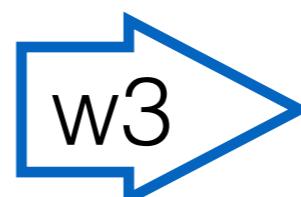


1.2	6.4	3.2
3.3	2.8	7.5
2.0	2.8	3.9

2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0

2x2 kernel  
stride=(1,1)

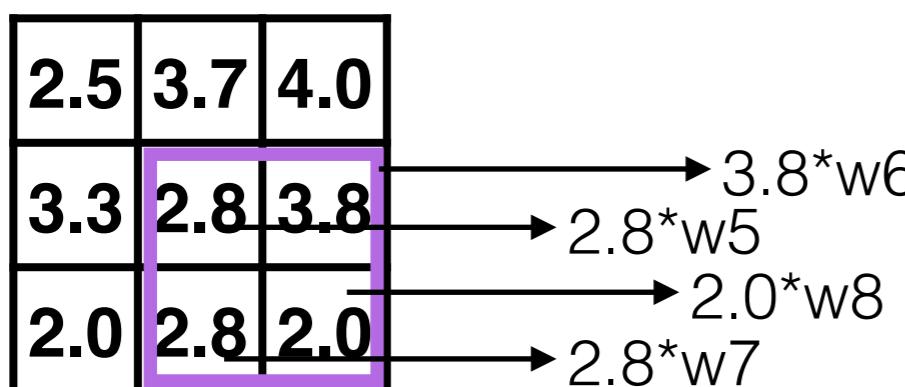
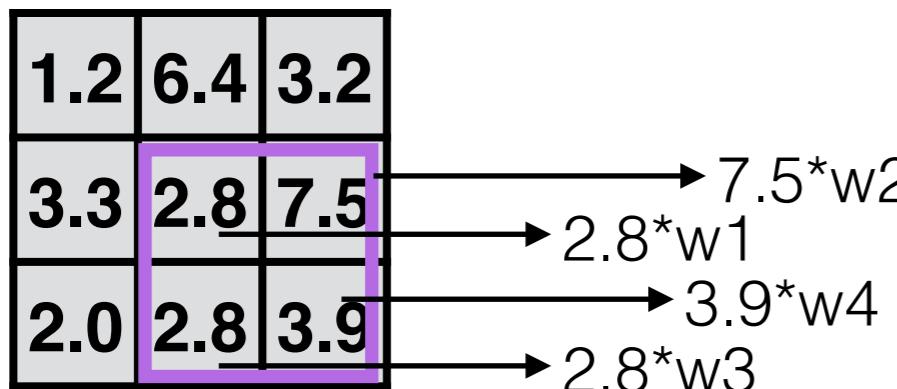
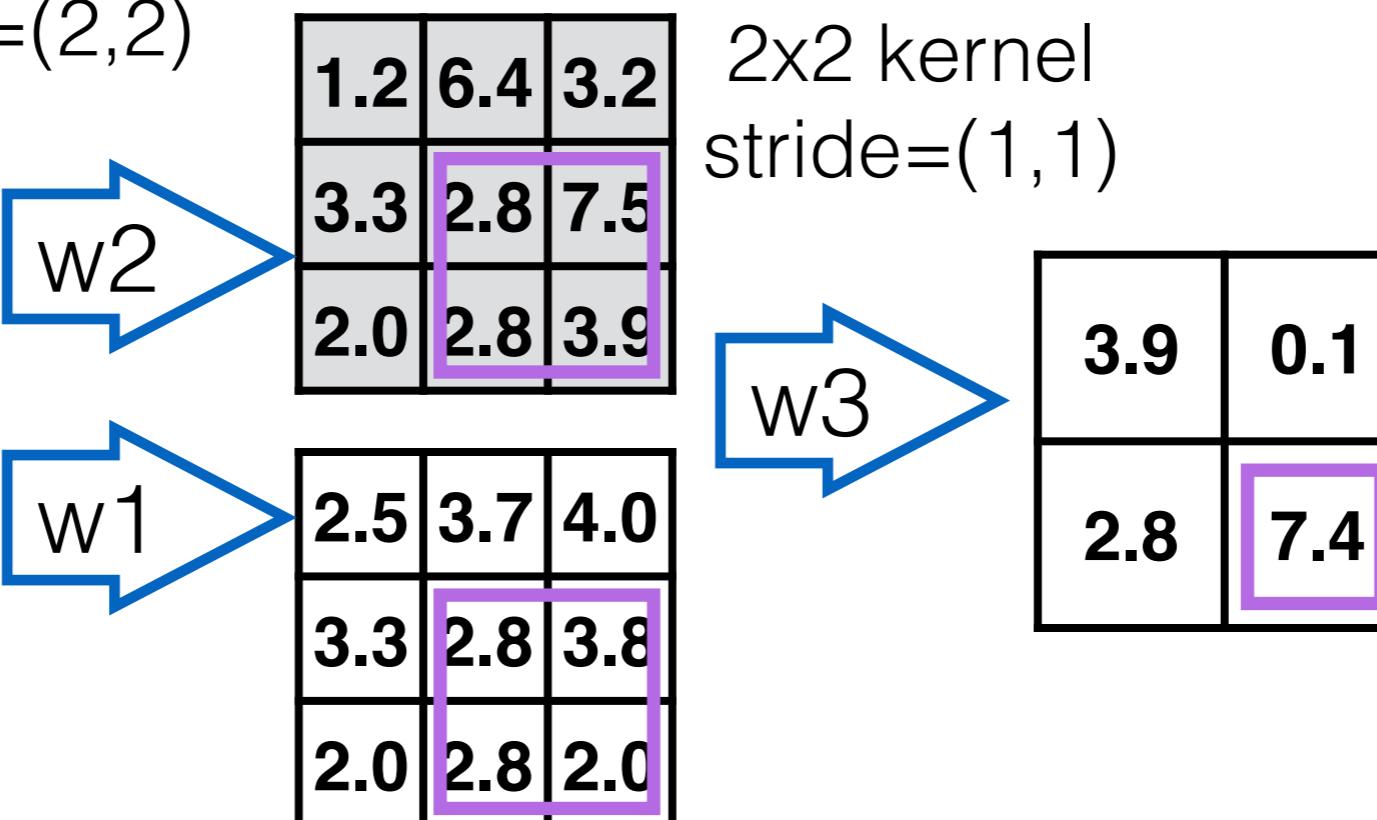


3.9	0.1
2.8	7.4

# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

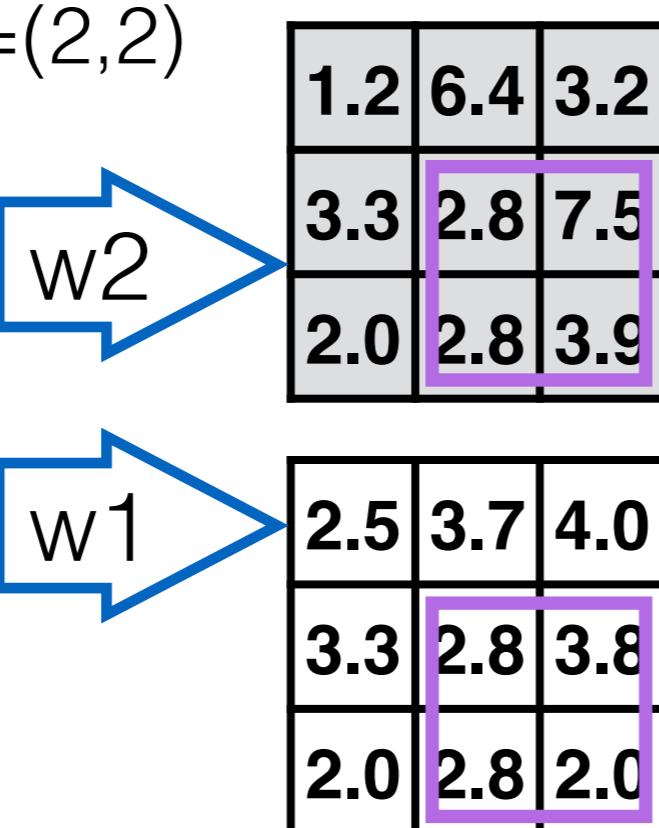
2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



2x2 kernel  
stride=(1,1)

3.9	0.1
2.8	7.4

1.2	6.4	3.2
3.3	2.8	7.5
2.0	2.8	3.9

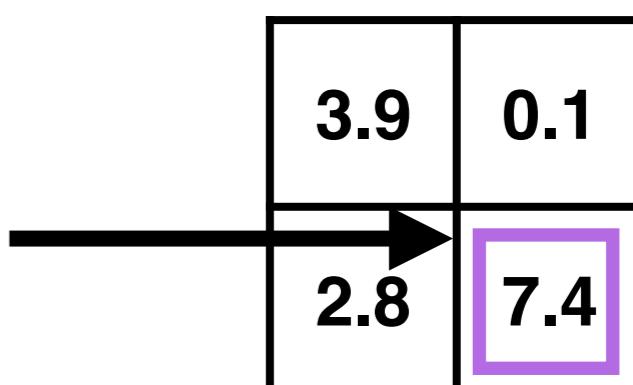
$$7.5 \cdot w_2 + 2.8 \cdot w_1 + 3.9 \cdot w_4 + 2.8 \cdot w_3$$

2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0

$$3.8 \cdot w_6 + 2.8 \cdot w_5 + 2.0 \cdot w_8 + 2.8 \cdot w_7$$

w3 is this:

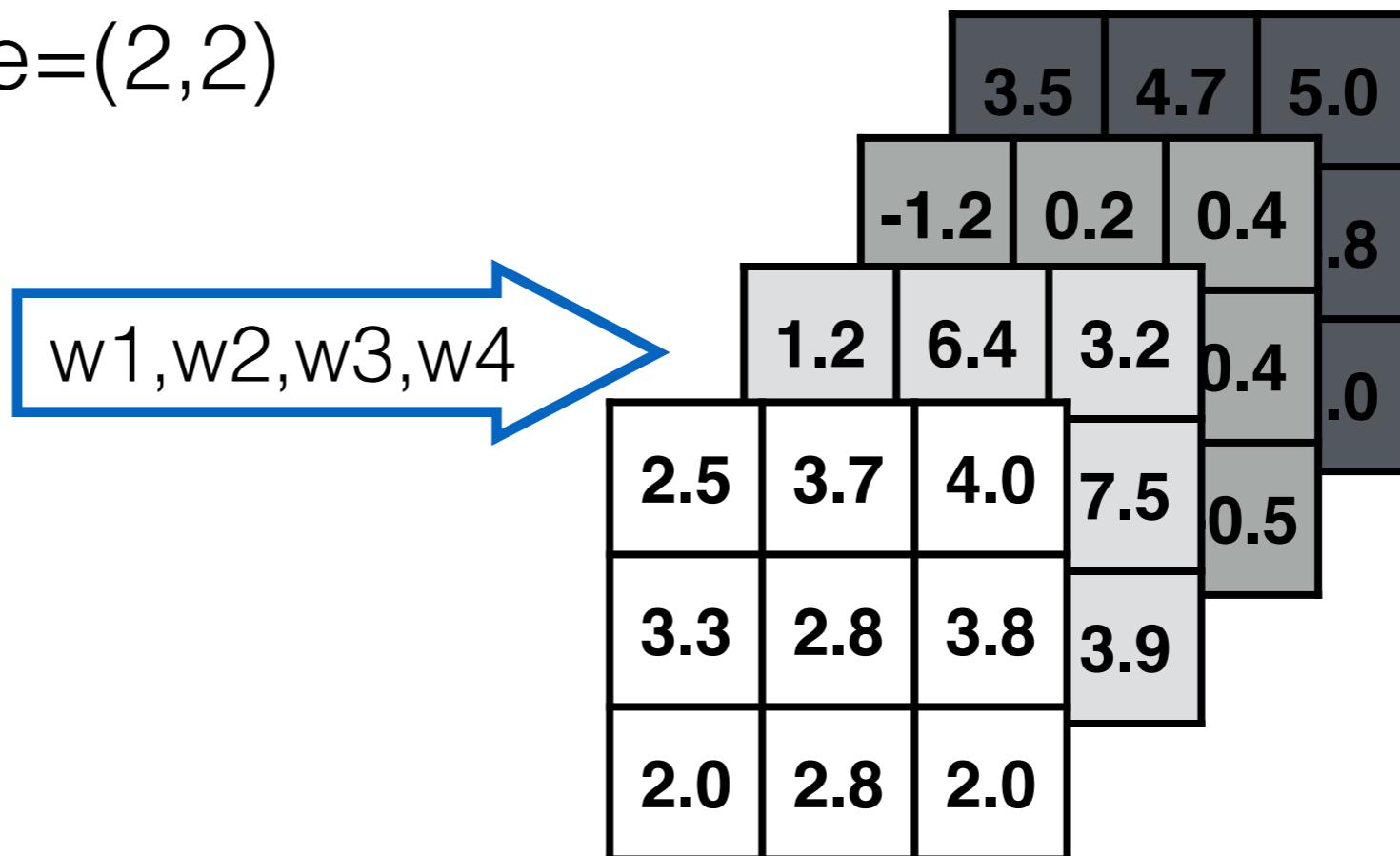
$$\begin{aligned} & 2.8 \cdot w_1 + 7.5 \cdot w_2 + \\ & 2.8 \cdot w_3 + 3.9 \cdot w_4 + \\ & 2.8 \cdot w_5 + 3.8 \cdot w_6 + \\ & 2.8 \cdot w_7 + 2.0 \cdot w_8 + b \\ = & Z \end{aligned}$$



# Convolutions with multiple filters

2x2 kernel, stride=(2,2)

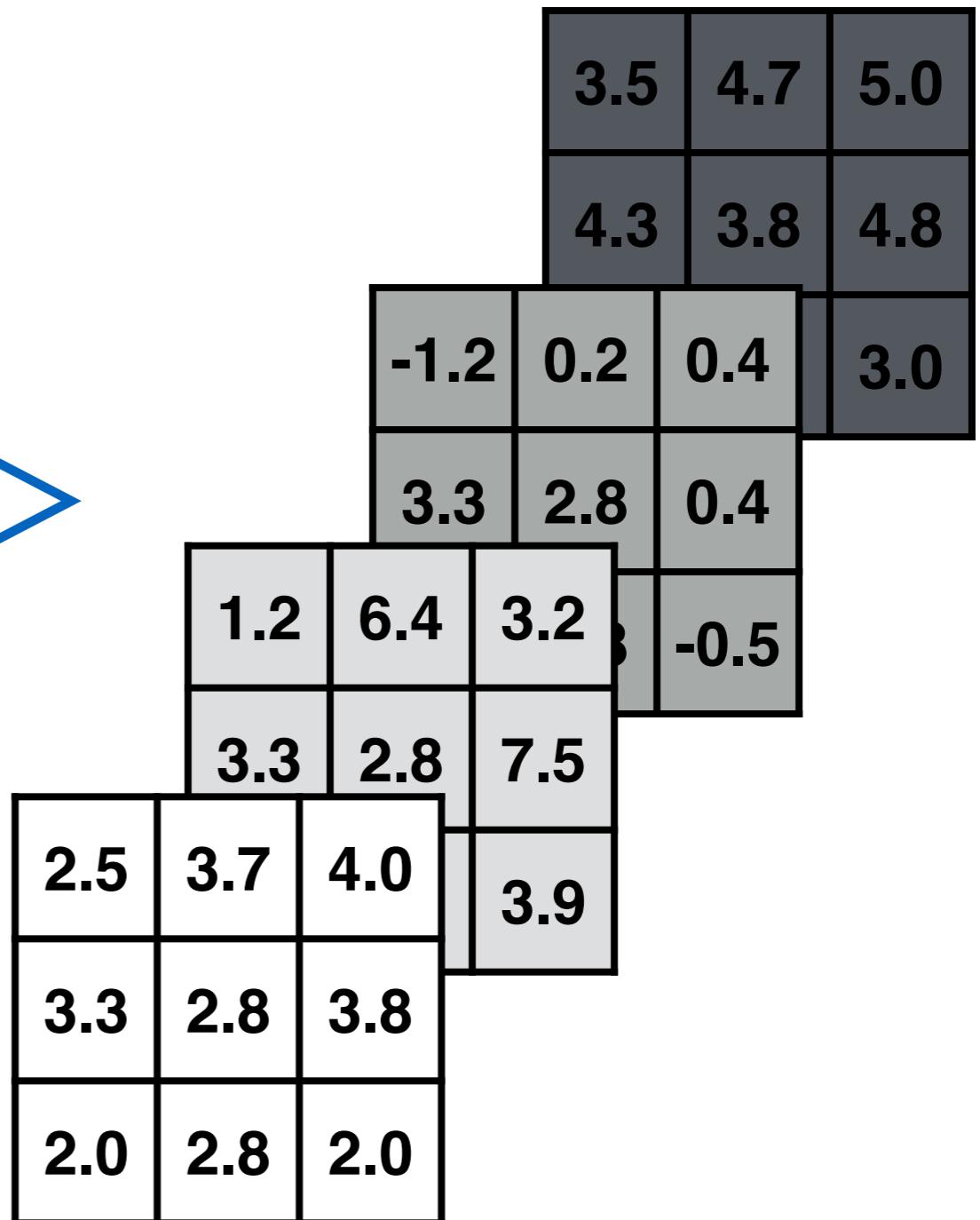
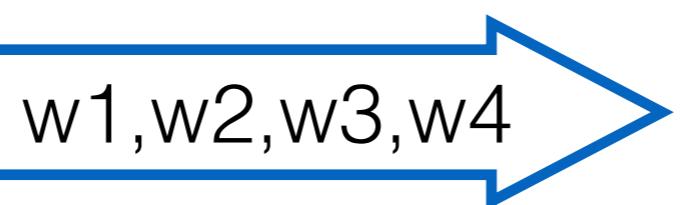
2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3

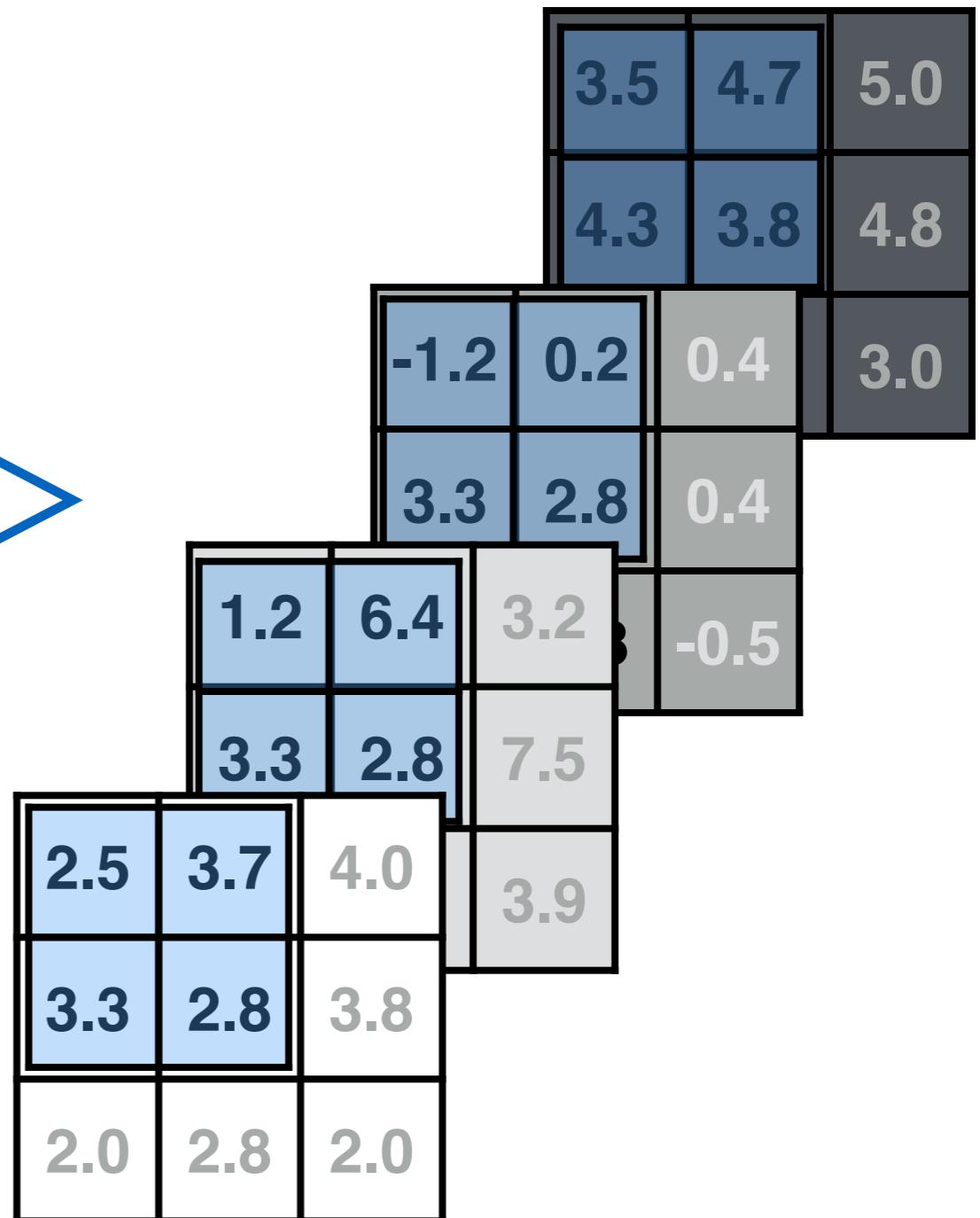
w1,w2,w3,w4



2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3

w1,w2,w3,w4



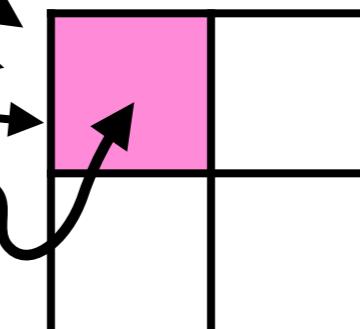
2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3

3.5	4.7	5.0
4.3	3.8	4.8
-1.2	0.2	0.4

2x2 kernel  
stride=(1,1)

1.2	6.4	3.2	-0.5
3.3	2.8	7.5	3.9
2.5	3.7	4.0	
3.3	2.8	3.8	
2.0	2.8	2.0	



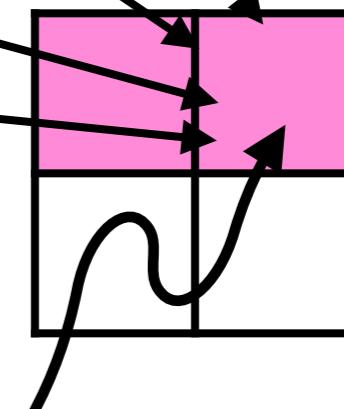
$$\sum_{\text{all blue pixels}} w_i x_i$$

2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



2x2 kernel  
stride=(1,1)



$$\sum_{\text{all blue pixels}} w_i x_i$$

2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3

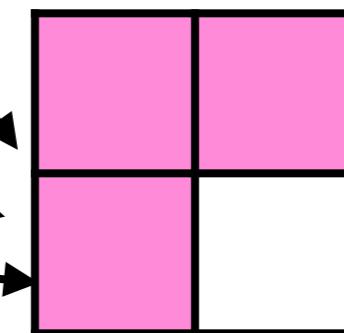
3.5	4.7	5.0
4.3	3.8	
		4.8

2x2 kernel  
stride=(1,1)

1.2	6.4	3.2
3.3	2.8	
		-0.5

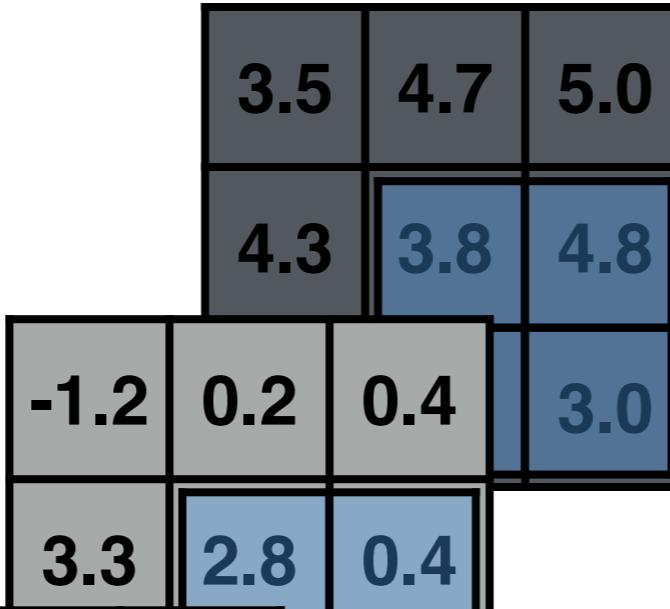
  

2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0

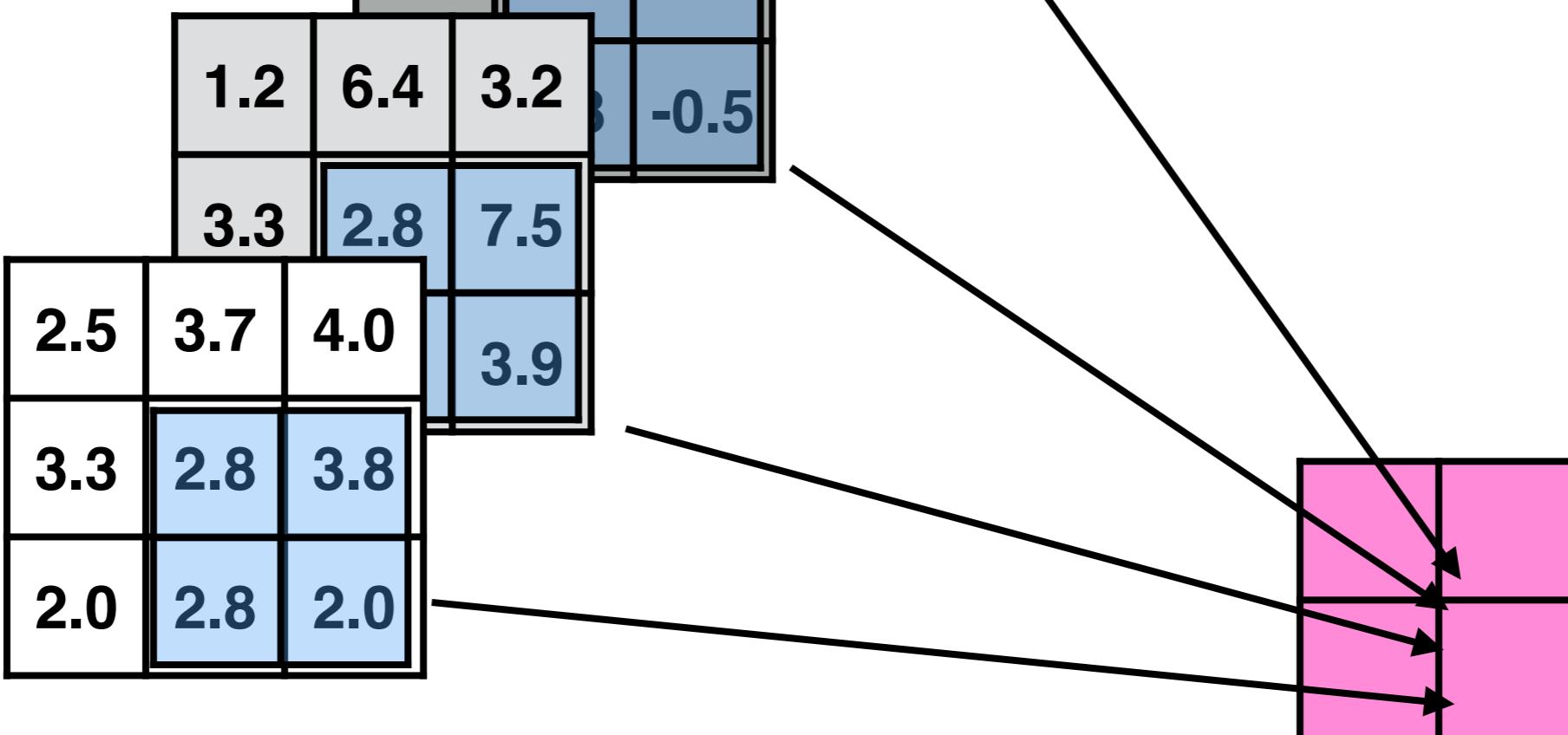


2x2 kernel, stride=(2,2)

2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3



2x2 kernel  
stride=(1,1)



2x2 kernel, stride=(2,2)

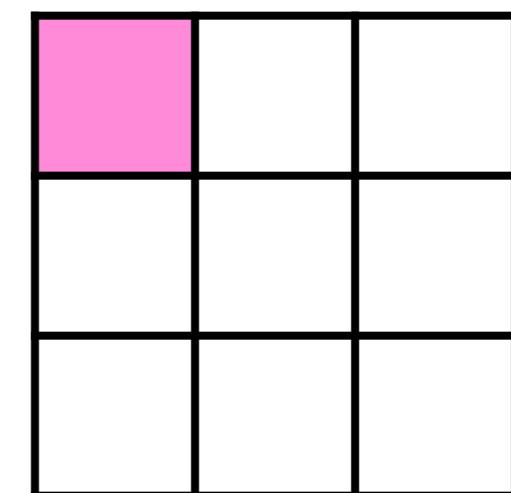
2	3	6	3	4	3
3	6	8	2	9	5
5	3	4	3	6	8
2	7	3	5	3	4
3	4	3	1	2	3
2	3	8	3	4	3

1x1 convolutions

3.5	4.7	5.0
4.3	3.8	4.8

2x2 kernel  
stride=(1,1)

1.2	6.4	3.2
3.3	2.8	7.5
2.5	3.7	4.0
3.3	2.8	3.8
2.0	2.8	2.0



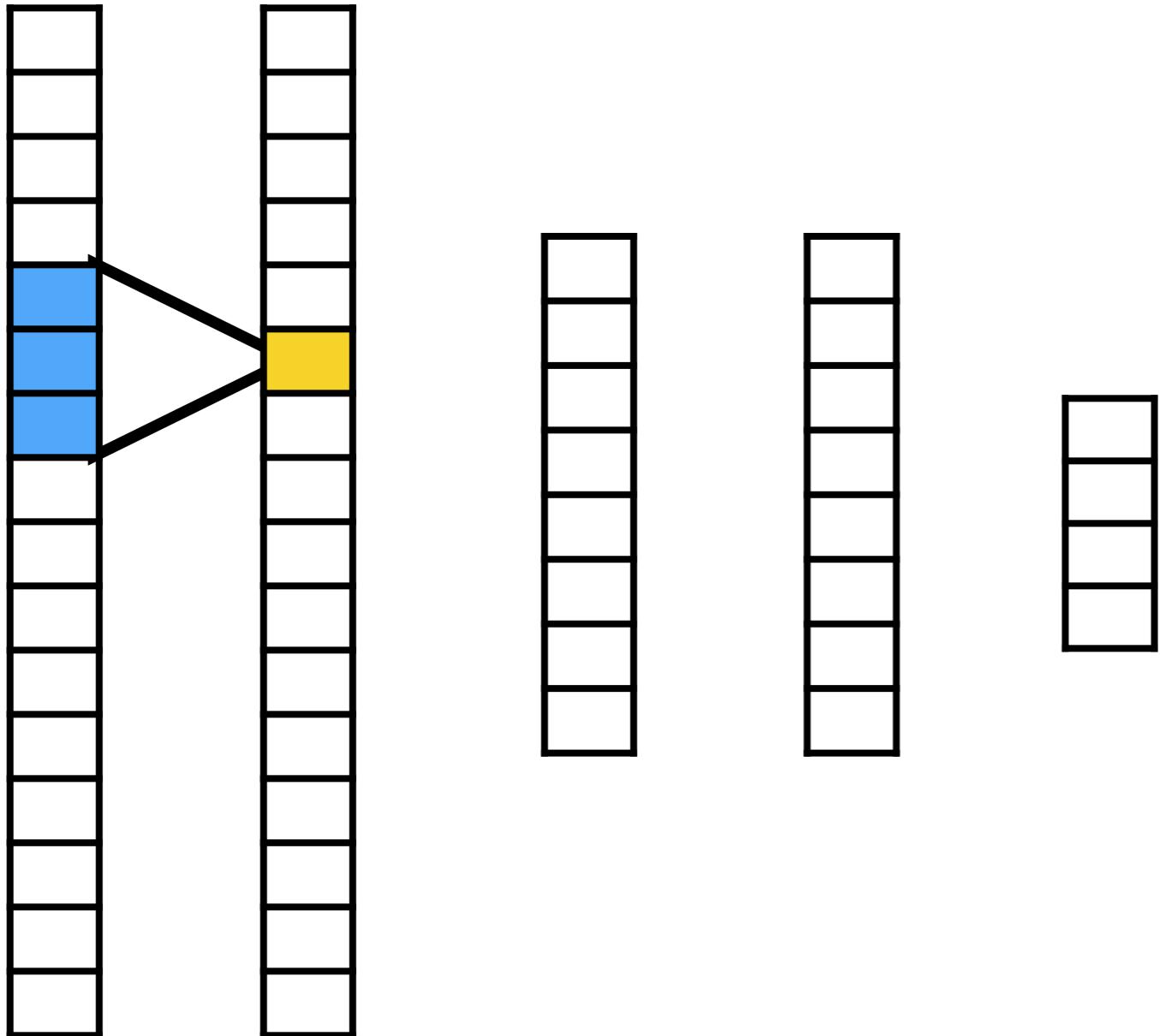
The effect of multiple filters is to  
do arithmetic with images

*add & subtract images*

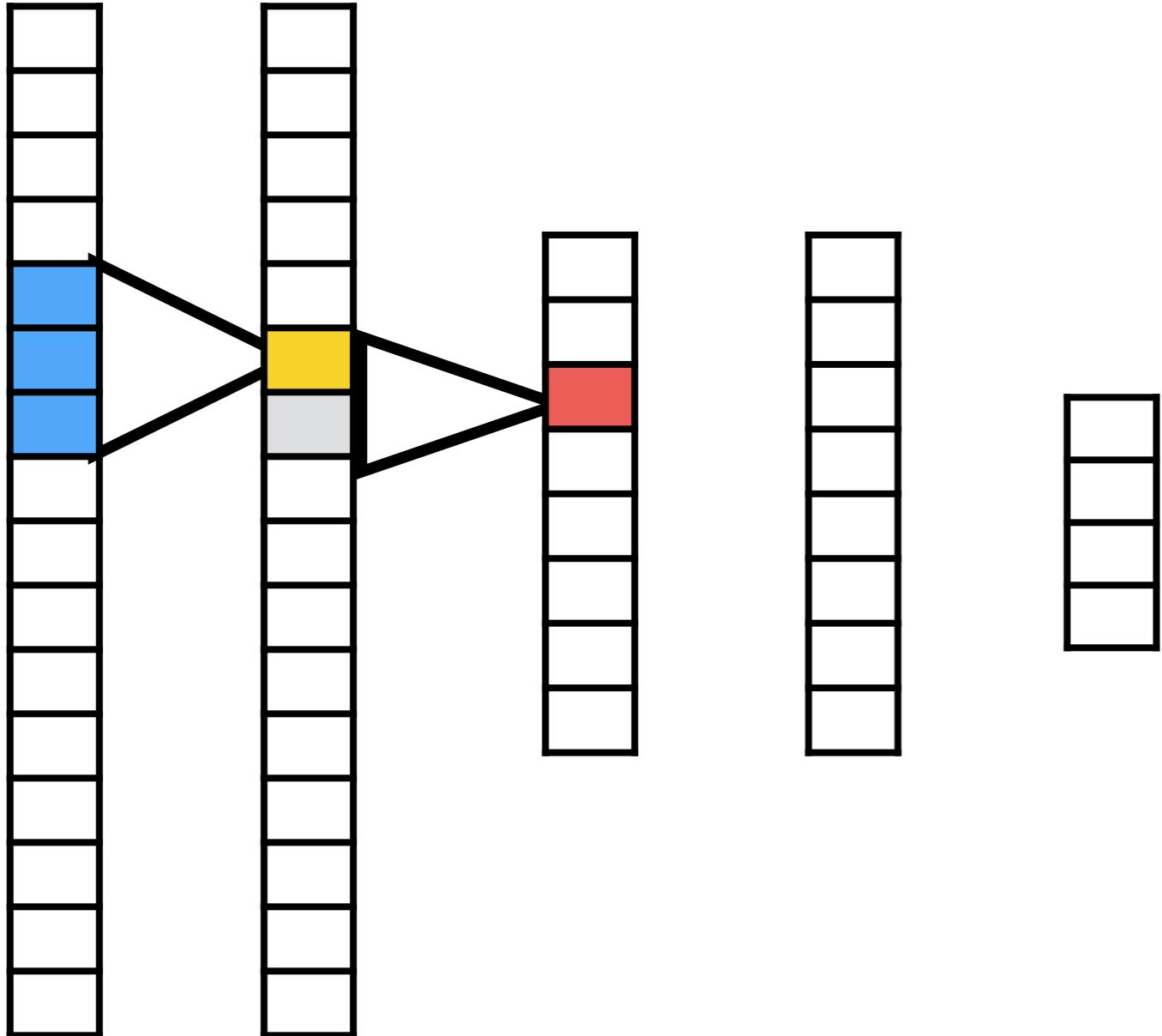
Show Desmos plot for convolution

# Receptive field

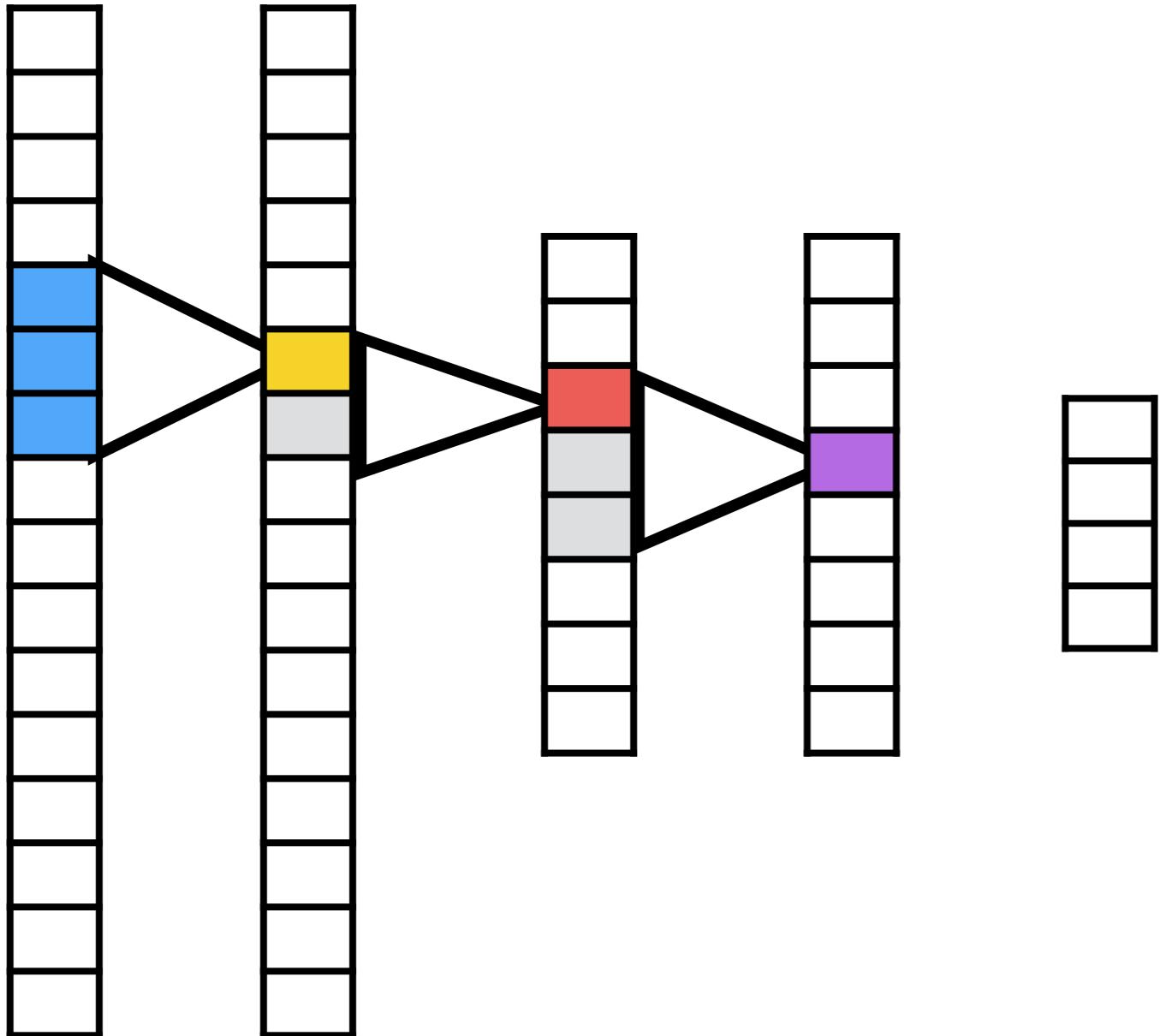
# Concept of receptive field



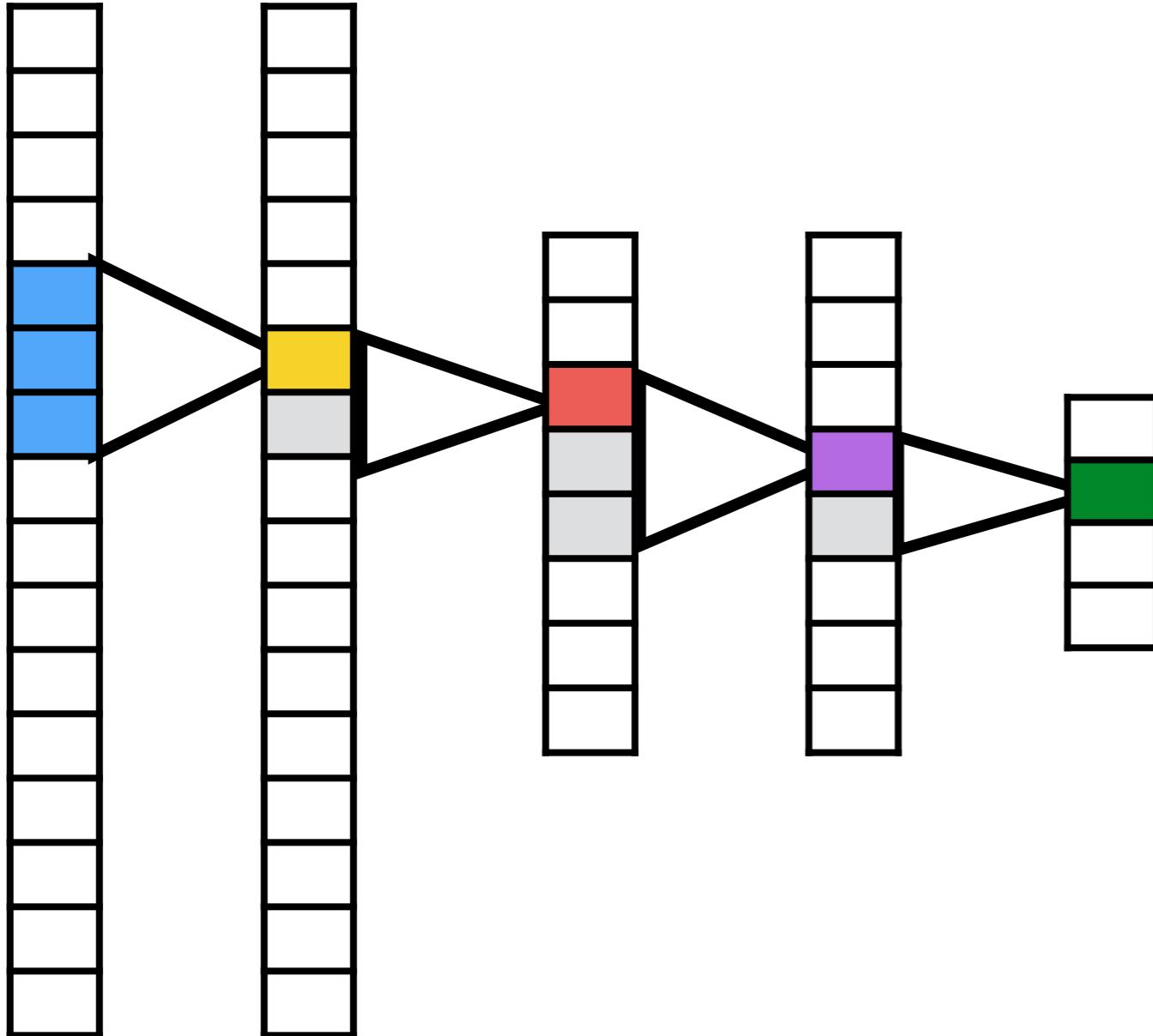
# Concept of receptive field



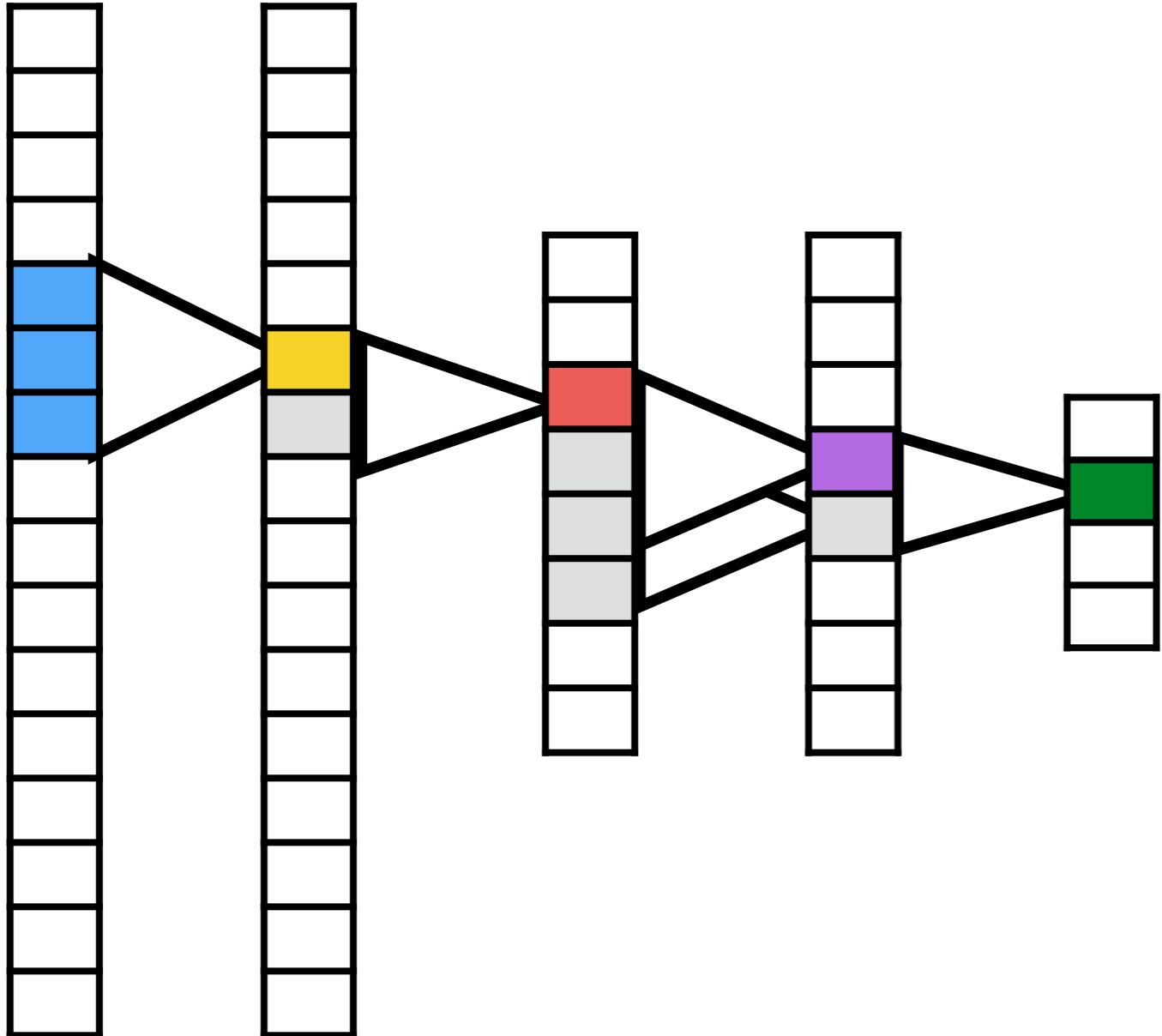
# Concept of receptive field



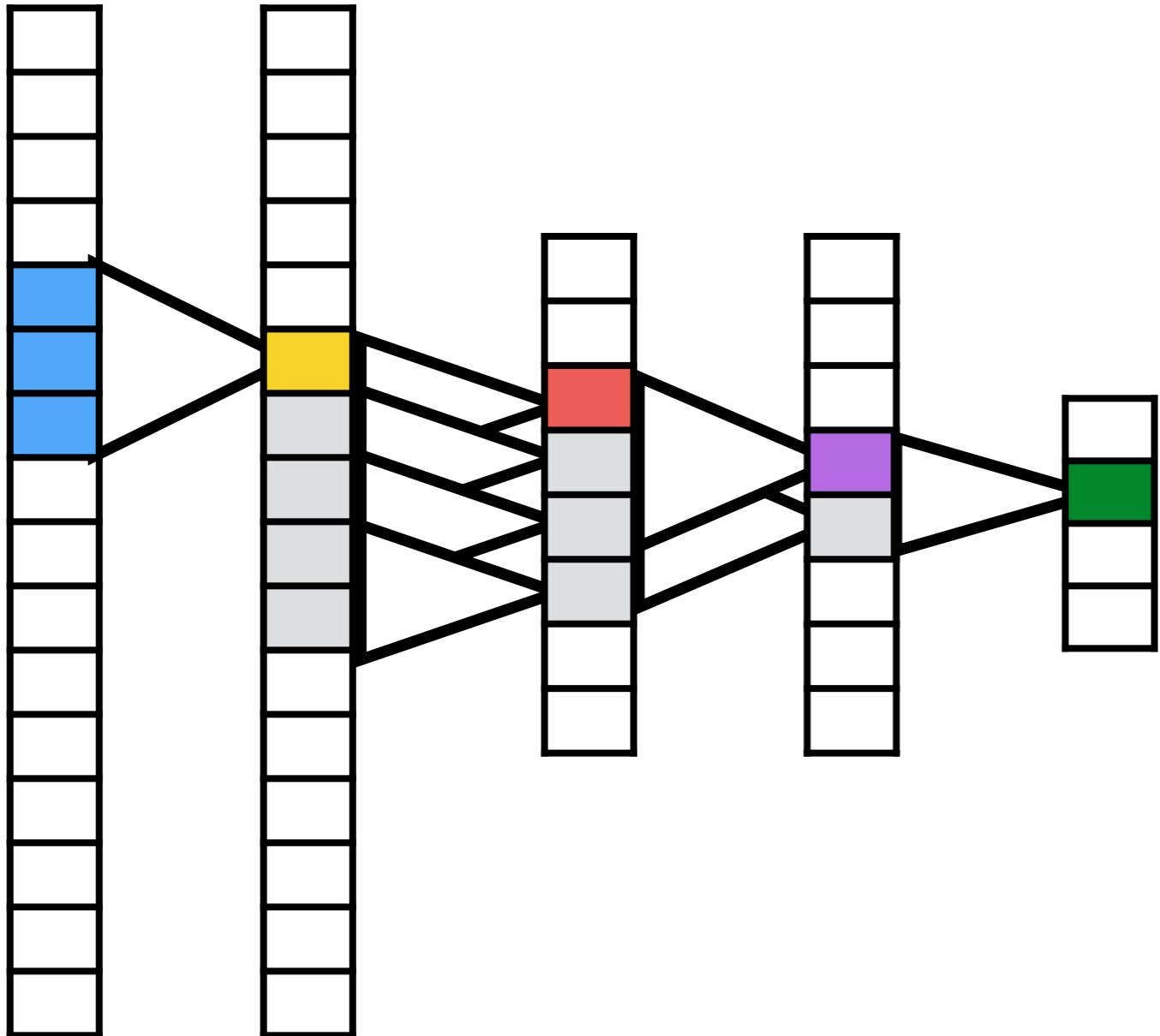
# Concept of receptive field



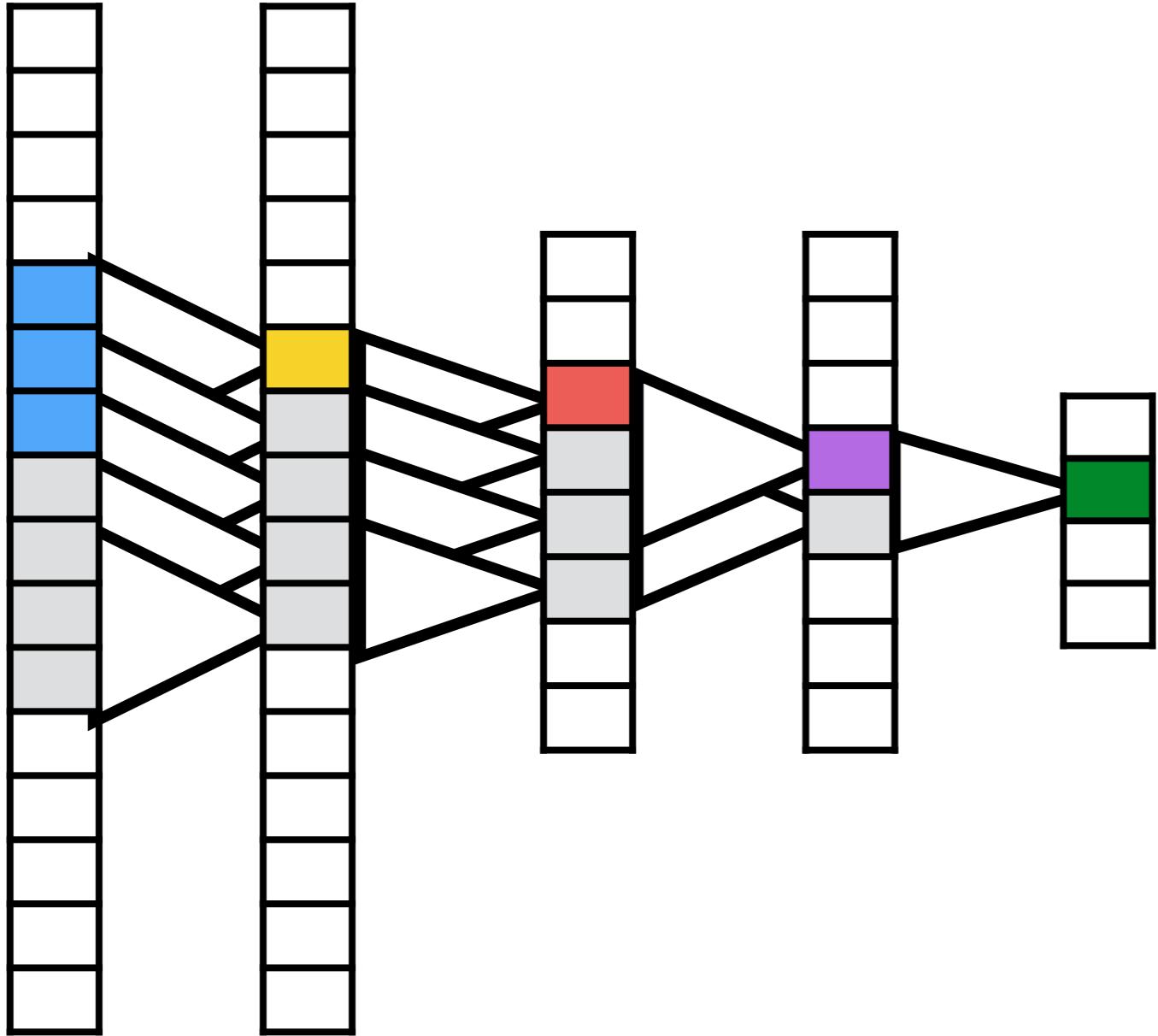
# Concept of receptive field



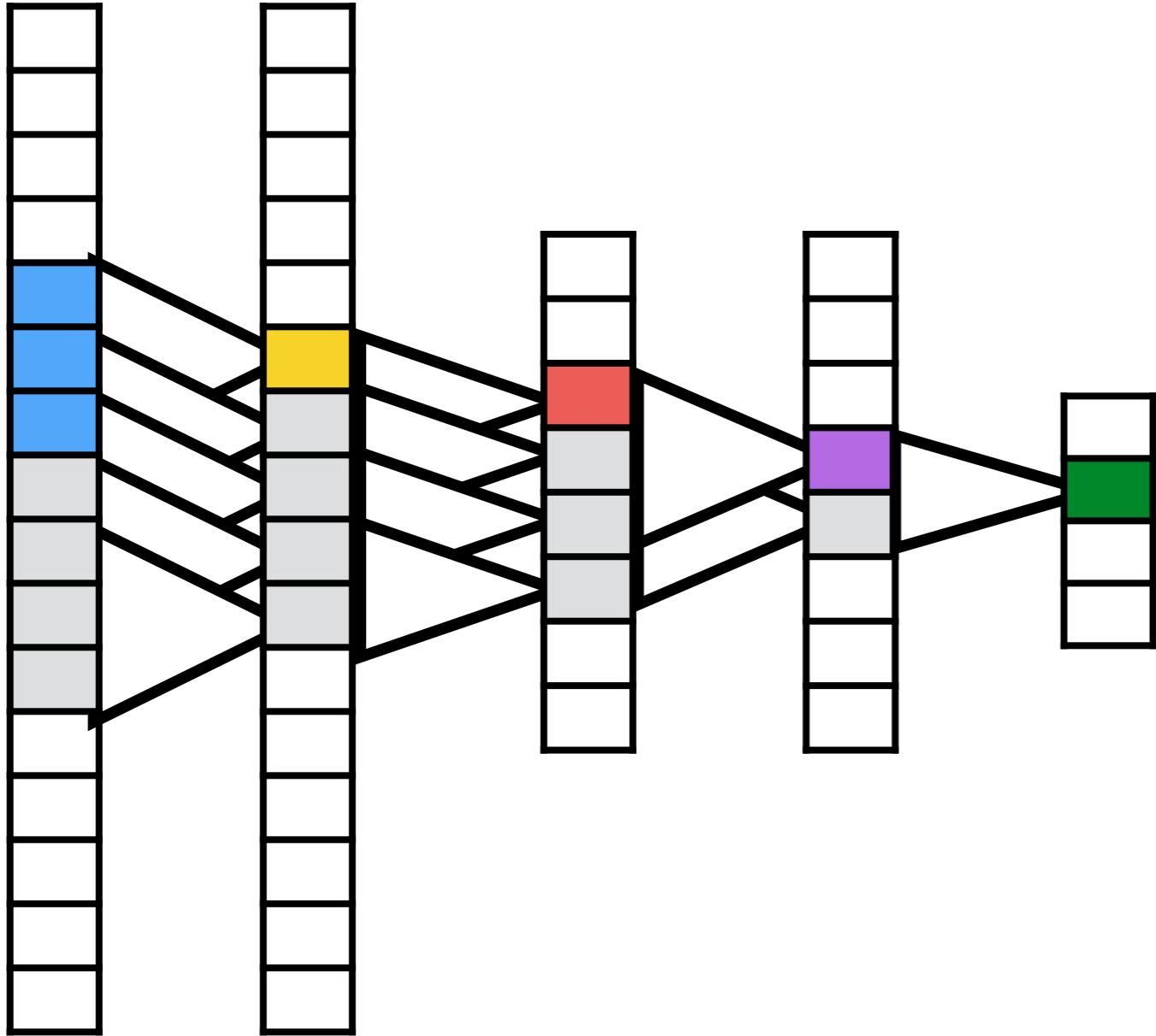
# Concept of receptive field

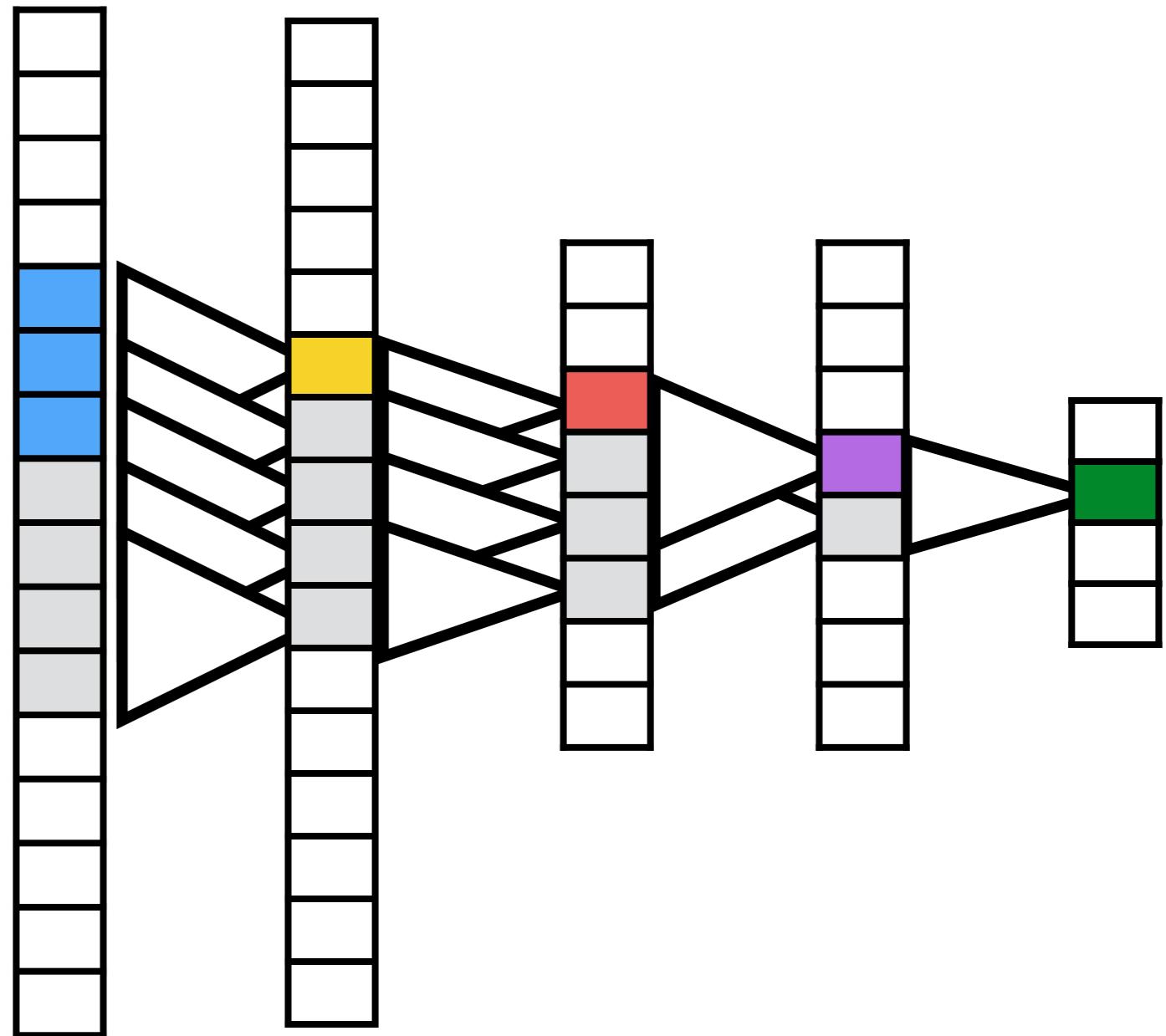


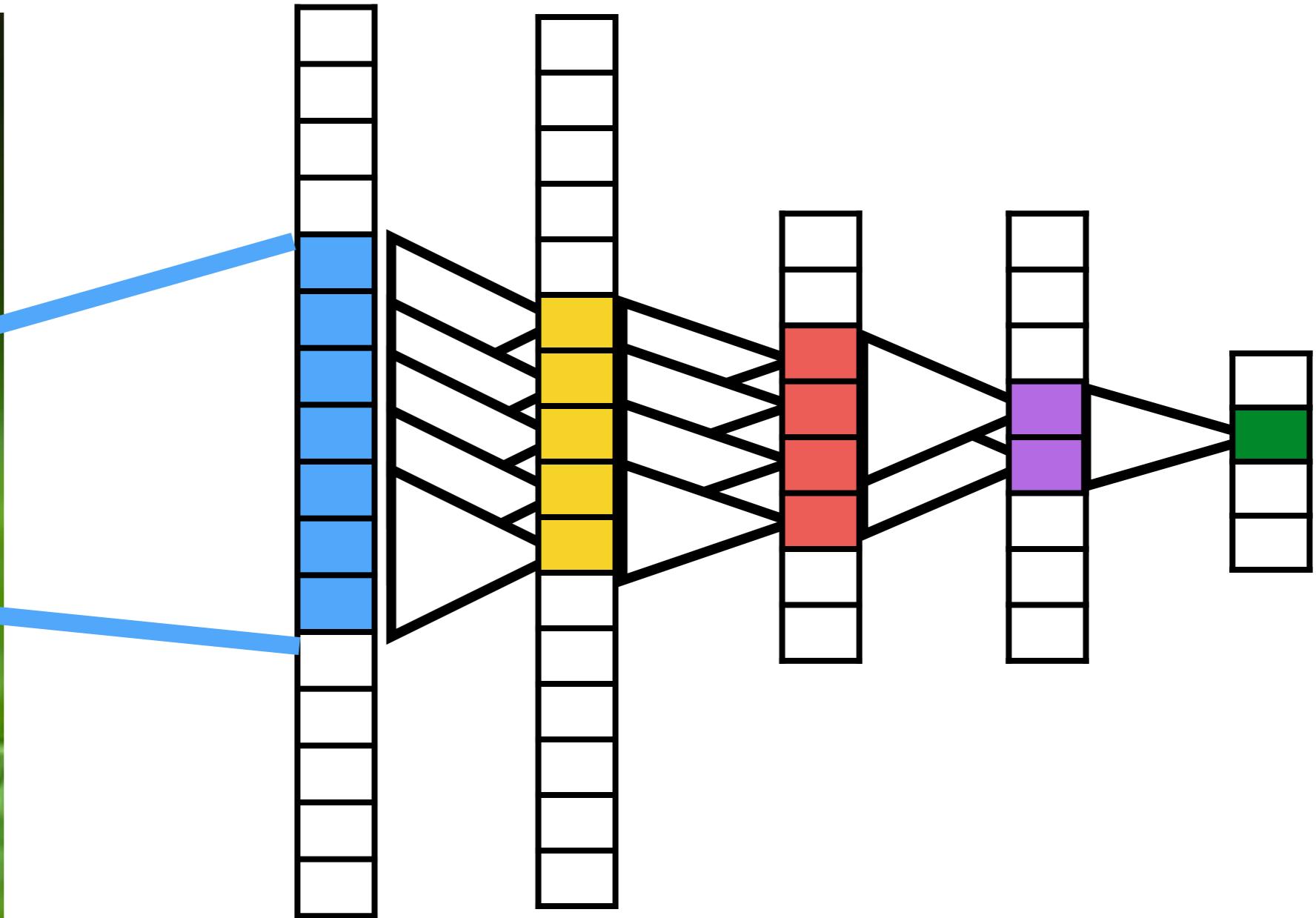
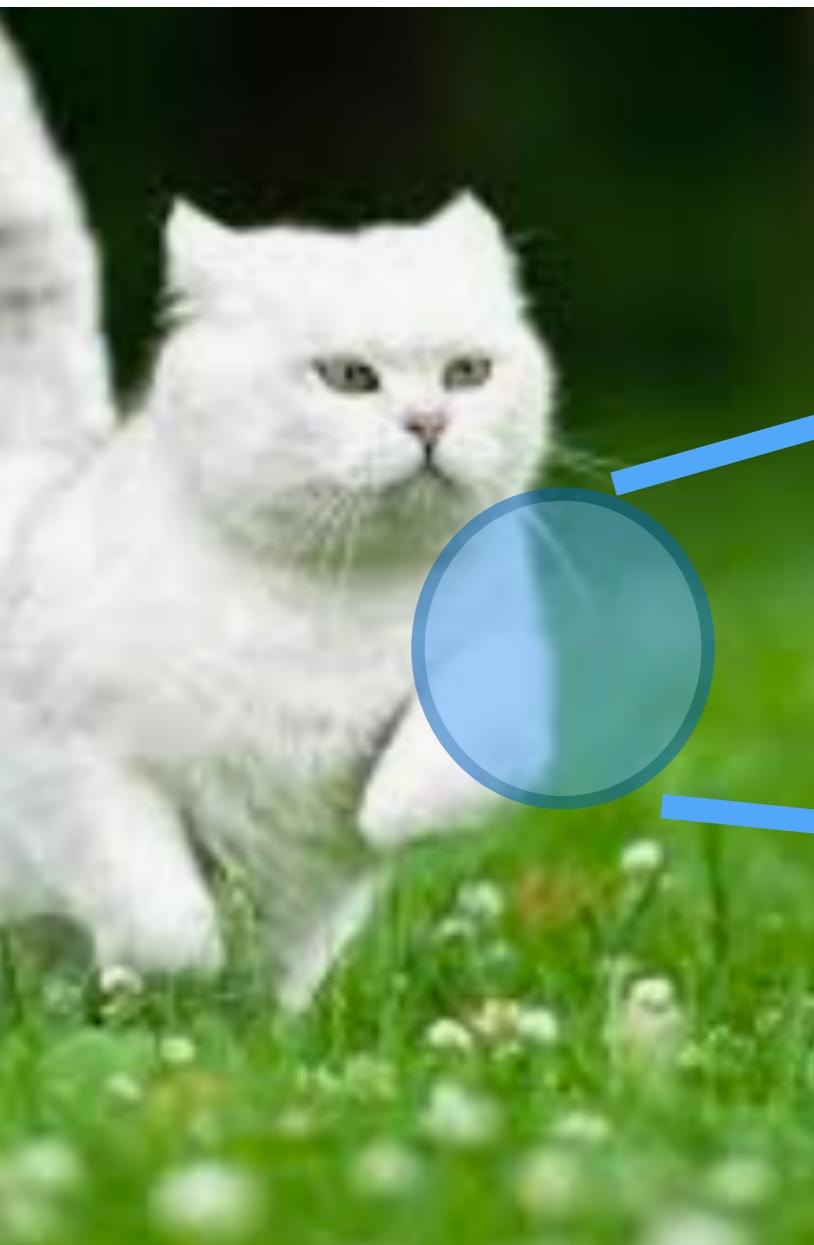
# Concept of receptive field

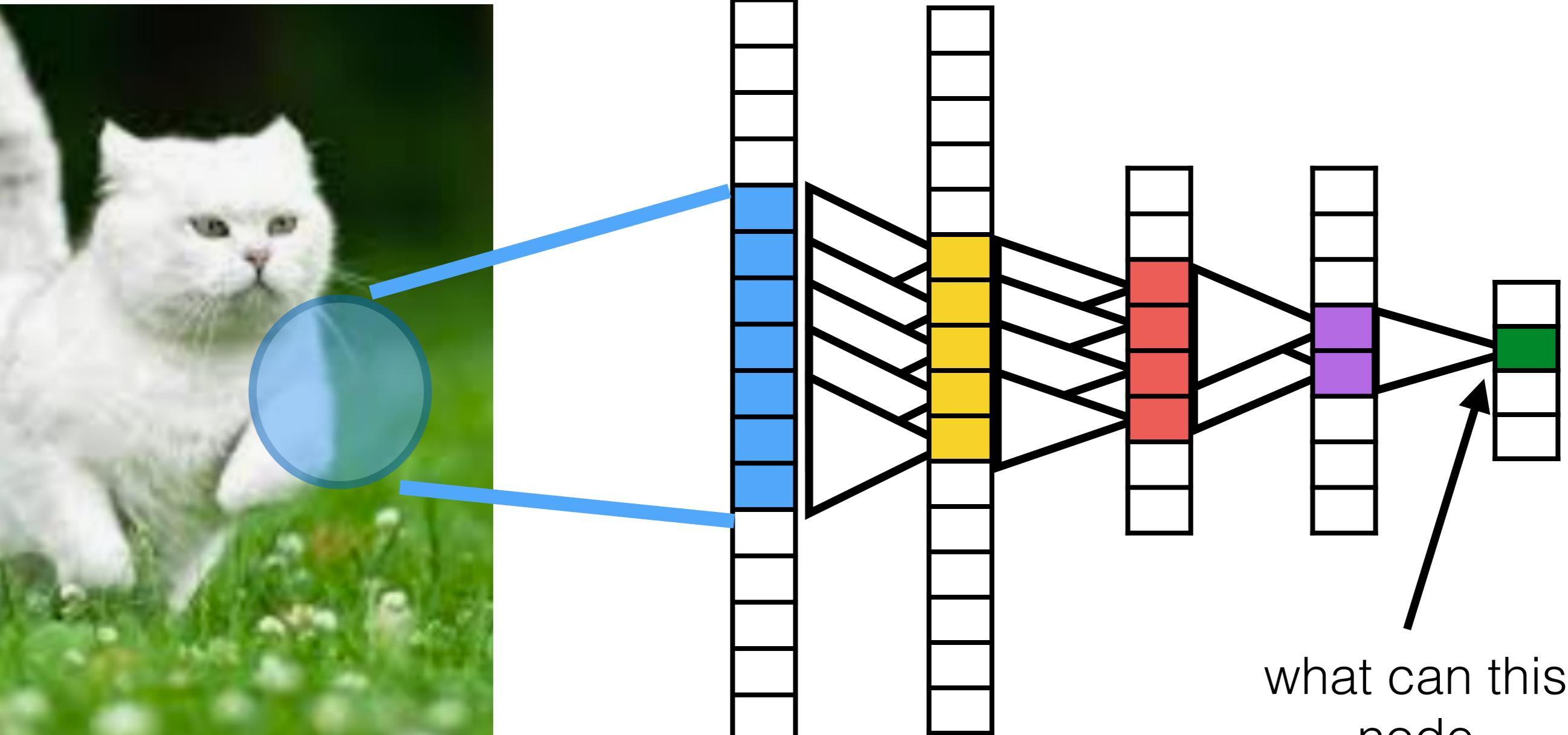


What is the lesson here?

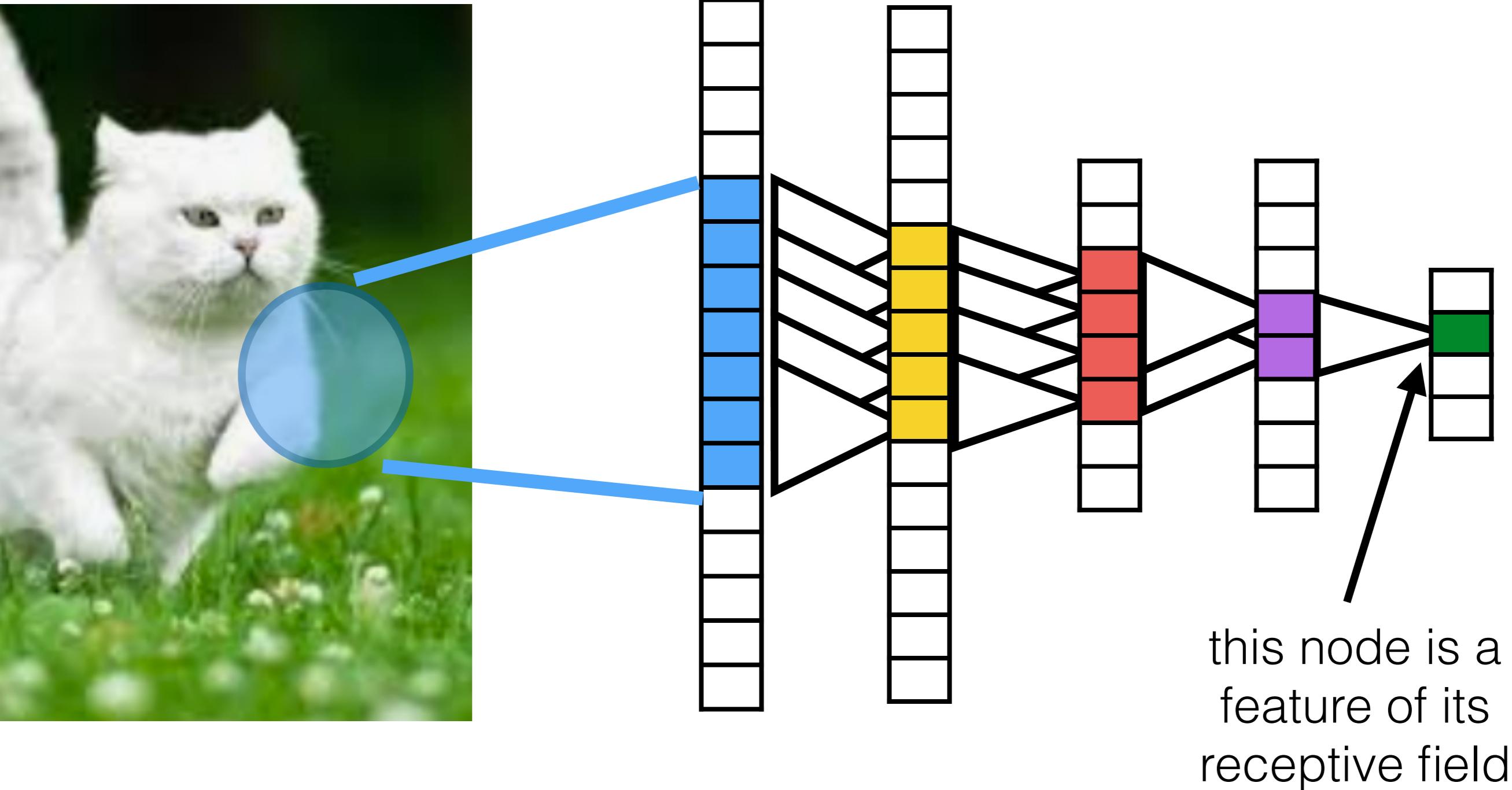




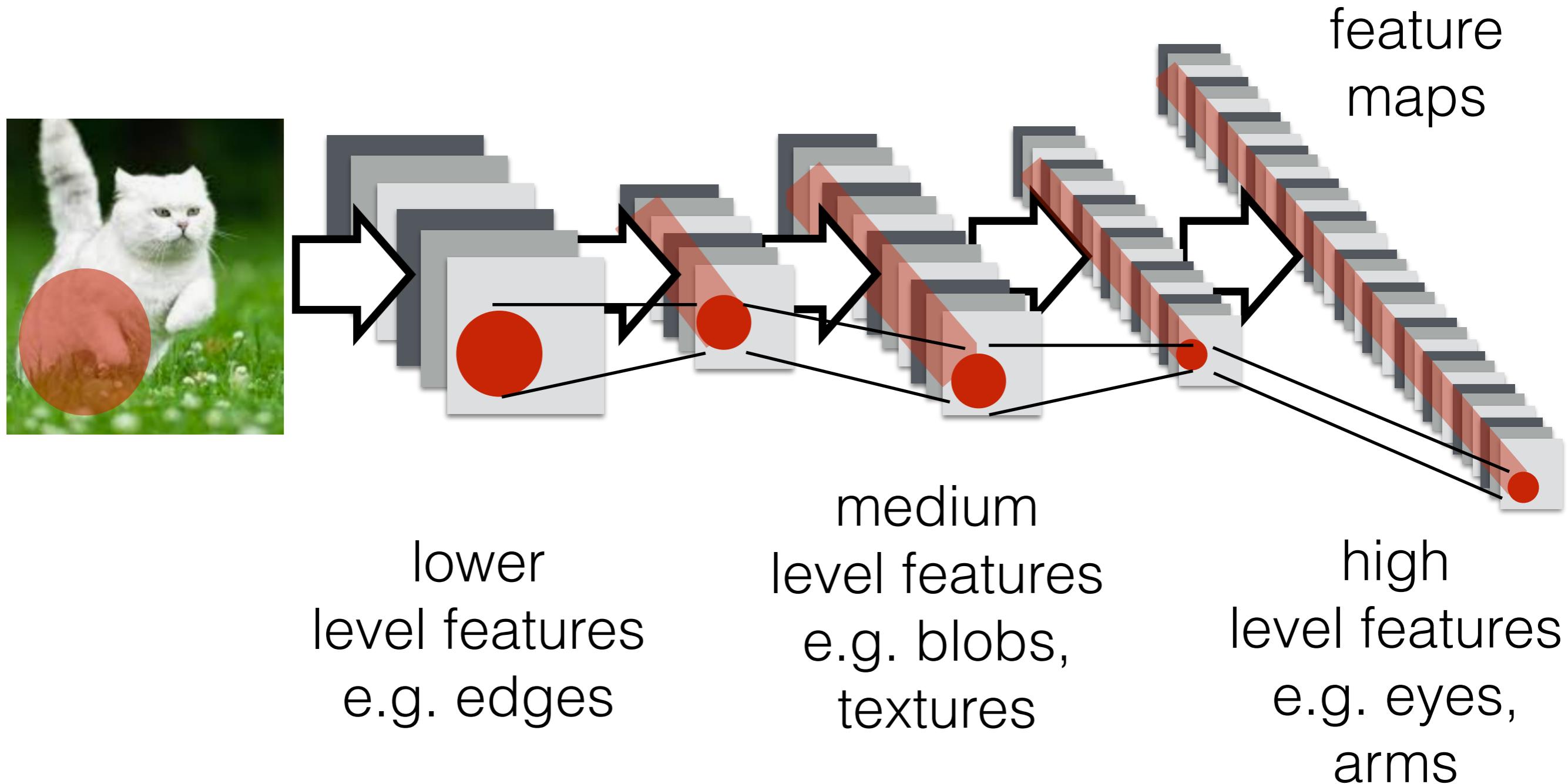




what can this  
node  
“understand”



# CNN part of the network is a image feature extractor for meaningful high level features



# Overall architecture of CNN

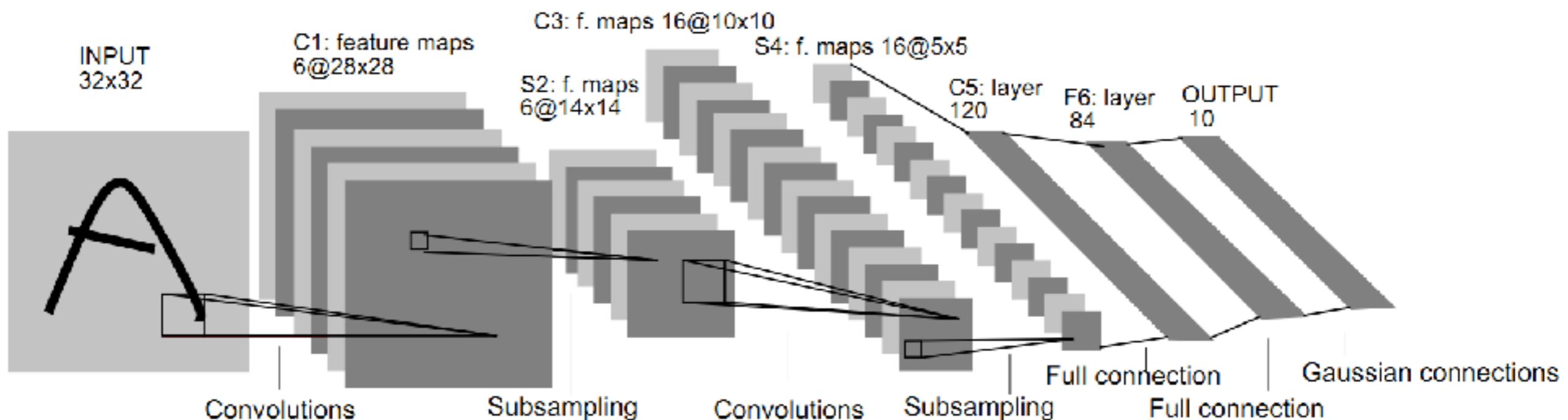
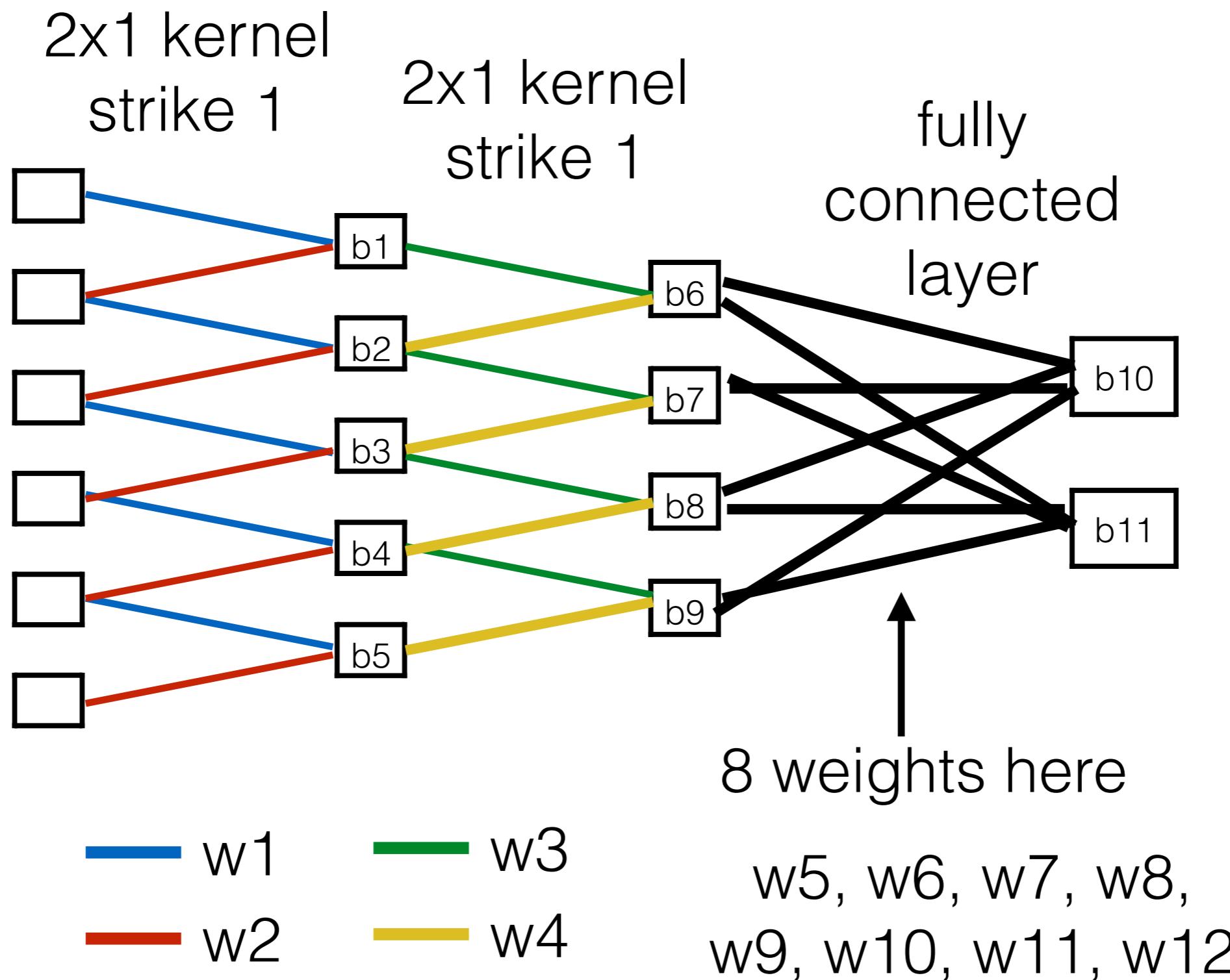


Fig. 2. Architecture of LeNet-5, a Convolutional Neural Network, here for digits recognition. Each plane is a feature map, i.e. a set of units whose weights are constrained to be identical.

<https://world4jason.gitbooks.io/research-log/content/deepLearning/CNN/Model%20&%20ImgNet/lenet.html>

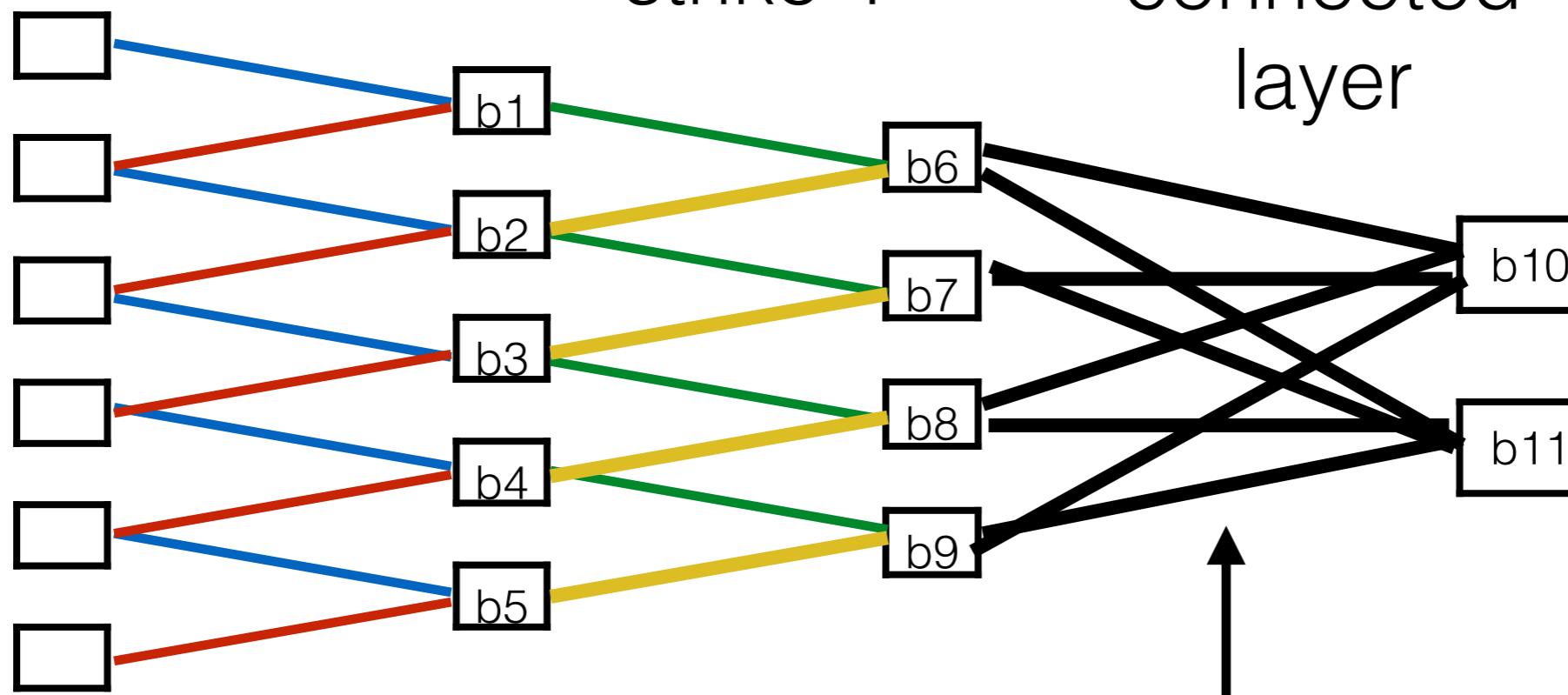
# Training of CNN (convolutional neural networks)



2x1 kernel  
strike 1

2x1 kernel  
strike 1

fully  
connected  
layer



w1

w2

w3

w4

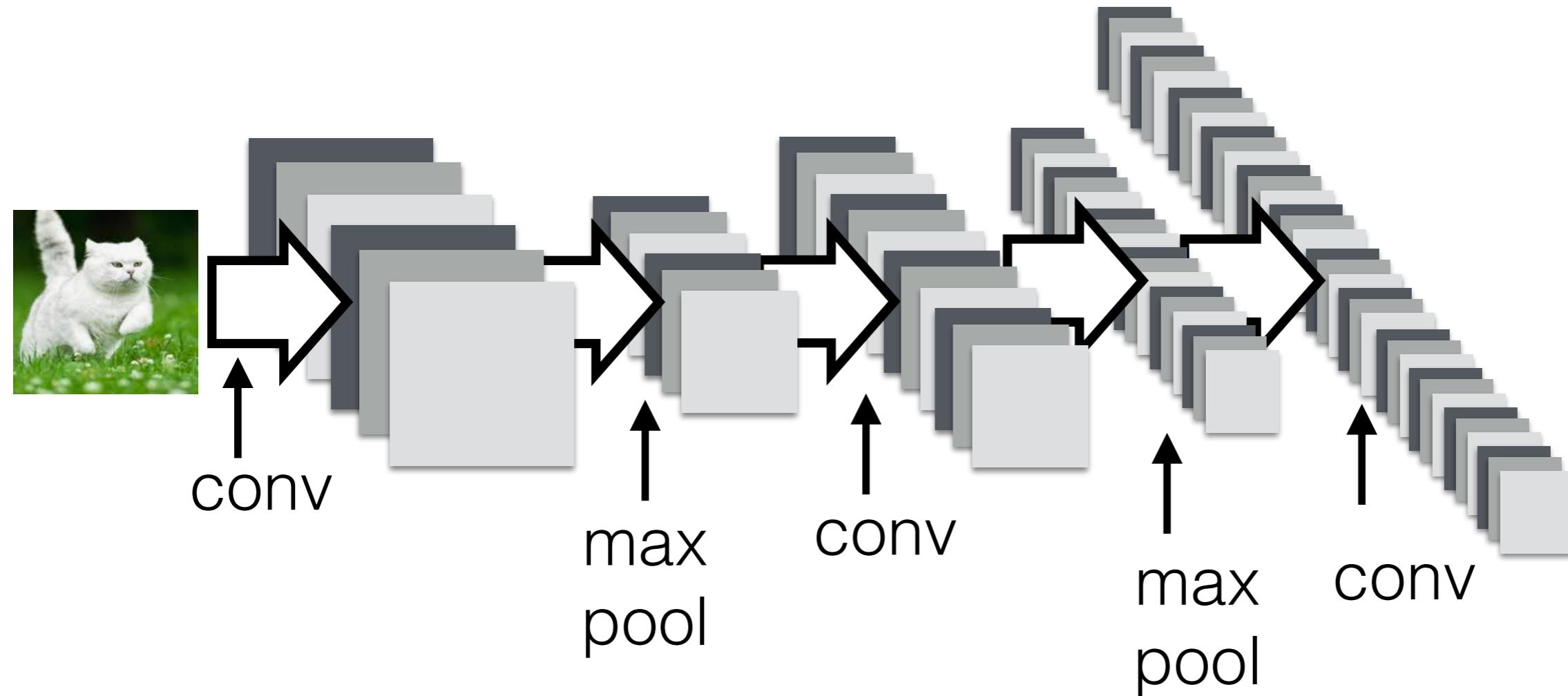
8 weights here

w5, w6, w7, w8,  
w9, w10, w11, w12

Using back propagation, minimize loss by adjusting  
w1, w2, . . . w12 & b1, . . . b11

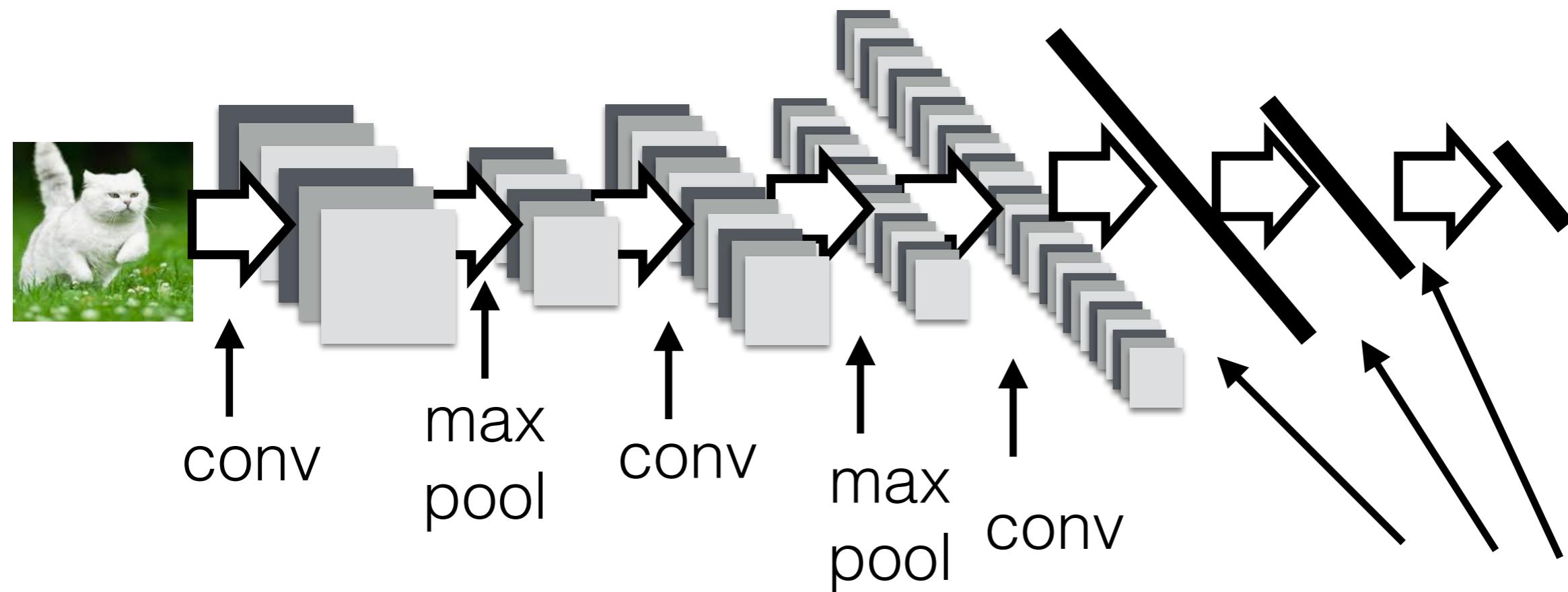
**these are called “Trainable parameters”**

# What exactly is a CNN?



convolution part of the CNN

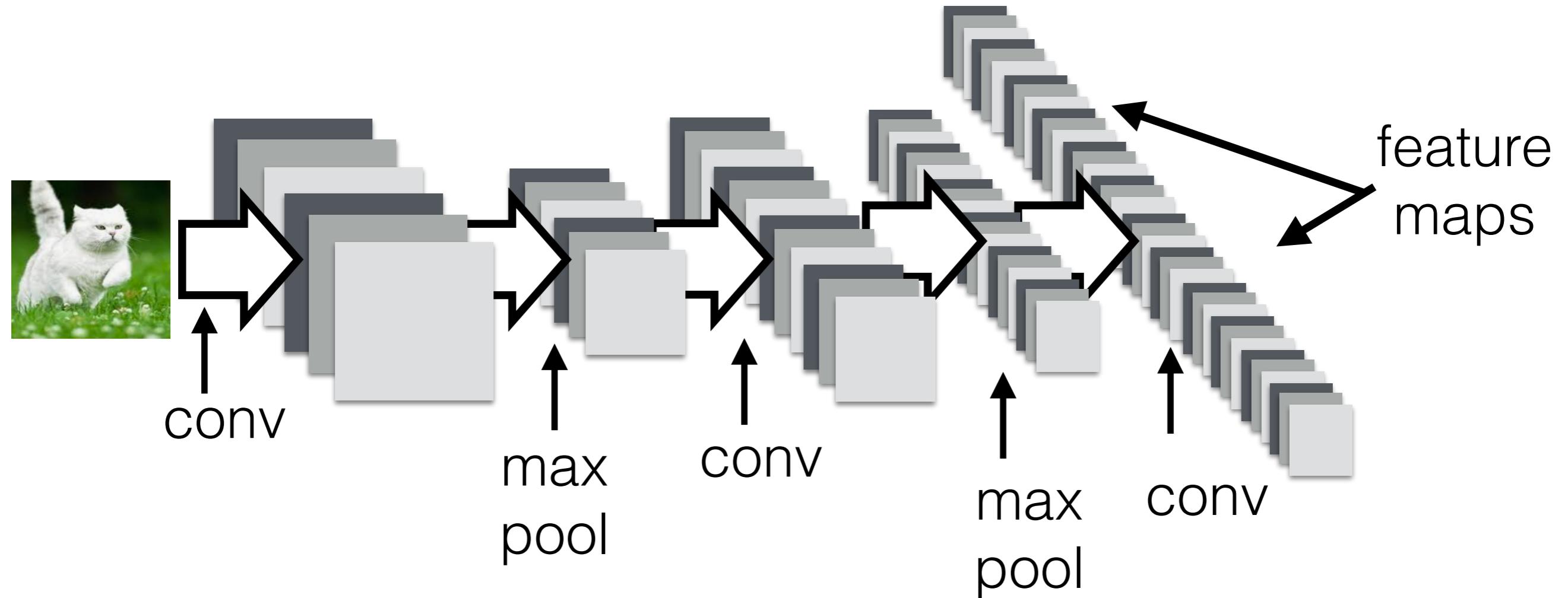
# What exactly is a CNN?



convolution part of the CNN

fully connected  
classification part

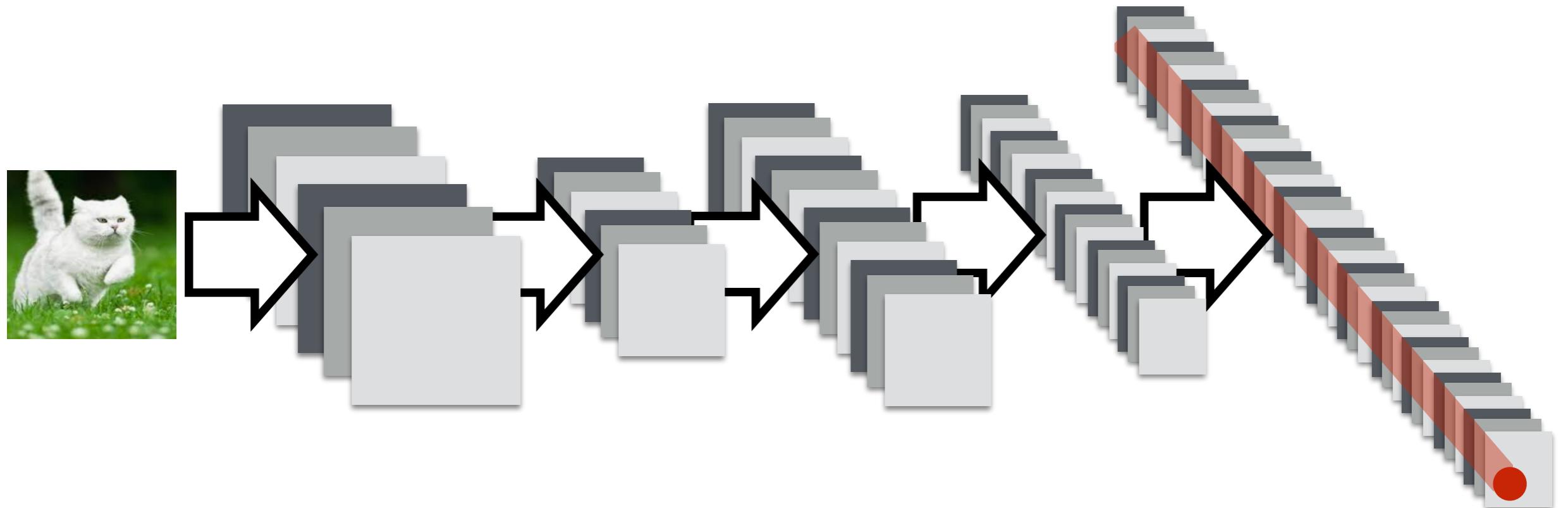
# What exactly is a CNN?



convolution part of the CNN

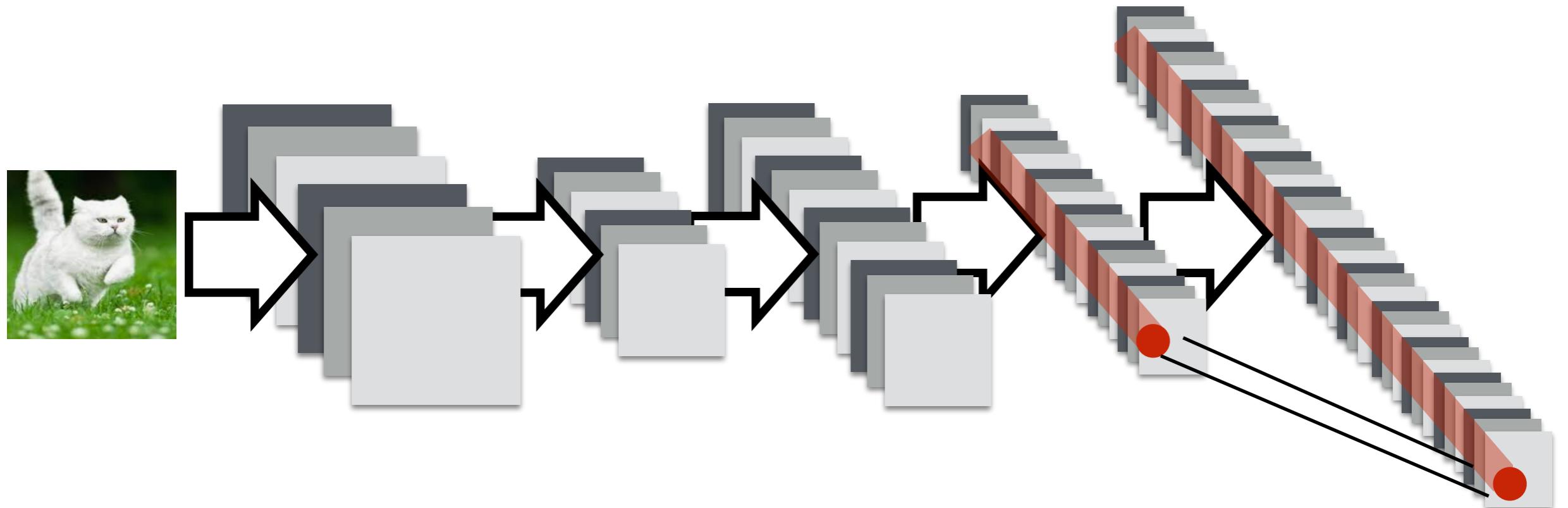
# Feature maps and receptive field

feature  
maps



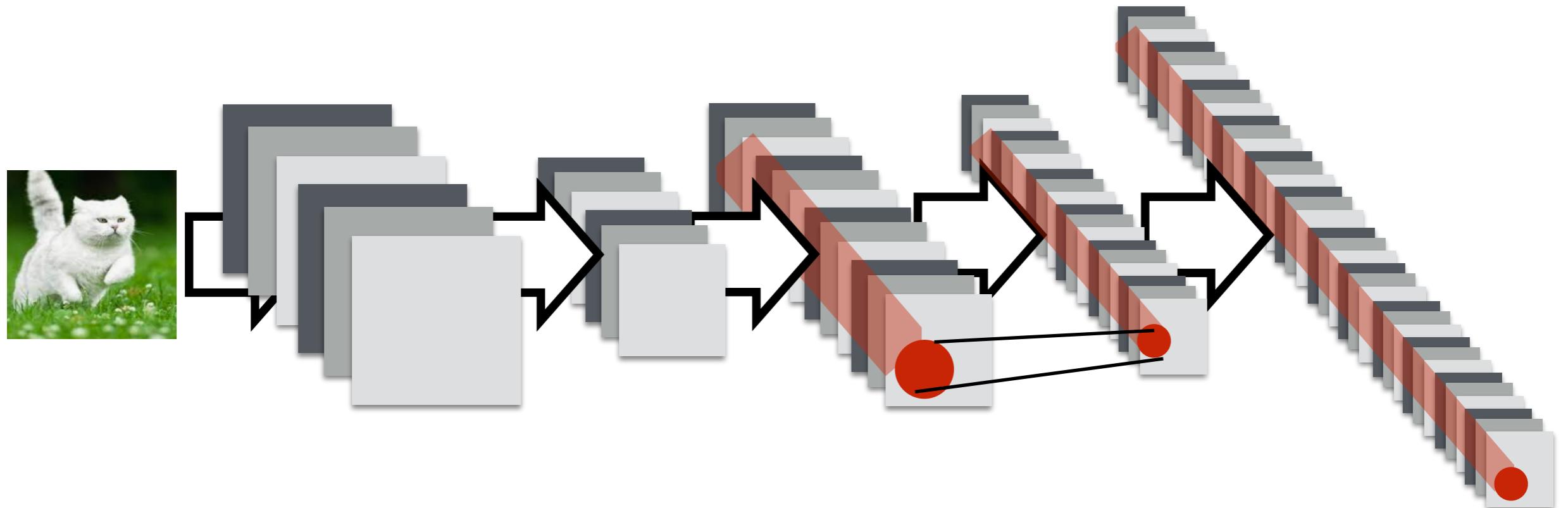
# Feature maps and receptive field

feature  
maps

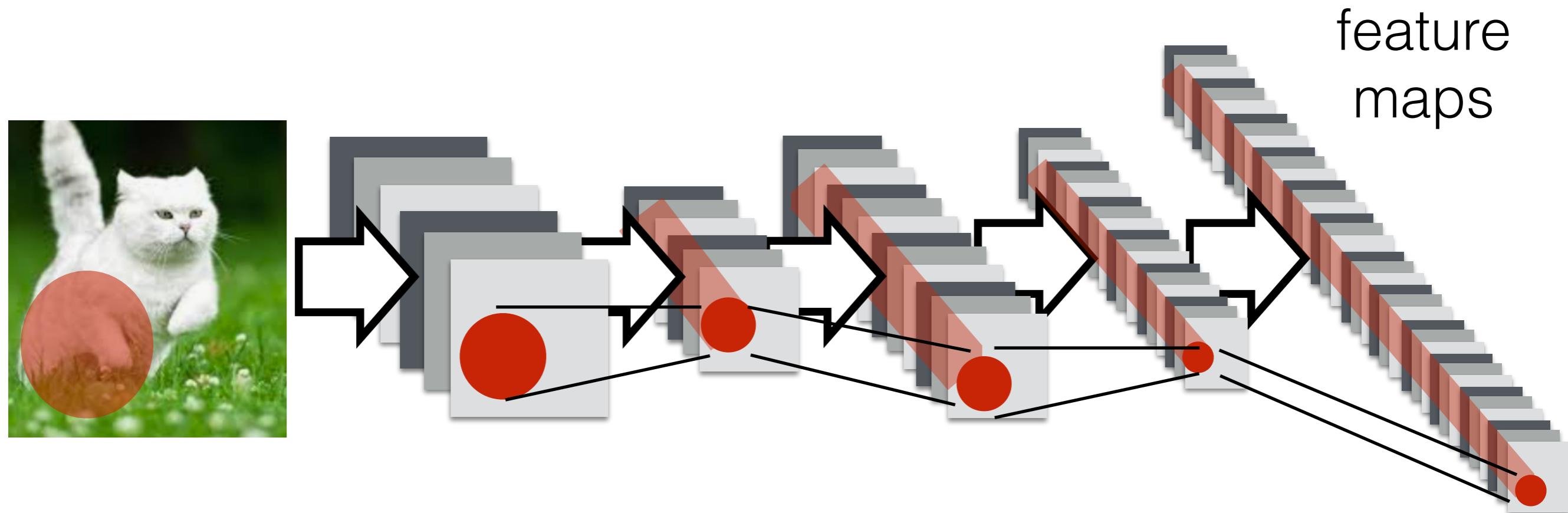


# Feature maps and receptive field

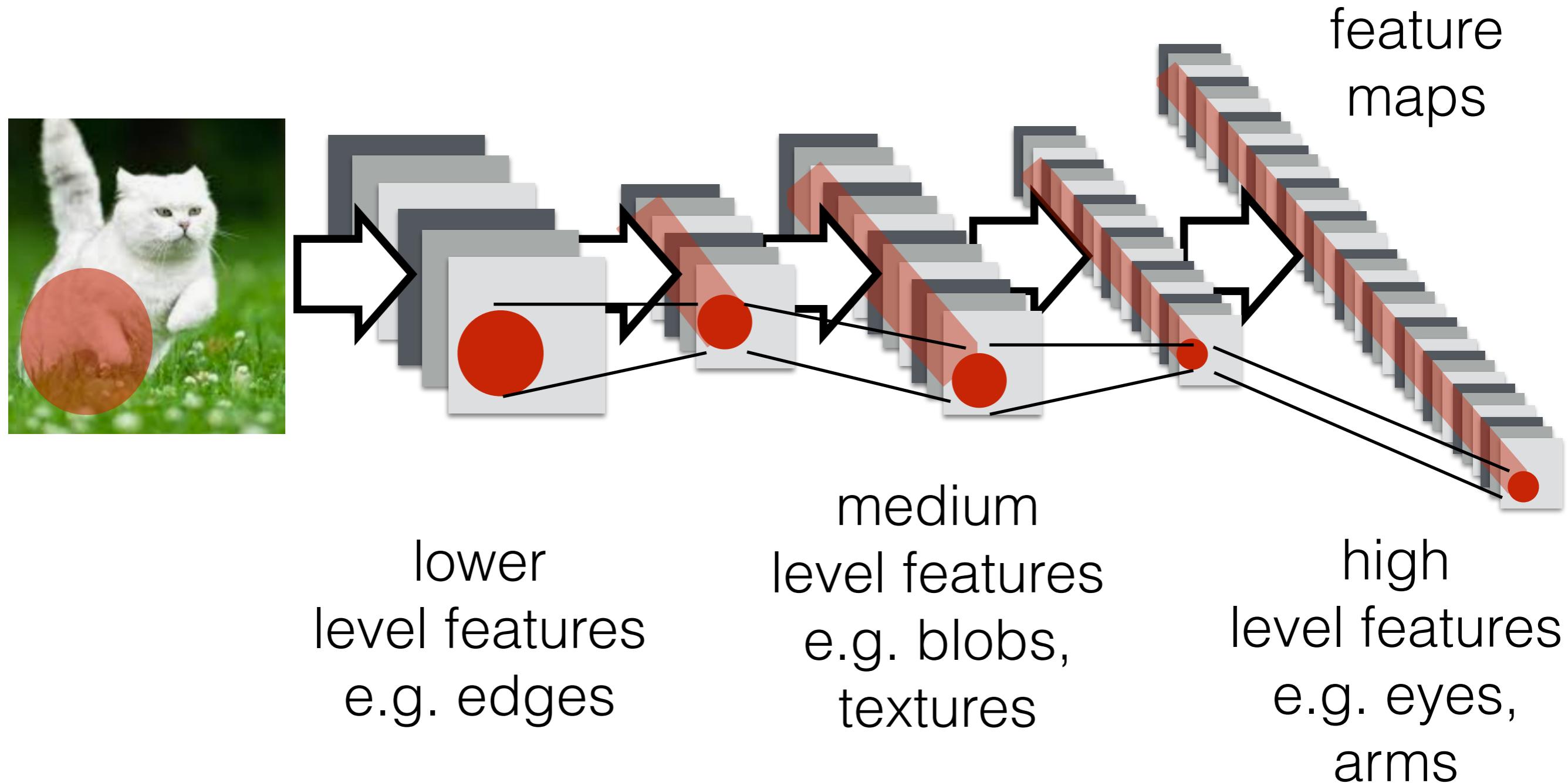
feature  
maps



# Feature maps and receptive field



# Feature maps and receptive field



# Batch normalization

Batch Normalization: Accelerating Deep Network Training by  
Reducing Internal Covariate Shift

Sergey Ioffe  
Google Inc., [sioffe@google.com](mailto:sioffe@google.com)

Christian Szegedy  
Google Inc., [szegedy@google.com](mailto:szegedy@google.com)

`keras.layers.BatchNormalization( . . . )`

suppose we want to use 3 features of a person to do a prediction,

1. height
2. weight
3. hair diameter

We have some issues:

1. units of measurements:
  1. height measure in meters? cm? mm?
  2. weight measure in kg? g? tons?
2. hair feature is going to be a non-factor because hair is so small (in mean and variance) compare to height

use the z score to make all features of equal importance

$$\mu = \frac{1}{n} \sum_i x_i$$

$$\sigma^2 = \frac{1}{n} \sum_i (x_i - \mu)^2$$

$$z_i = \frac{x_i - \mu}{\sigma}$$

[https://en.wikipedia.org/wiki/Standard\\_score](https://en.wikipedia.org/wiki/Standard_score)

use the z score to make all features of equal importance

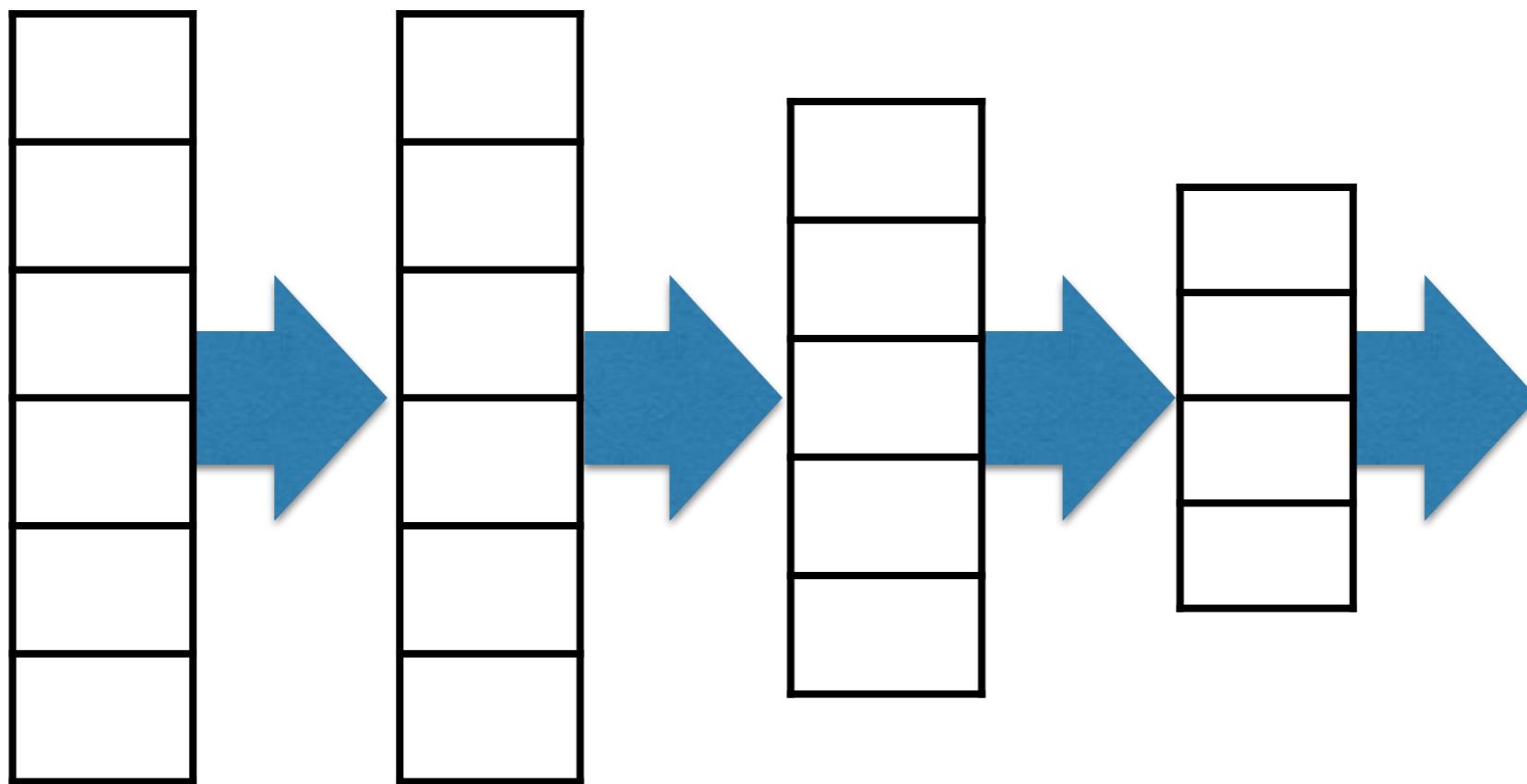
$$\mu = \frac{1}{n} \sum_i x_i$$

$$\sigma^2 = \frac{1}{n} \sum_i (x_i - \mu)^2$$

$$z_i = \frac{x_i - \mu}{\sigma}$$

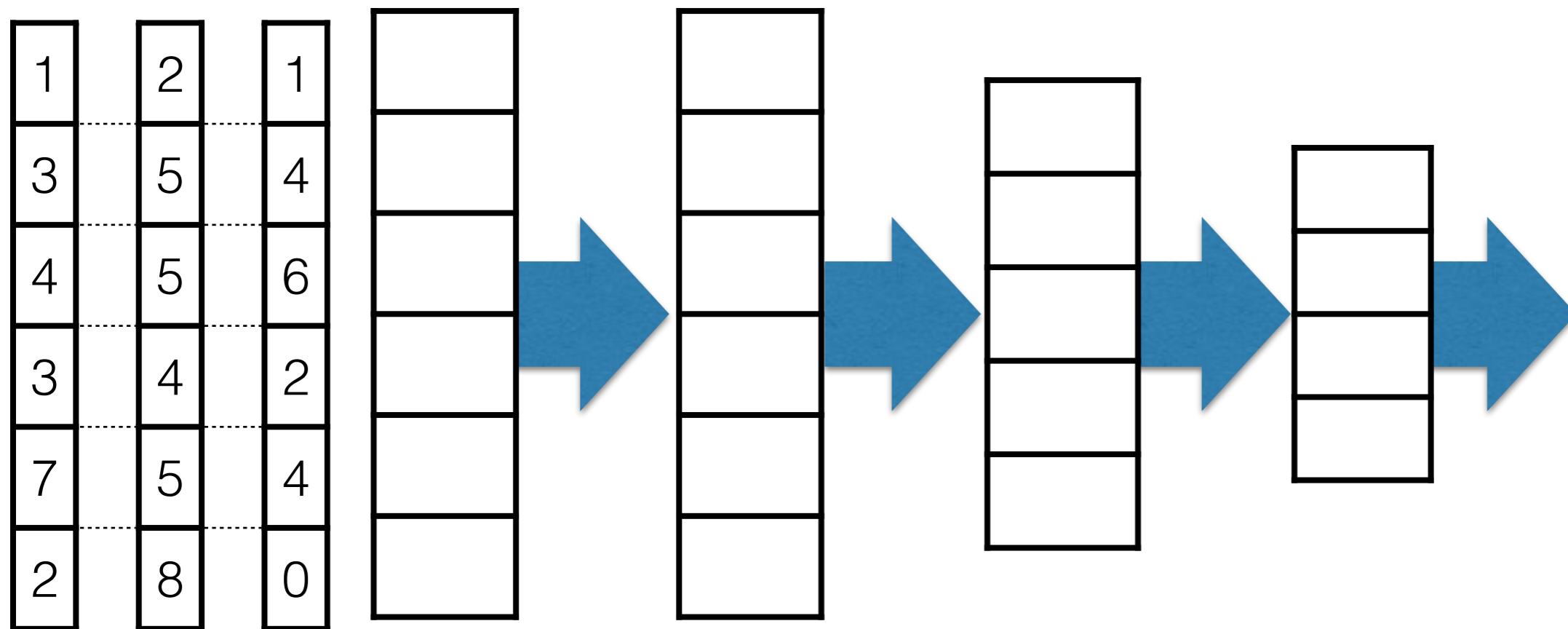
[https://en.wikipedia.org/wiki/Standard\\_score](https://en.wikipedia.org/wiki/Standard_score)

# Feeding in batches - without batch normalization



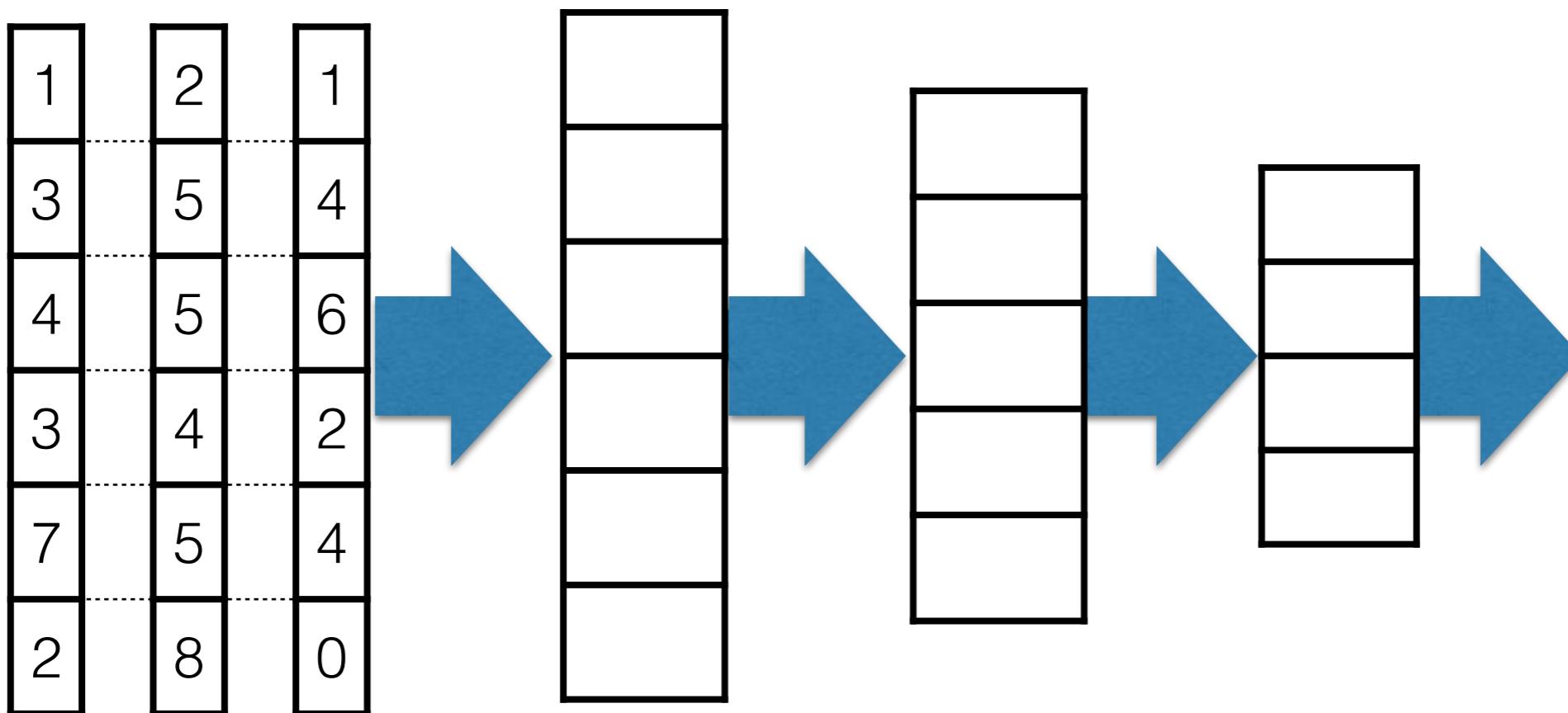
# Feeding in batches - without batch normalization

batch of  
3 data points



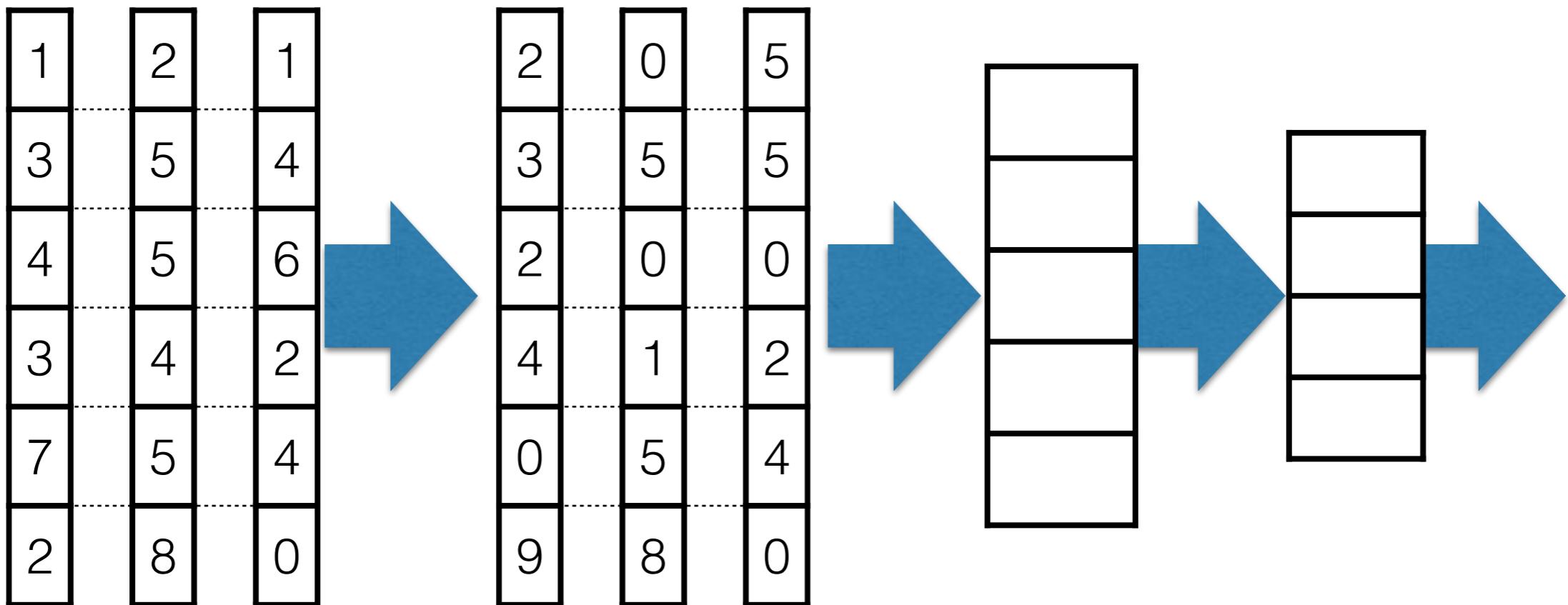
# Feeding in batches - without batch normalization

batch of  
3 data points



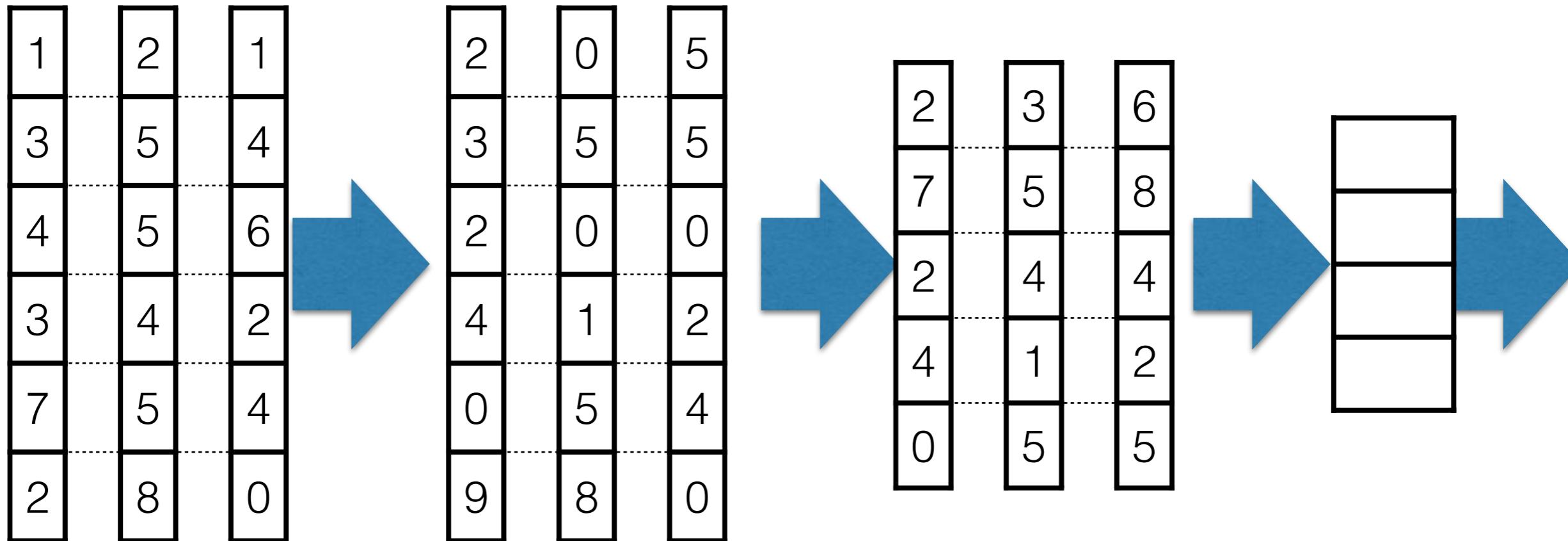
# Feeding in batches - without batch normalization

batch of  
3 data points



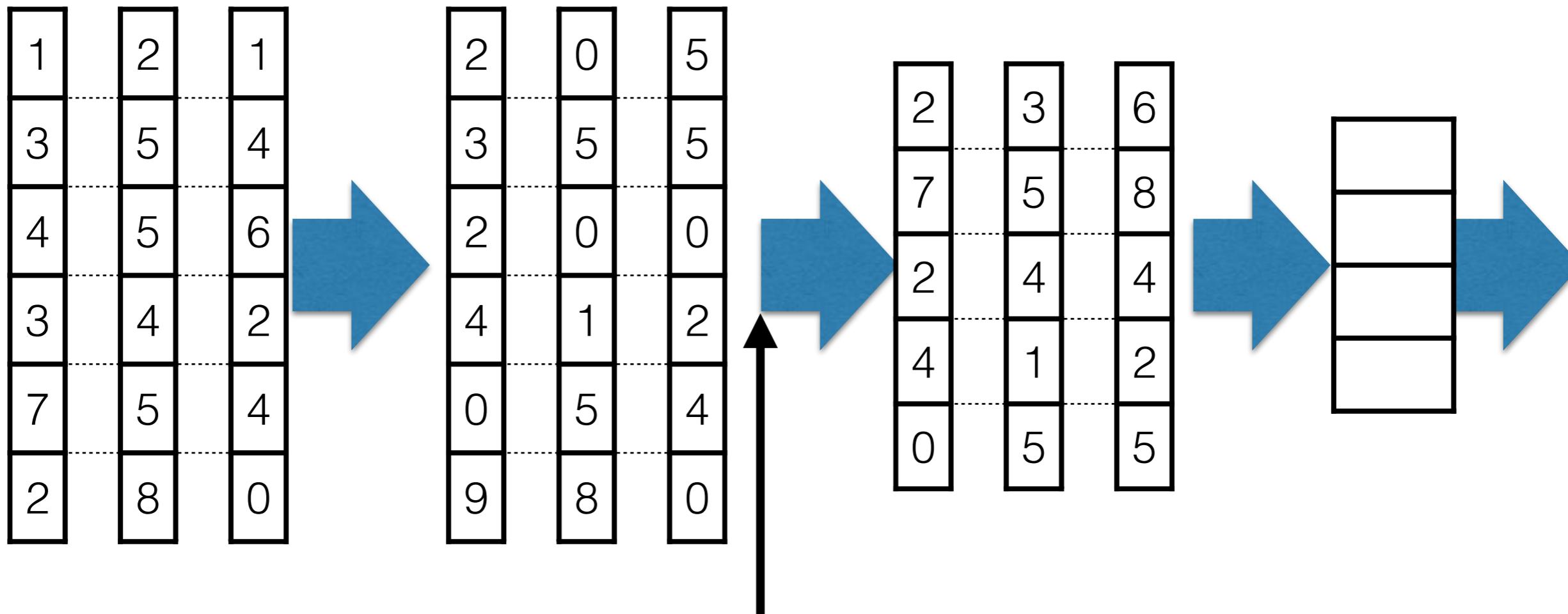
# add batch normalization layer

batch of  
3 data points



add batch normalization layer

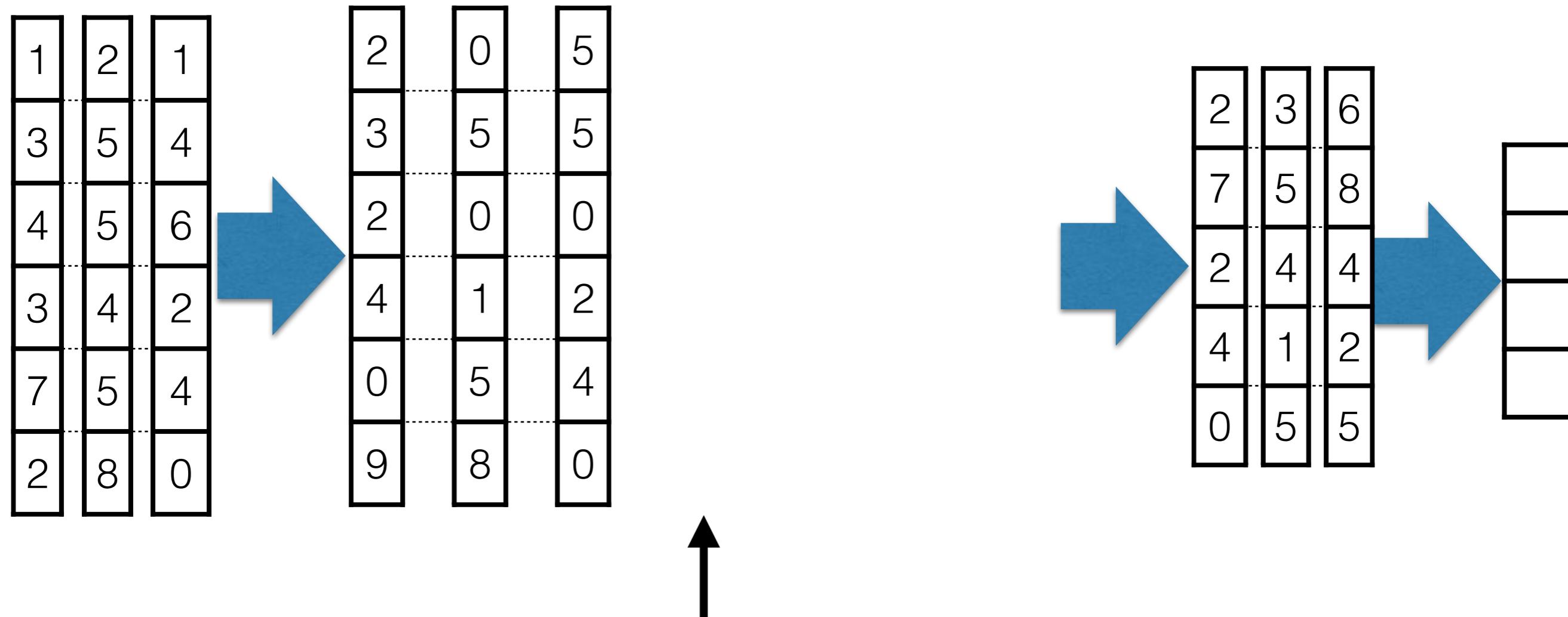
batch of  
3 data points



add batch normalization  
layer here - note: before the  
weights for the next layer

# add batch normalization (BN) layer

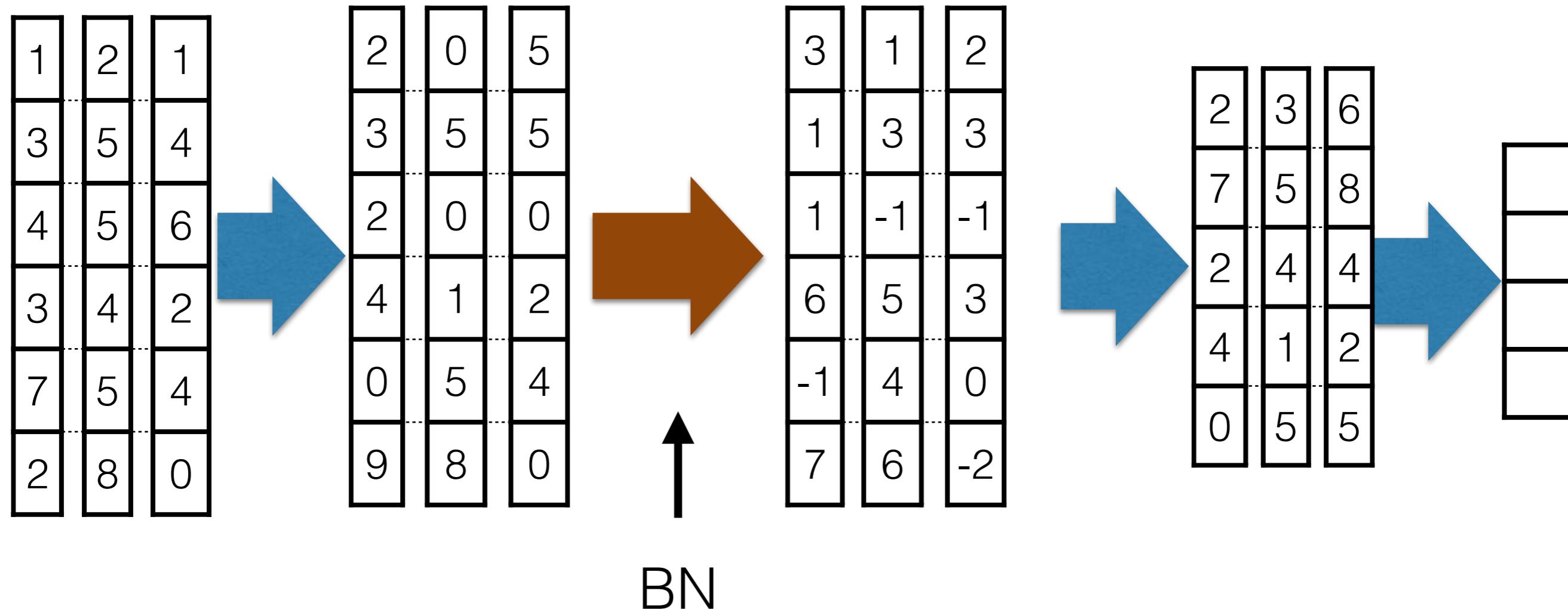
batch of  
3 data points



moved to make space for  
BN

# add batch normalization (BN) layer

batch of  
3 data points



# what happened at BN?

batch of  
3 data points

1	2	1
3	5	4
4	5	6
3	4	2
7	5	4
2	8	0

2	0	5
3	5	5
2	0	0
4	1	2
0	5	4
9	8	0

3	1	2
1	3	3
6	5	3
-1	4	0
7	6	-2

2	3	6
7	5	8
2	4	4
4	1	2
0	5	5

BN

$u_1 = (2+0+5)/3$  — take average

$s_1 = \text{stddev}(2,0,5)$  — take standard deviation

$z_{1,1} = (2-u_1)/s_1$  — transform first data point

$z_{2,1} = (0-u_1)/s_1$  — transform second data point

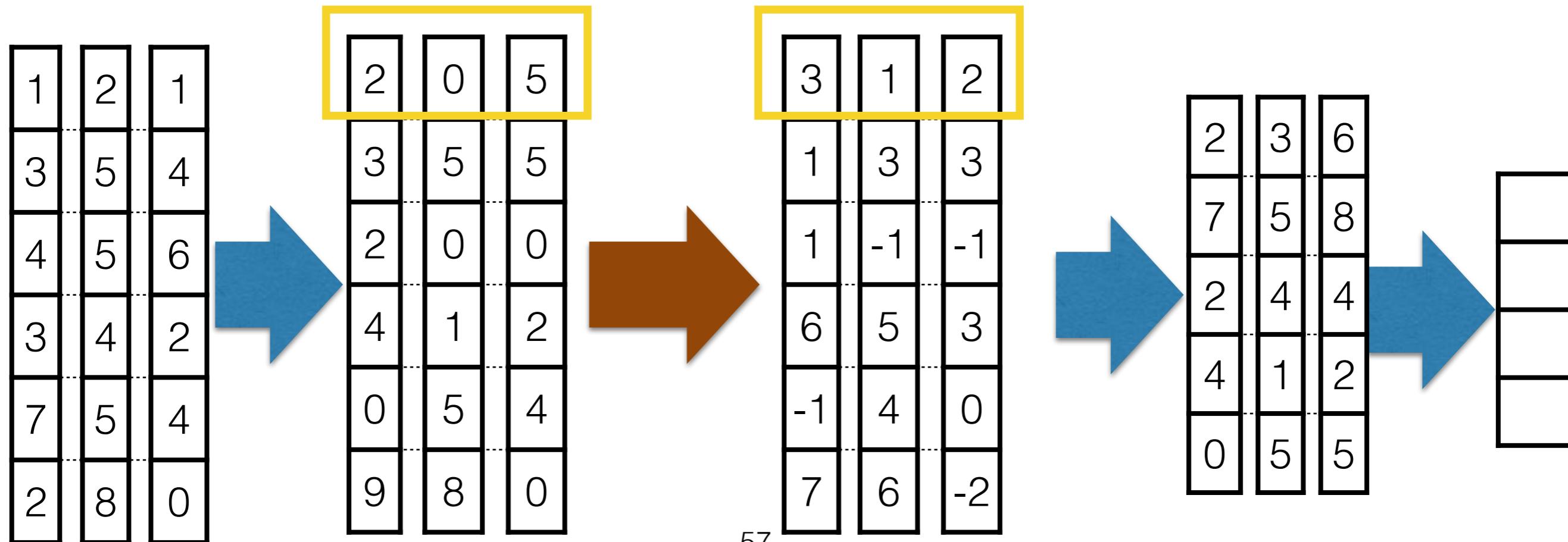
$z_{3,1} = (5-u_1)/s_1$  — transform third data point

$g_1$   $b_1$  are trainable parameters

$$3 = g_1 * z_{1,1} + b_1$$

$$1 = g_1 * z_{2,1} + b_1$$

$$2 = g_1 * z_{3,1} + b_1$$



$u_2 = (3+4+5)/3$  — take average

$s_2 = \text{stddev}(3,5,5)$  — take standard deviation

$z_{1,2} = (3-u_2)/s_2$  — transform first data point

$z_{2,2} = (5-u_2)/s_2$  — transform second data point

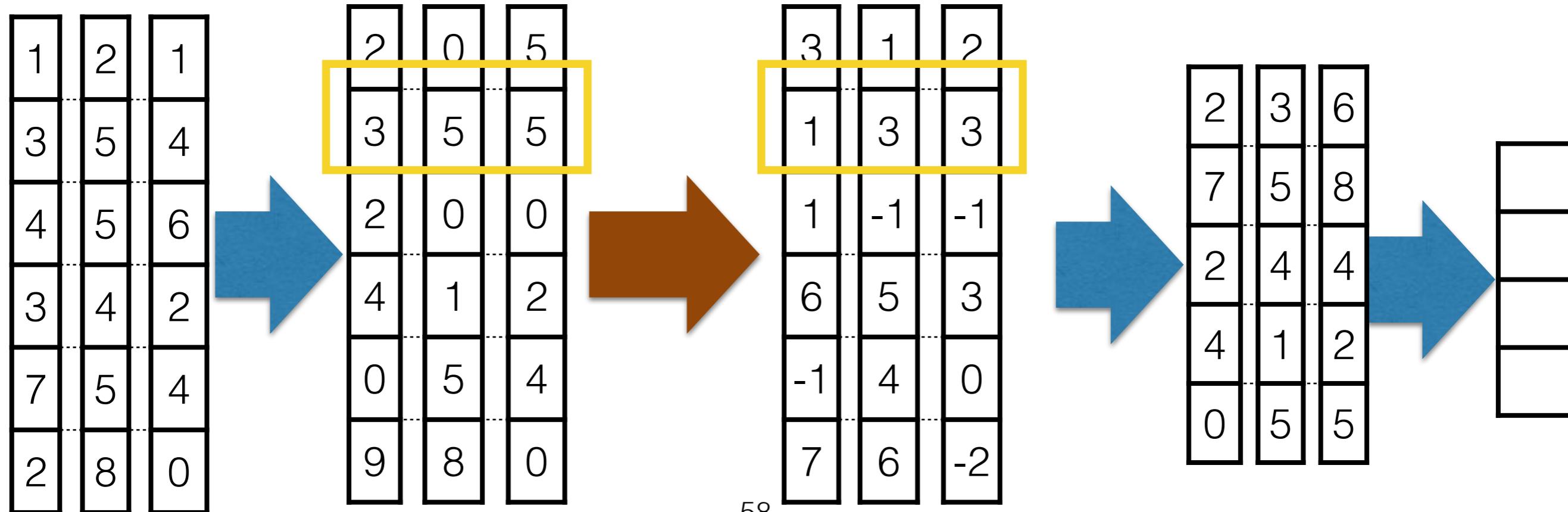
$z_{3,2} = (5-u_2)/s_2$  — transform third data point

$g_2$   $b_2$  are trainable parameters

$$1 = g_2 * z_{1,2} + b_2$$

$$3 = g_2 * z_{2,2} + b_2$$

$$3 = g_2 * z_{3,2} + b_2$$



$u_3 = (2+0+0)/3$  — take average

$s_3 = \text{stddev}(2,0,0)$  — take standard deviation

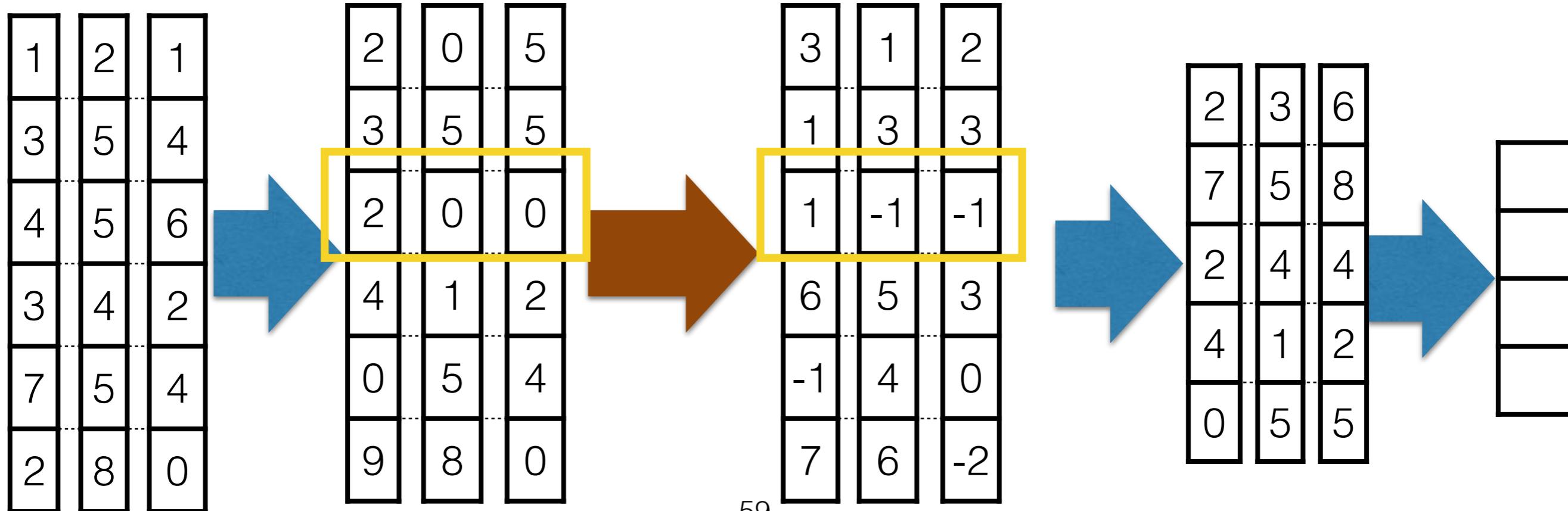
$z_{1,3} = (2-u_3)/s_3$  — transform first data point

$z_{2,3} = (0-u_3)/s_3$  — transform second data point

$z_{3,3} = (0-u_3)/s_3$  — transform third data point

$g_3$   $b_3$  are trainable parameters

$$\begin{aligned} 1 &= g_3 * z_{1,3} + b_3 \\ -1 &= g_3 * z_{2,3} + b_3 \\ -1 &= g_3 * z_{3,3} + b_3 \end{aligned}$$



# Transfer learning

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## How transferable are features in deep neural networks?

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**Jason Yosinski,<sup>1</sup> Jeff Clune,<sup>2</sup> Yoshua Bengio,<sup>3</sup> and Hod Lipson<sup>4</sup>**

<sup>1</sup> Dept. Computer Science, Cornell University

<sup>2</sup> Dept. Computer Science, University of Wyoming

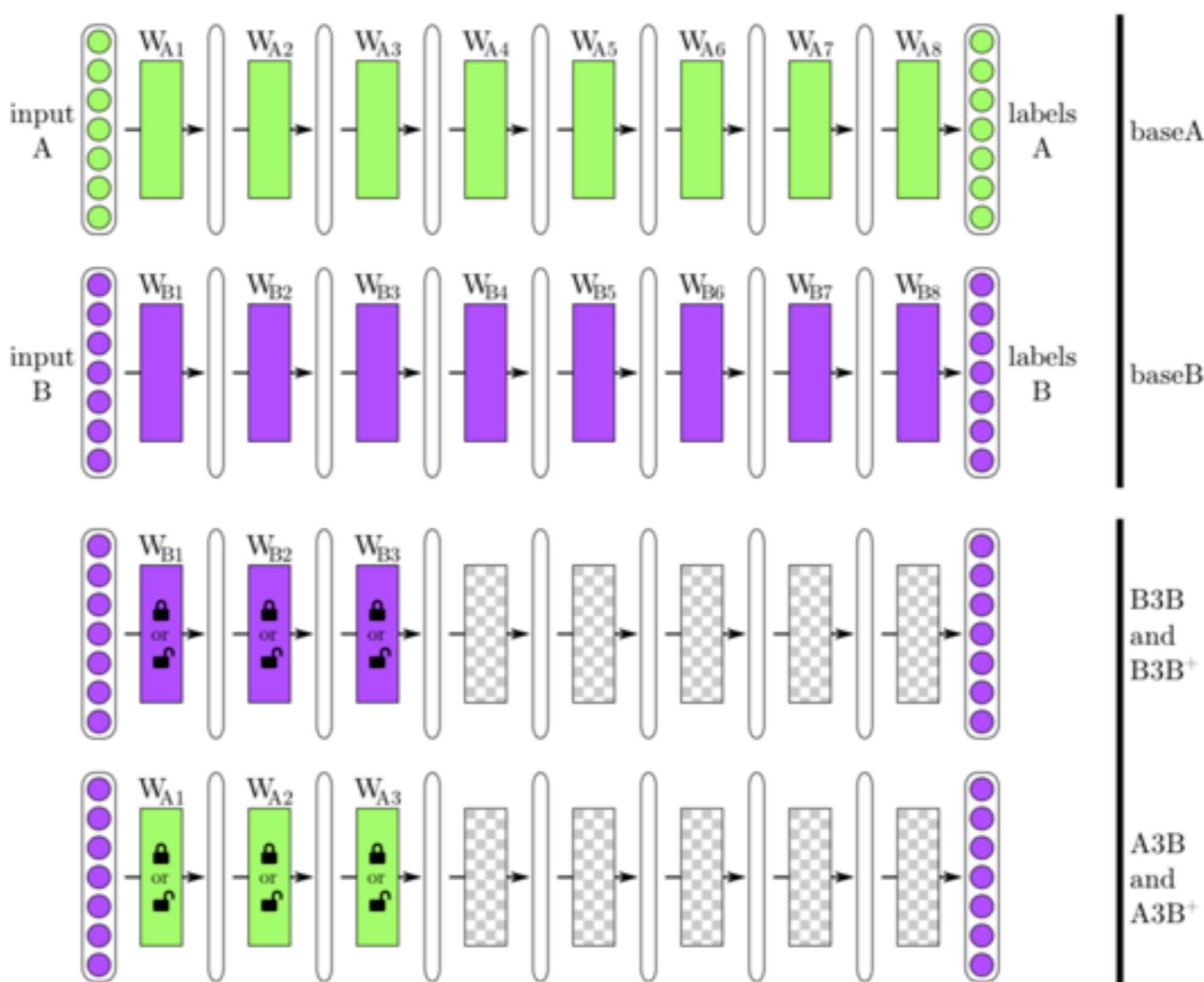
<sup>3</sup> Dept. Computer Science & Operations Research, University of Montreal

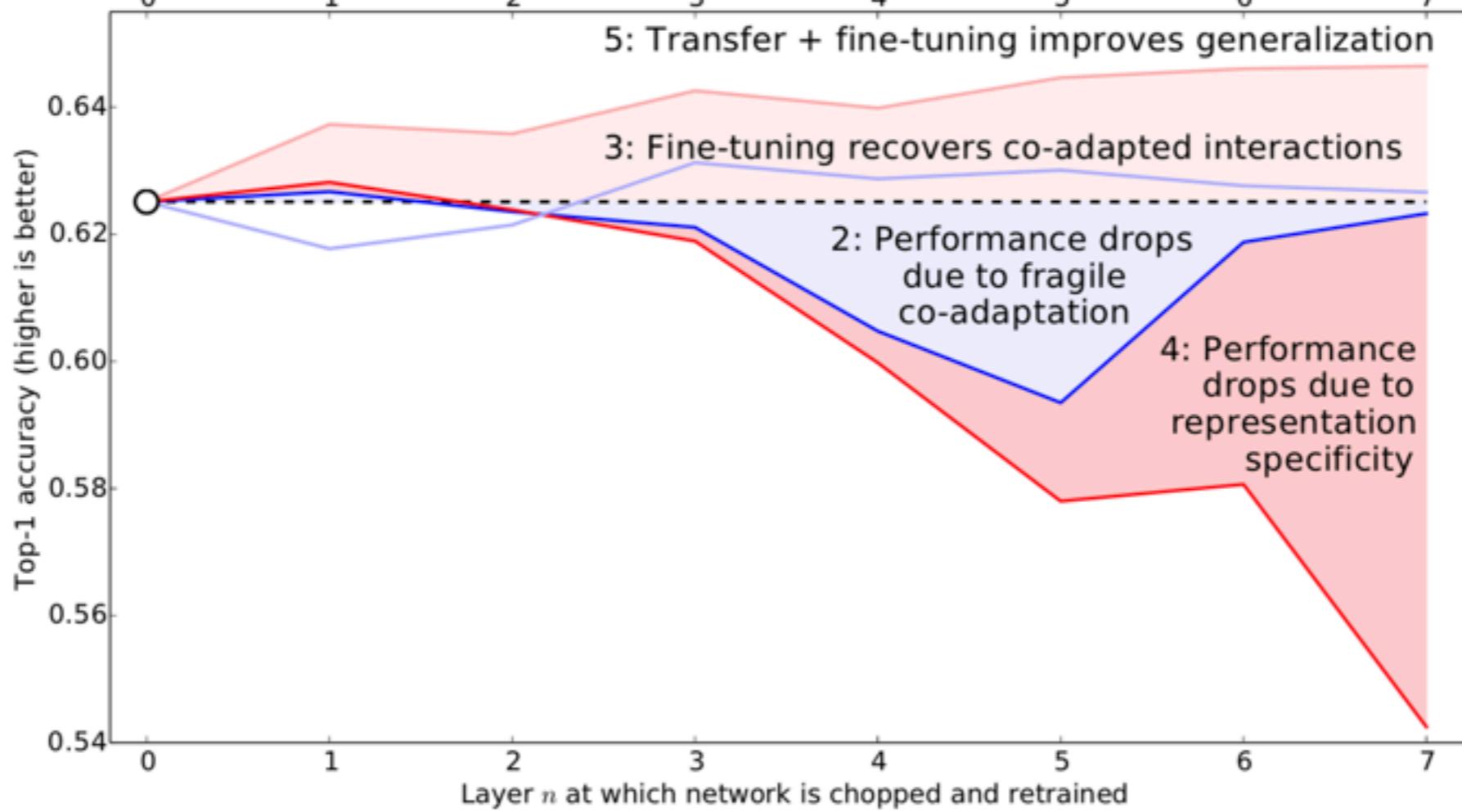
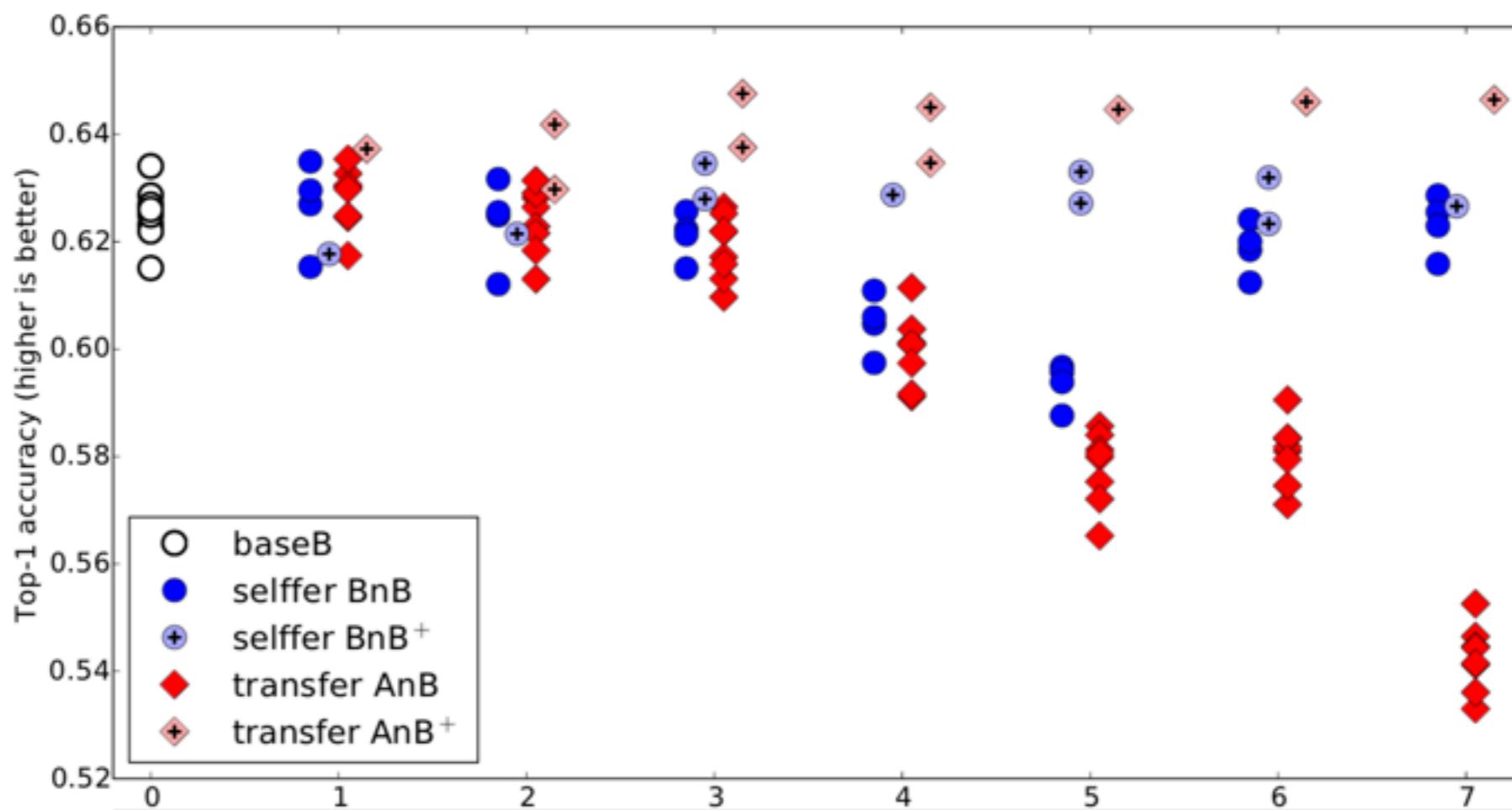
<sup>4</sup> Dept. Mechanical & Aerospace Engineering, Cornell University

image-net 1000class. randomly split

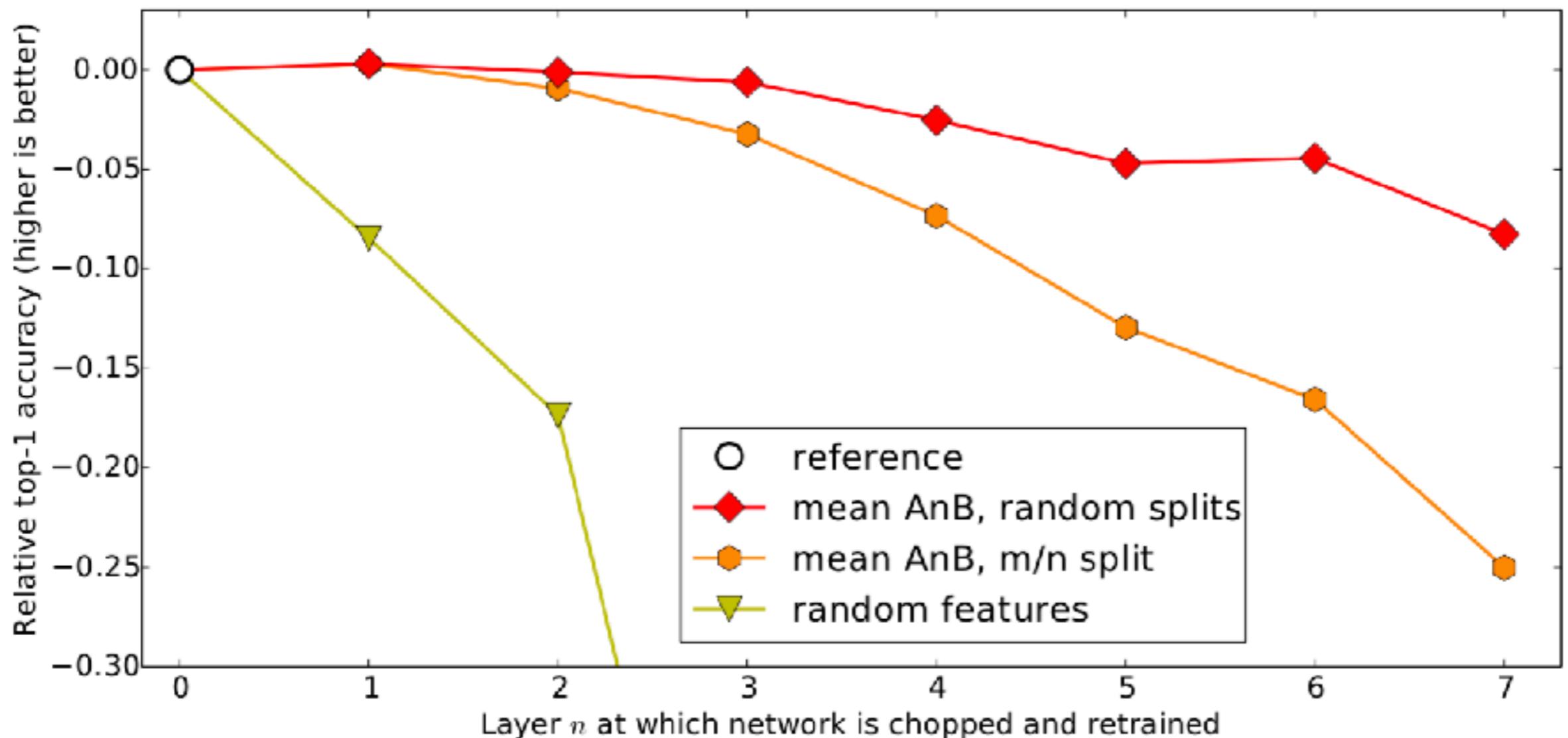
500 ->A, 500 -> B

train A, transfer to B and vice versa  
e.g. A to A, B to B, A to B, B to A





# split and transfer between man-made and natural images



thinking time  
& question time again

when do we use transfer learning?

how do we check if transfer learning is good?

## Image data augmentation

- 1.to increase the amount of data > 10x data
- 2.to make the CNN more robust to transformation in images

original image



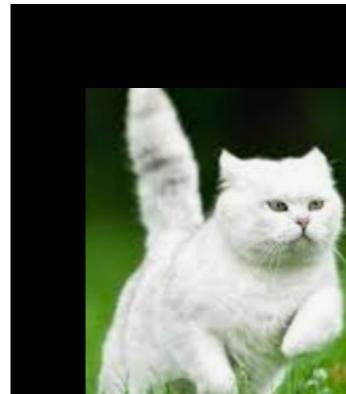
scaling



flipping



translation

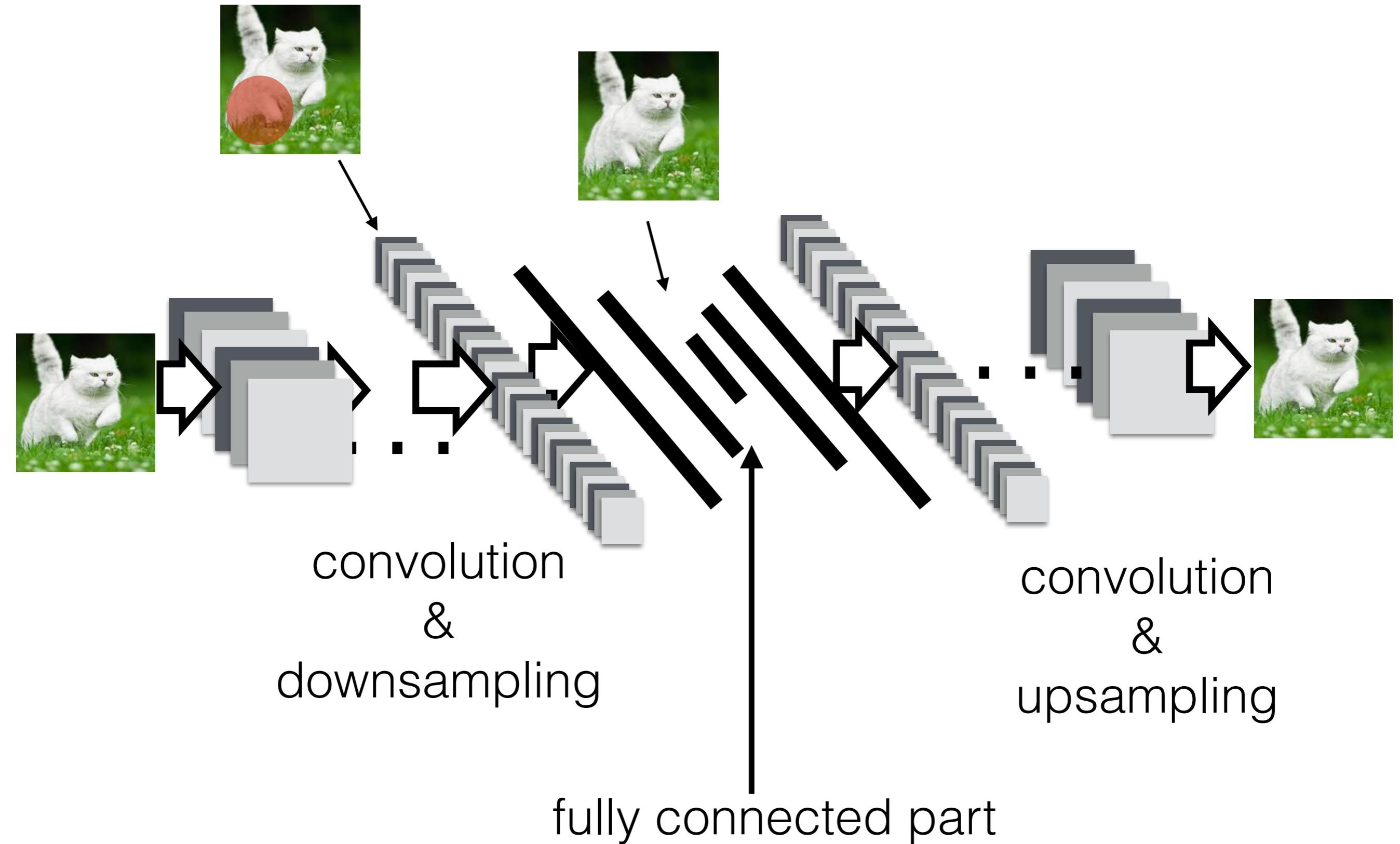


rotation

using another neural network to generate data  
Generative Adversarial Networks (GAN)

# CNN with autoencoder

# CNN auto encoder



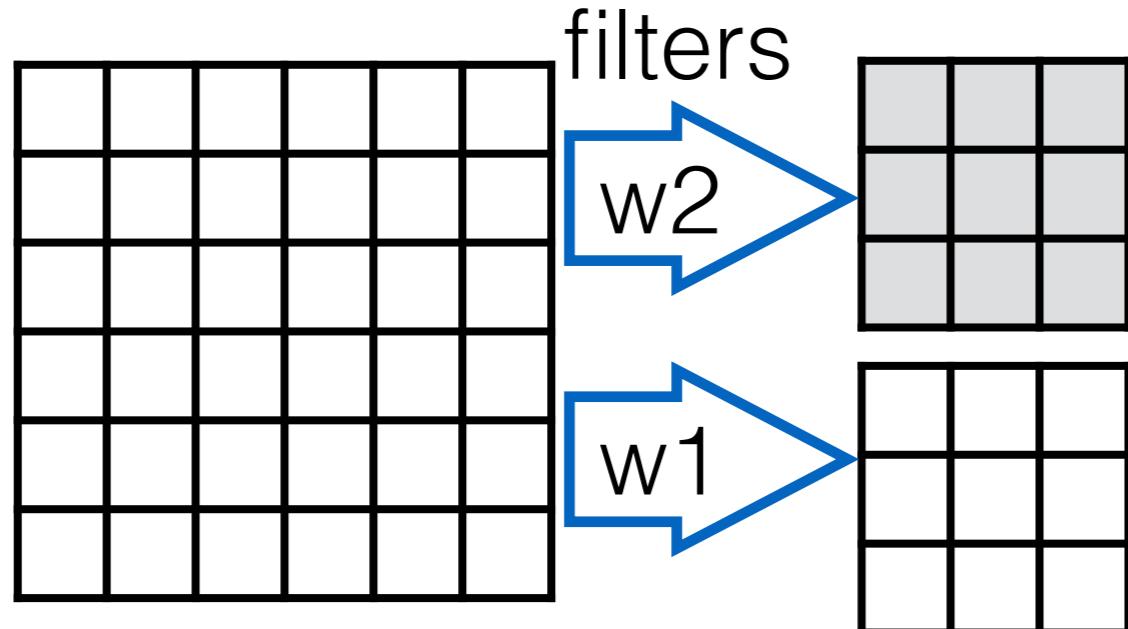
# Region Of Interest Pooling

## ROI - Pooling

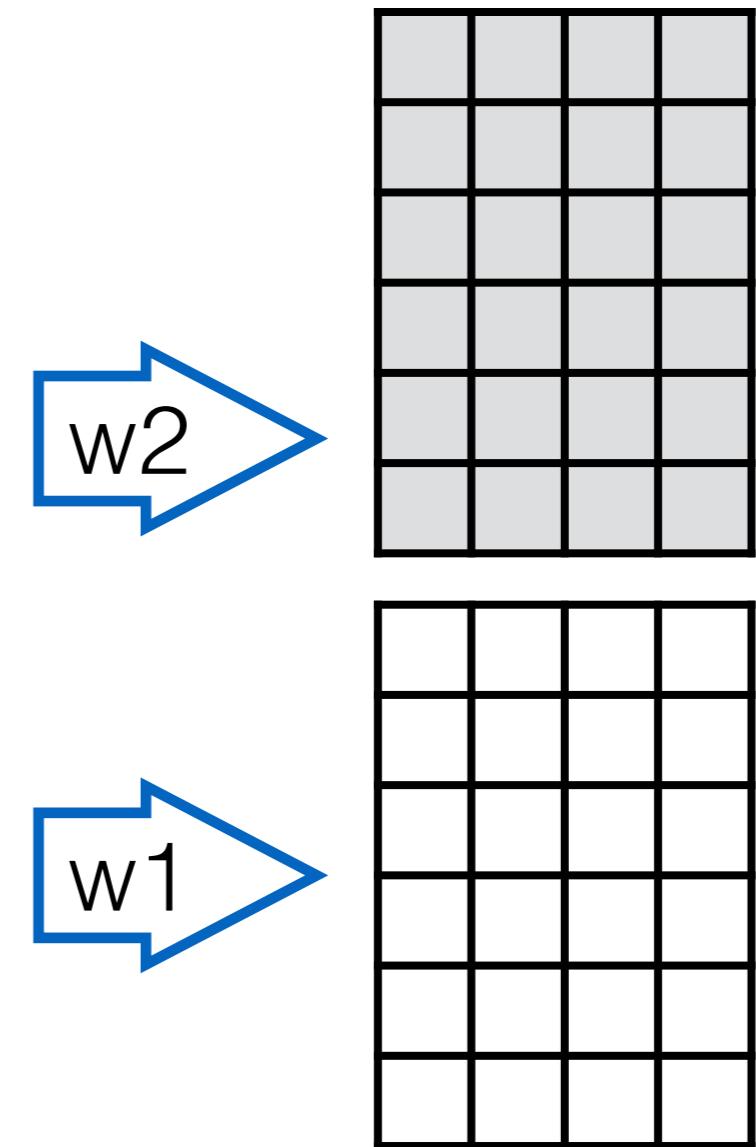
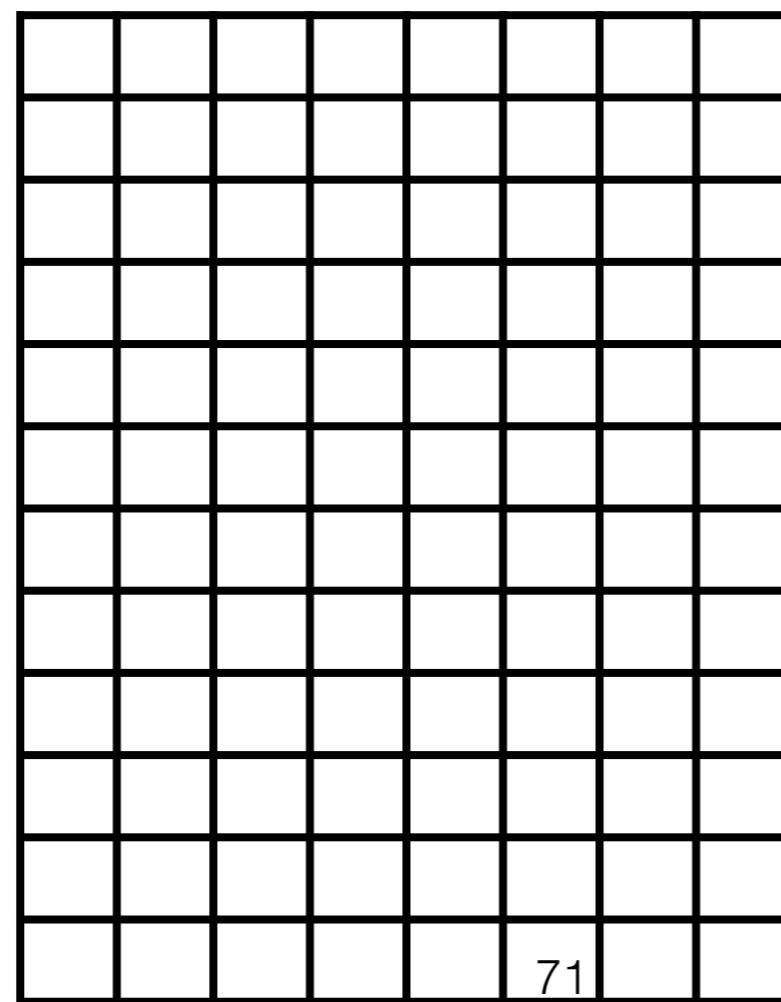
<https://deepsense.ai/region-of-interest-pooling-explained/>

CNN part of the network can take image of any size

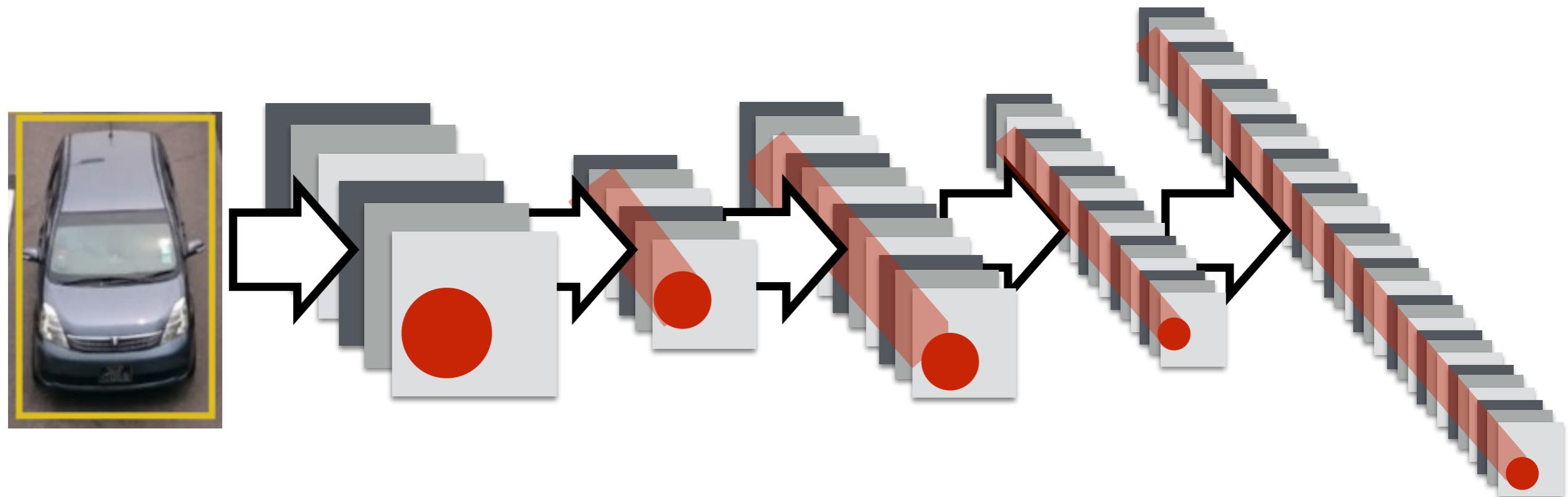
2x2 kernel, stride=(2,2)



same filters can be used for different image sizes to generate feature maps



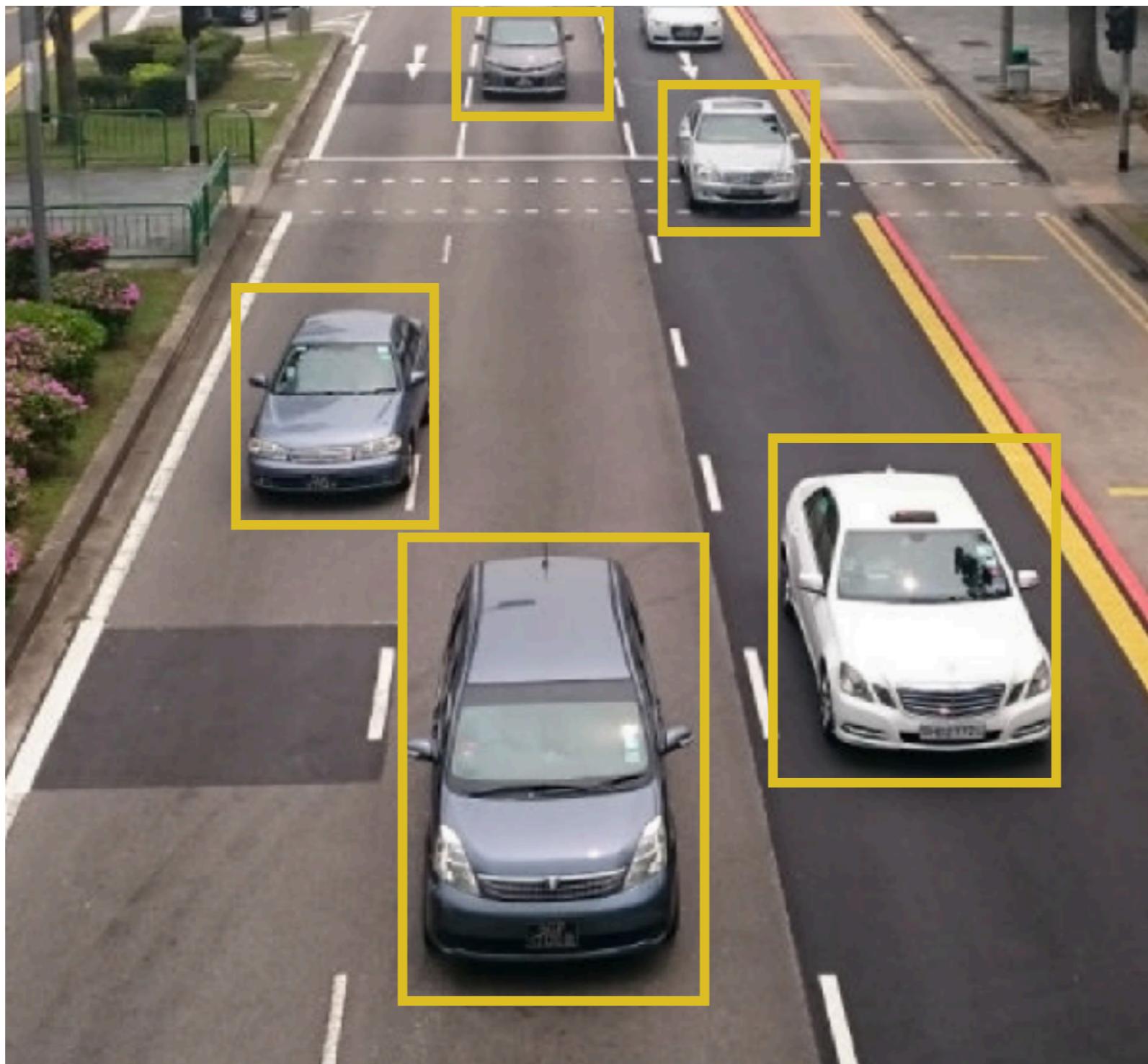
# CNN to convert images into feature maps



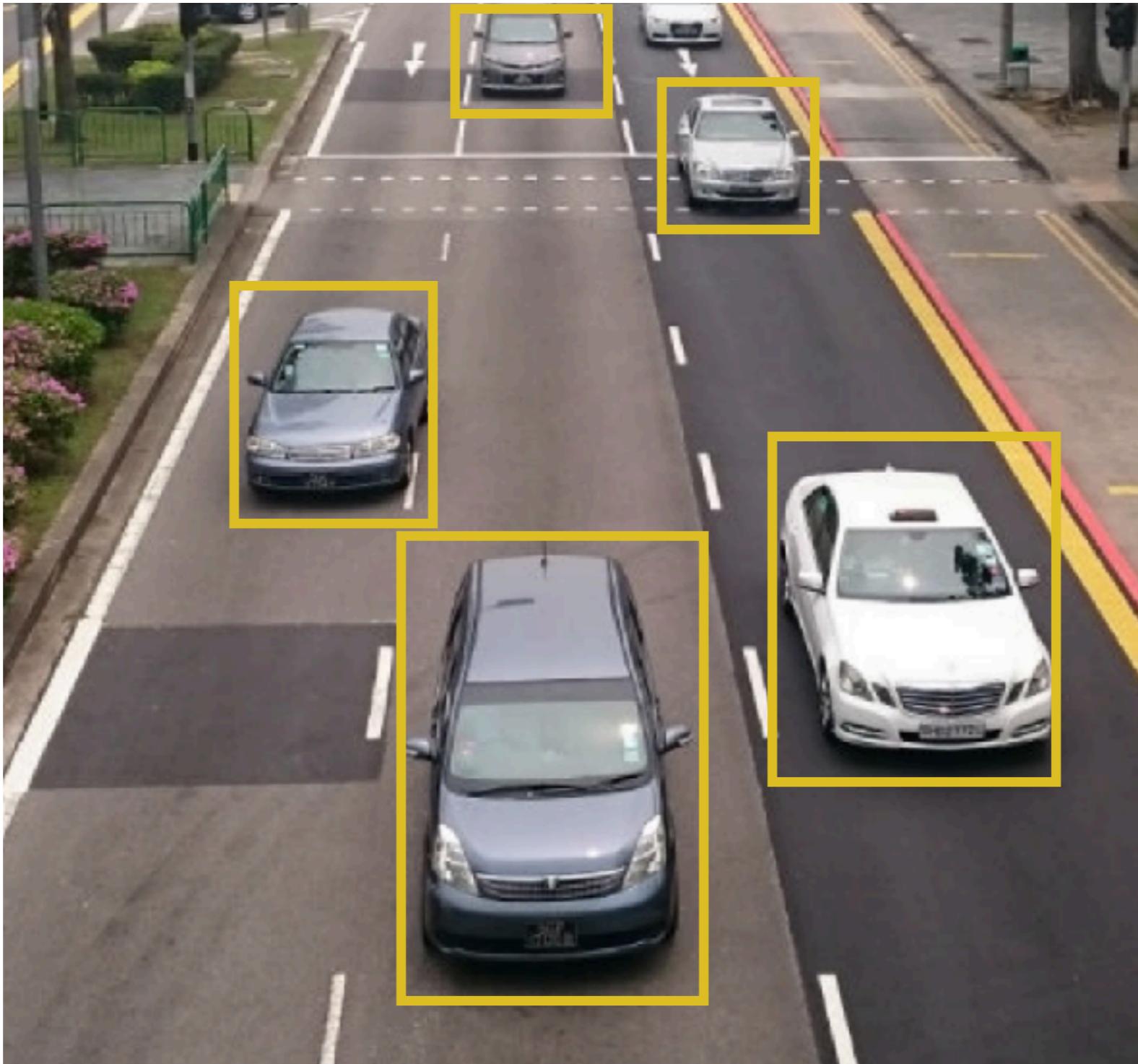
want to detect cars on a road



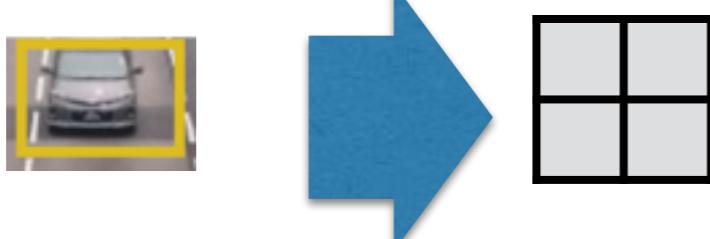
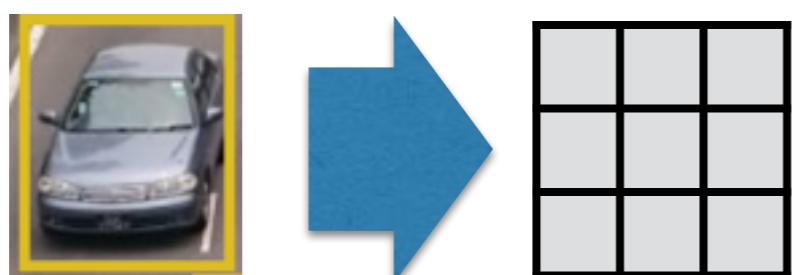
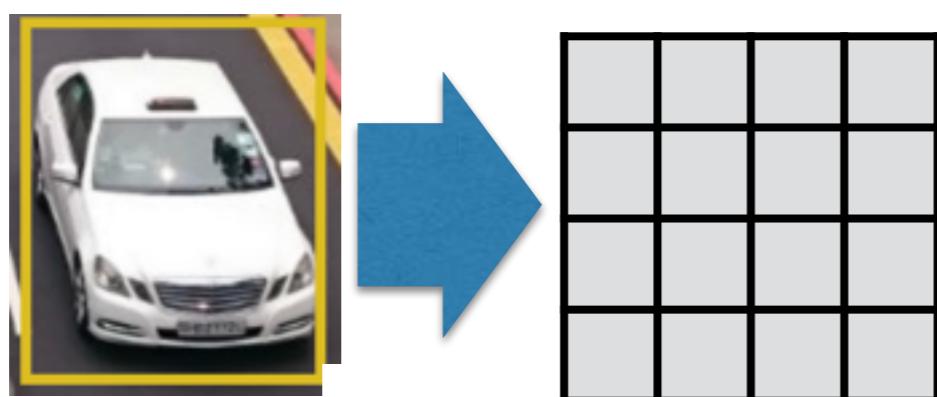
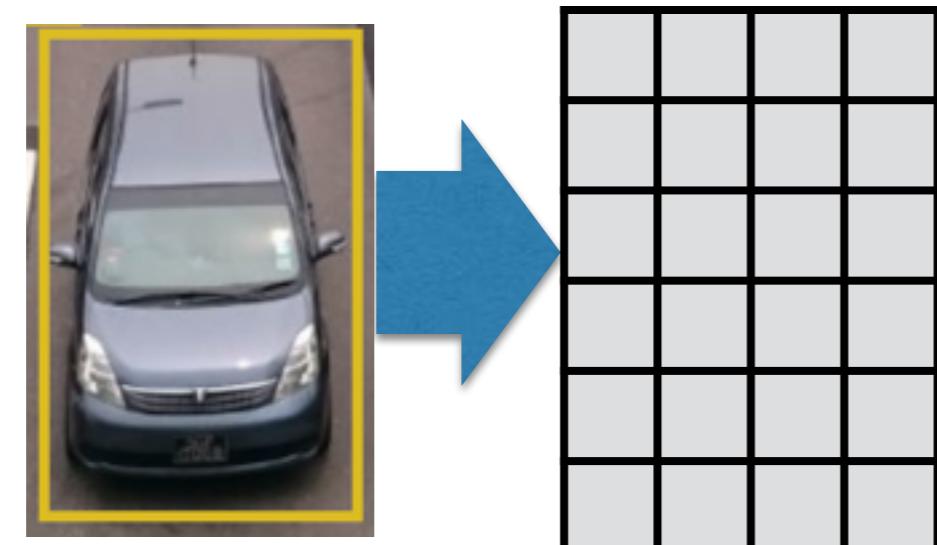
propose different regions to CNN



feed these regions into CNN and ask if  
there is a car in proposed region



use conv part of CNN to convert ROIs into feature maps



# feed feature maps into the rest of CNN

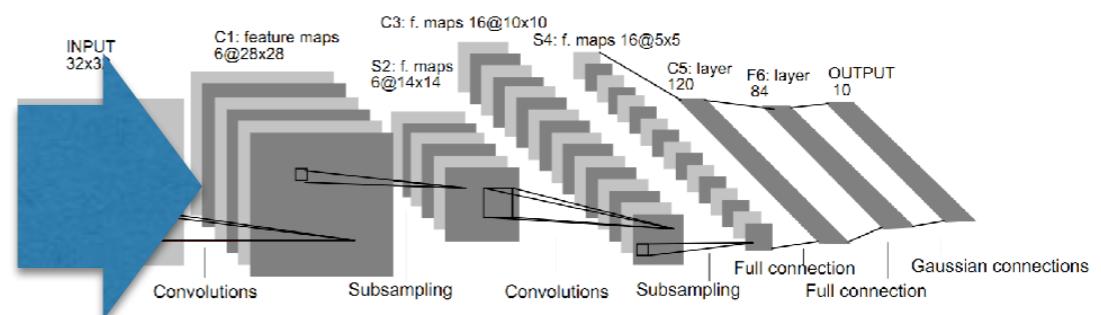
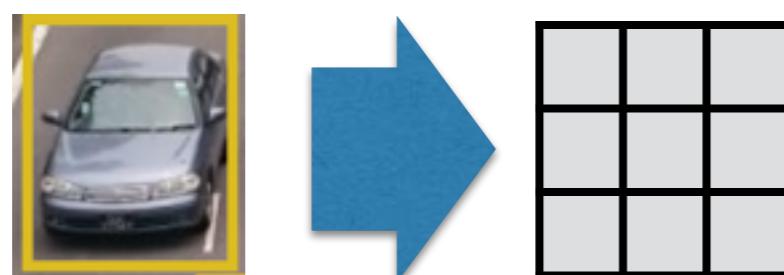
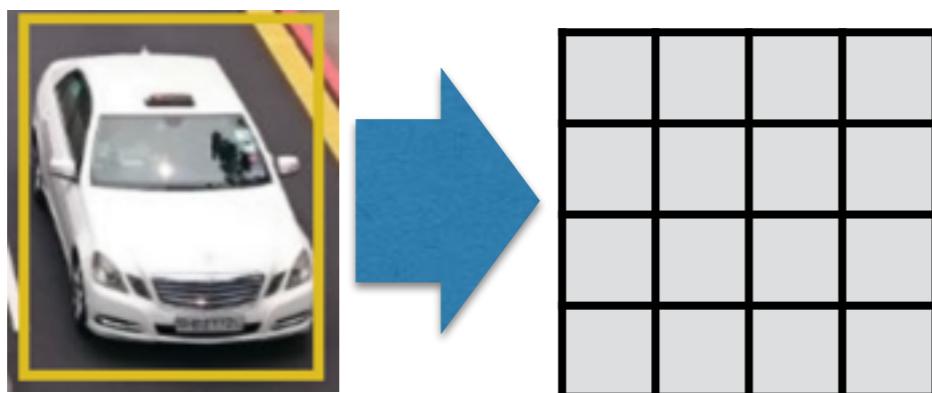
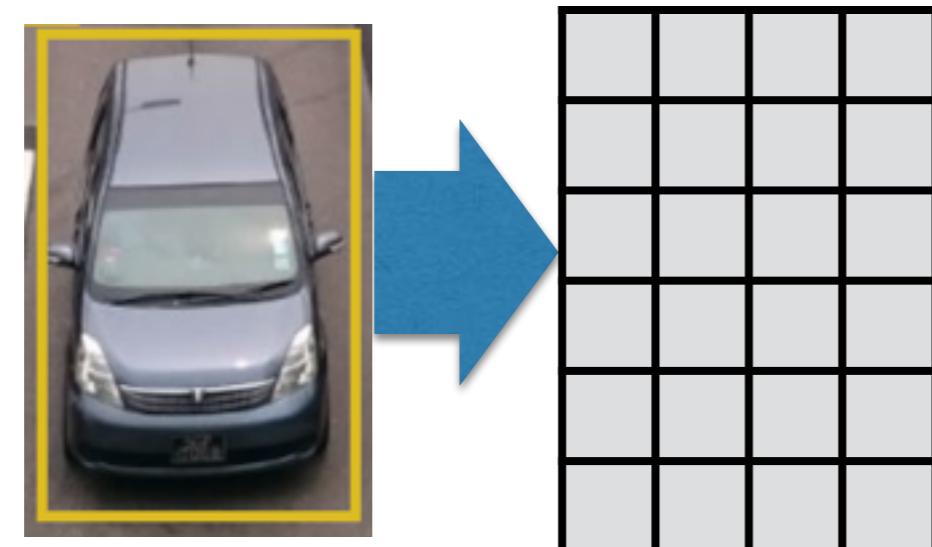


Fig. 2. Architecture of LeNet-5, a Convolutional Neural Network, here for digits recognition. Each plane is a feature map, i.e. a set of units whose weights are constrained to be identical.

CNN

problem is feature  
maps are of  
different sizes!

## Solutions

1. resize / reshape the feature maps before feeding
2. Region of interest pooling (ROI pooling)

# ROI - Pooling example

1	2	6	2	8	2	0
4	7	1	3	5	2	4
3	0	7	4	5	2	9
9	1	2	7	0	3	0

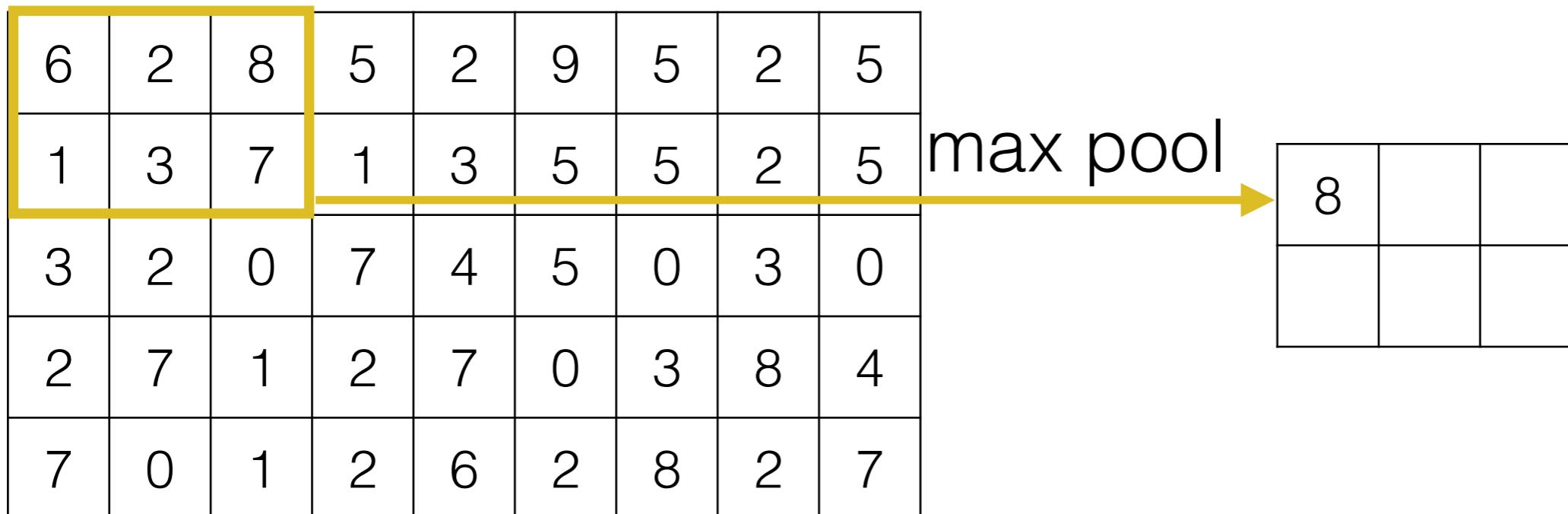
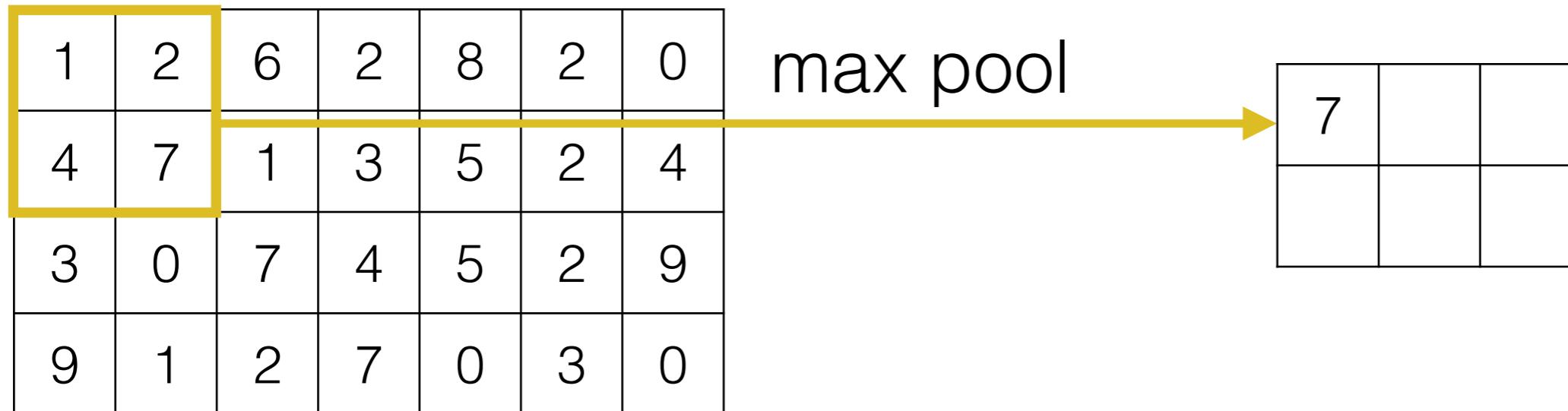
6	2	8	5	2	9	5	2	5
1	3	7	1	3	5	5	2	5
3	2	0	7	4	5	0	3	0
2	7	1	2	7	0	3	8	4
7	0	1	2	6	2	8	2	7

reduce these two ROI into 3x2 pixels features

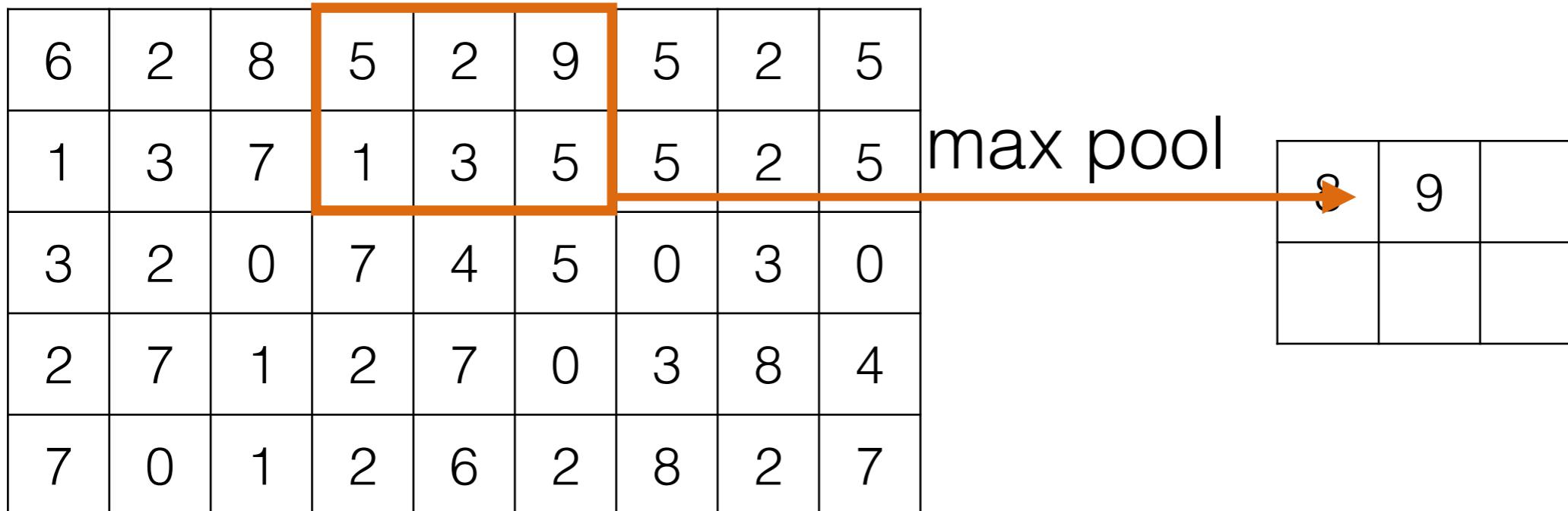
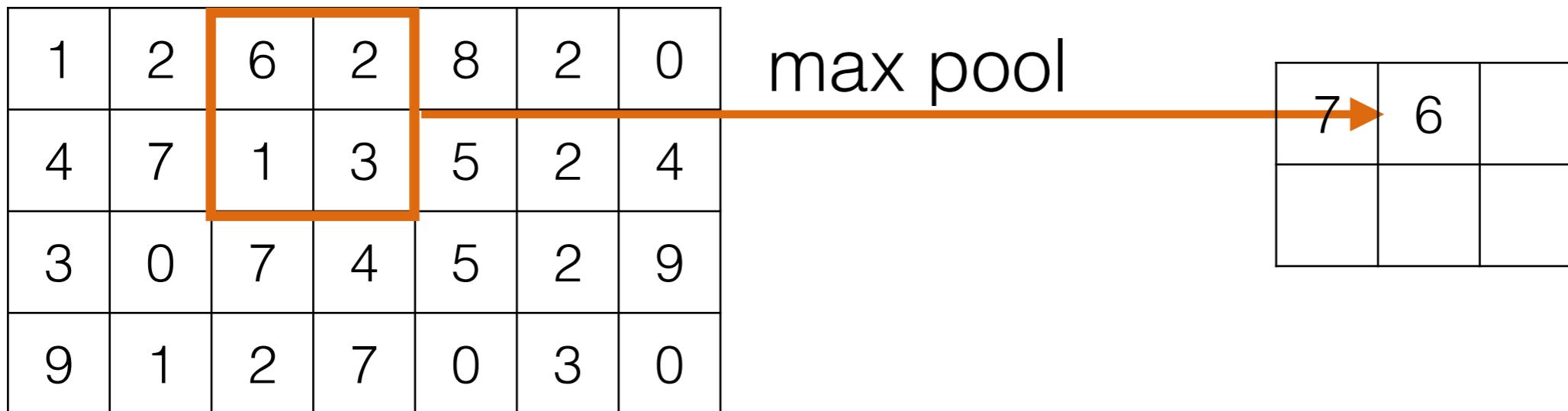
1	2	6	2	8	2	0
4	7	1	3	5	2	4
3	0	7	4	5	2	9
9	1	2	7	0	3	0

6	2	8	5	2	9	5	2	5
1	3	7	1	3	5	5	2	5
3	2	0	7	4	5	0	3	0
2	7	1	2	7	0	3	8	4
7	0	1	2	6	2	8	2	7

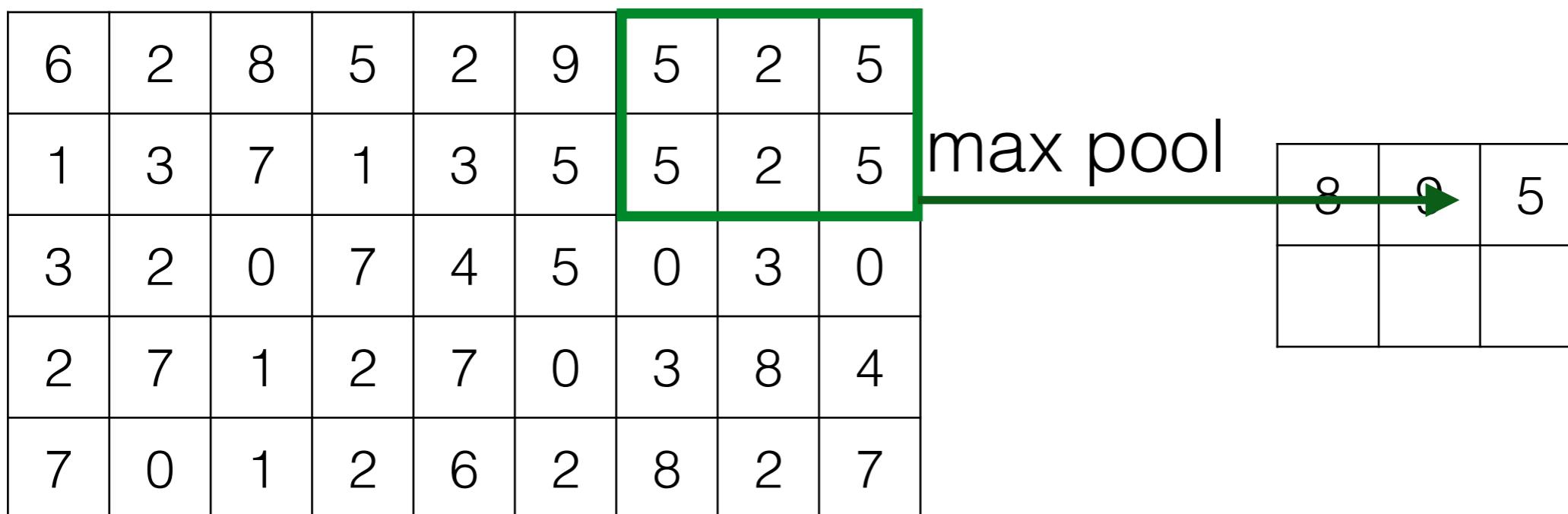
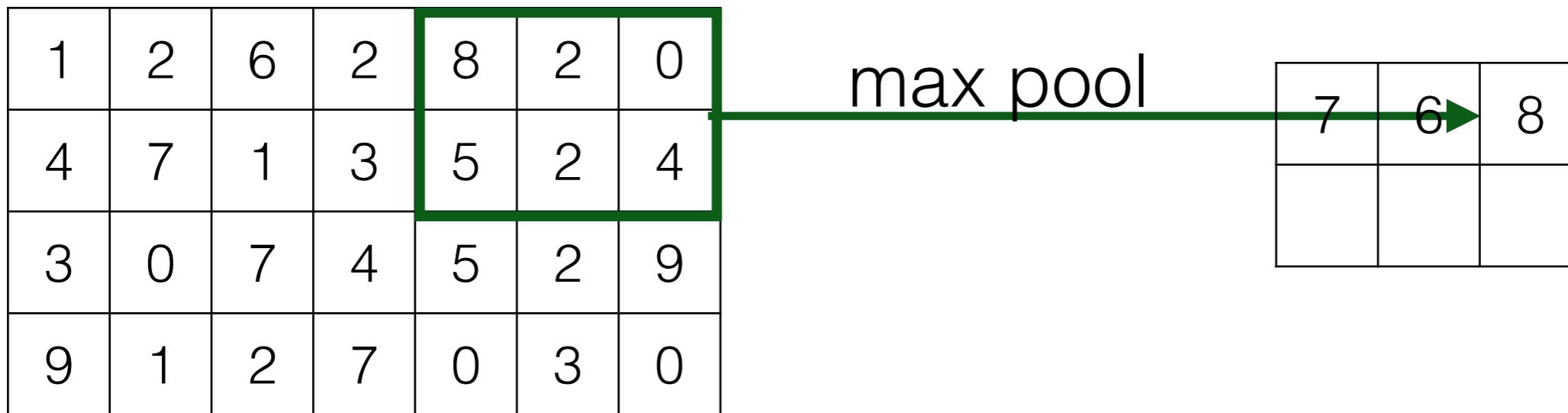
reduce these two ROI into 3x2 pixels features



reduce these two ROI into 3x2 pixels features



reduce these two ROI into 3x2 pixels features



reduce these two ROI into 3x2 pixels features

1	2	6	2	8	2	0
4	7	1	3	5	2	4
3	0	7	4	5	2	9
9	1	2	7	0	3	0

7	6	8
9		

6	2	8	5	2	9	5	2	5
1	3	7	1	3	5	5	2	5
3	2	0	7	4	5	0	3	0
2	7	1	2	7	0	3	8	4
7	0	1	2	6	2	8	2	7

8	9	5
7		

reduce these two ROI into 3x2 pixels features

1	2	6	2	8	2	0
4	7	1	3	5	2	4
3	0	7	4	5	2	9
9	1	2	7	0	3	0

7	6	8
9	7	

6	2	8	5	2	9	5	2	5
1	3	7	1	3	5	5	2	5
3	2	0	7	4	5	0	3	0
2	7	1	2	7	0	3	8	4
7	0	1	2	6	2	8	2	7

8	9	5
7	7	

reduce these two ROI into 3x2 pixels features

1	2	6	2	8	2	0
4	7	1	3	5	2	4
3	0	7	4	5	2	9
9	1	2	7	0	3	0

7	6	8
9	7	9

6	2	8	5	2	9	5	2	5
1	3	7	1	3	5	5	2	5
3	2	0	7	4	5	0	3	0
2	7	1	2	7	0	3	8	4
7	0	1	2	6	2	8	2	7

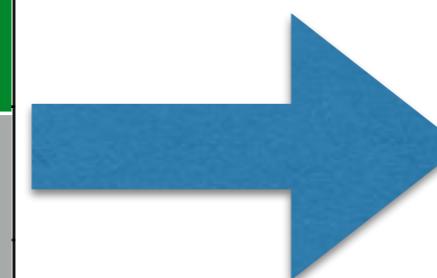
8	9	5
7	8	8

1	2	6	2	8	2	0
4	7	1	3	5	2	4
3	0	7	4	5	2	9
9	1	2	7	0	3	0



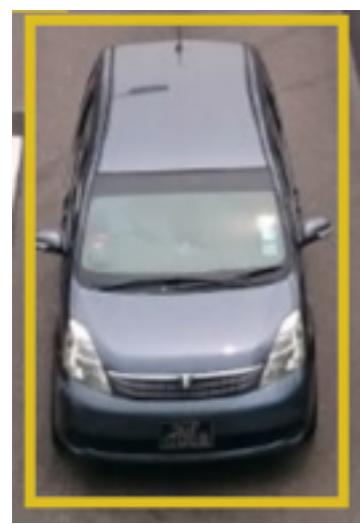
7	6	8
9	7	9

6	2	8	5	2	9	5	2	5
1	3	7	1	3	5	5	2	5
3	2	0	7	4	5	0	3	0
2	7	1	2	7	0	3	8	4
7	0	1	2	6	2	8	2	7

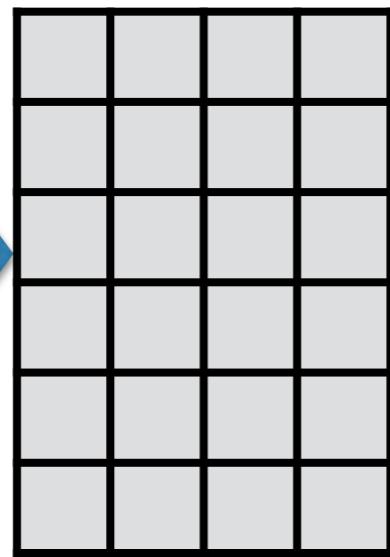


8	9	5
7	7	8

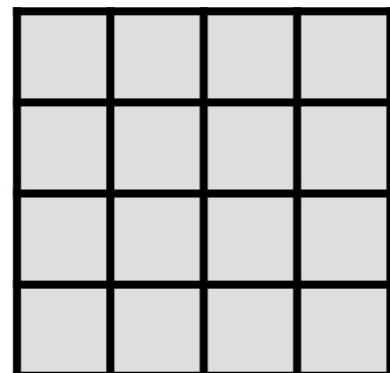
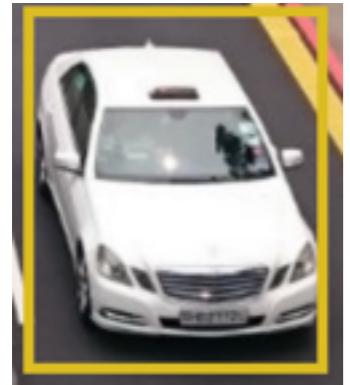
image



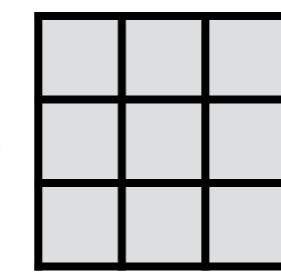
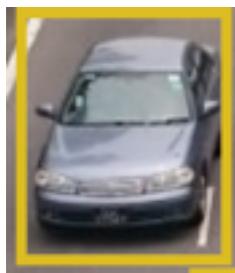
feature maps



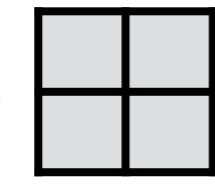
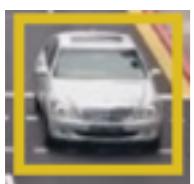
ROI  
pooling



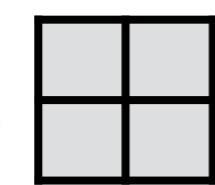
ROI  
pooling



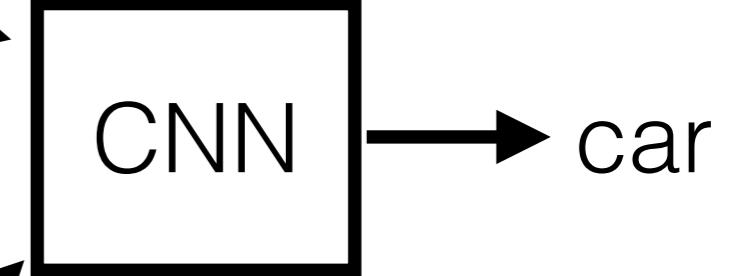
ROI  
pooling



ROI  
pooling



ROI  
pooling



To avoid just following what others do without understanding, we need to ask questions!

Any questions?

- 1.Why do ROI pooling on feature maps and not do ROI pooling on the original image?
- 2.why not rescale all the image to the same size?

1.Why do ROI pooling on feature maps and not do ROI pooling on the original image?

- taking maximum response of feature makes a lot of sense, taking maximum local intensity may not make sense

2.why not rescale all the image to the same size?

- computational efficiency
- some reasons can become more obvious when we study region proposal network